

# $E0$ transition strength from $X(5)$ to the rigid rotor

Andreas Krugmann



- ▶ Motivation
- ▶ Introduction to CBS rotor model
- ▶ Relative  $E0$  transition strength
- ▶ Evolution of absolute  $E0$  transition strength
- ▶  $E2 - E0$  correlation observables
- ▶ Summary

SFB 634

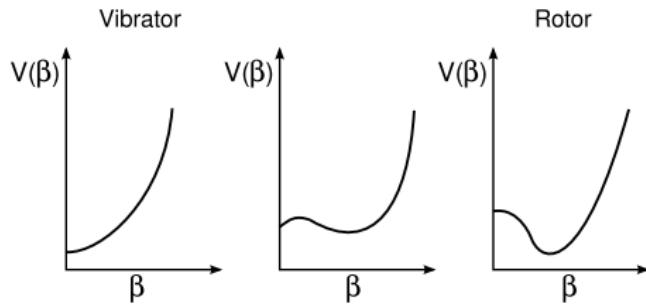


J. Bonnet, A. Krugmann, J. Beller, N. Pietralla, and R. V. Jolos  
Phys. Rev. C **79**, 034307 (2009)

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ökonomischer Exzellenz

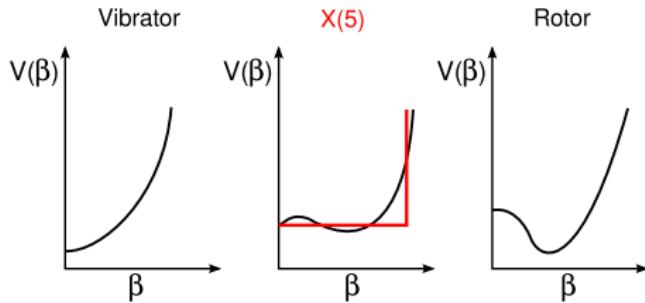
# Motivation

- With increasing  $A$ , heavy nuclei can undergo rapid quantum phase transitions



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- Geometrical collective solution of the Bohr Hamiltonian:

$$H = -\frac{\hbar^2}{2B} \left[ \frac{1}{\beta^4} \frac{\partial}{\partial \beta} \beta^4 \frac{\partial}{\partial \beta} + \frac{1}{\beta^2 \sin 3\gamma} \frac{\partial}{\partial \gamma} \sin 3\gamma \frac{\partial}{\partial \gamma} - \frac{1}{4\beta^2} \sum_k \frac{Q_k^2}{\sin^2(\gamma - \frac{2}{3}\pi k)} \right] + V(\beta, \gamma)$$

- Parameter free square well potential
- Analytical wave functions (Bessel functions)

# Motivation

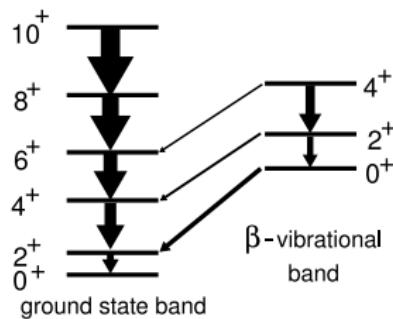
- ▶ Calculate level scheme for X(5) solution

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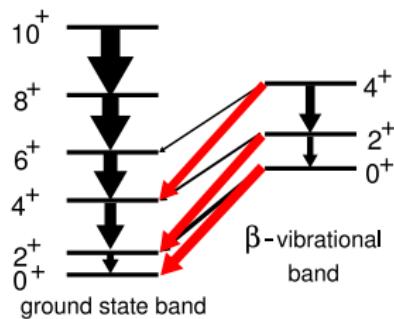
$$R_{4/2} = \frac{E(4_1^+)}{E(2_1^+)} = 2.90$$



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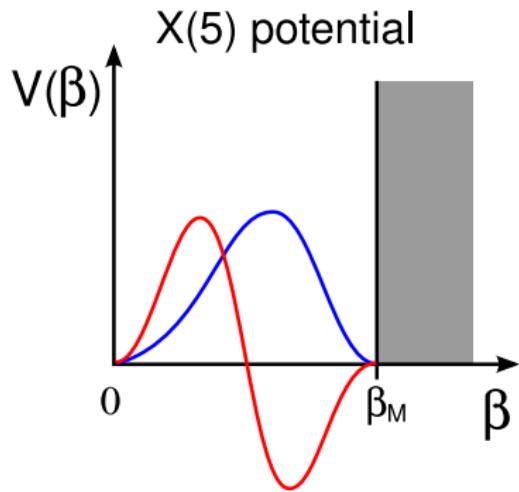


- ▶ High  $E0$  (electric monopole) transition strengths in case of shape change

# Confined $\beta$ -soft (CBS) rotor model



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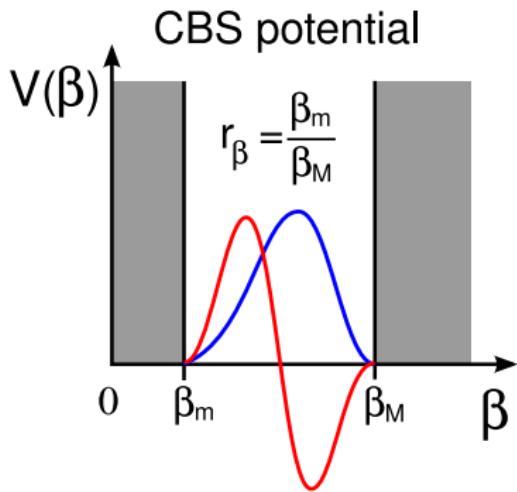


F. Iachello,  
Phys. Rev. Lett. **87**, 052502 (2001)

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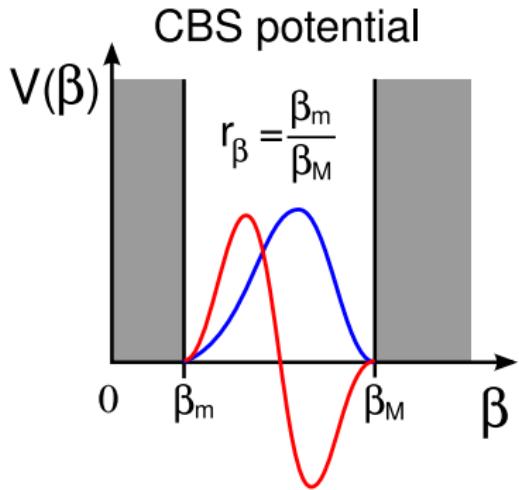


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N.Pietralla and O.M.Gorbachenko,  
Phys.Rev. C **70**, 011304 (2004)

# Confined $\beta$ -soft (CBS) rotor model



N.Pietralla and O.M.Gorbachenko,  
Phys.Rev. C **70**, 011304 (2004)

- ▶ Wave functions are **confined** in a  $\beta$ -**soft** potential
- ▶ Potential stiffness is defined as
$$r_\beta = \frac{\beta_m}{\beta_M}$$
$$r_\beta = 0 \rightarrow X(5)$$
$$r_\beta = 1 \rightarrow \text{rigid rotor}$$
Typical values between 0.1 ( $^{150}\text{Nd}$ ) and 0.5 (well deformed nuclei)
- ▶ Study  $E0$  transition strengths on the path from  $X(5)$  to the well deformed nuclei

# $E0$ operator and $E0$ transition strength

- ▶  $E0$  operator for axially symmetric quadrupole deformation:

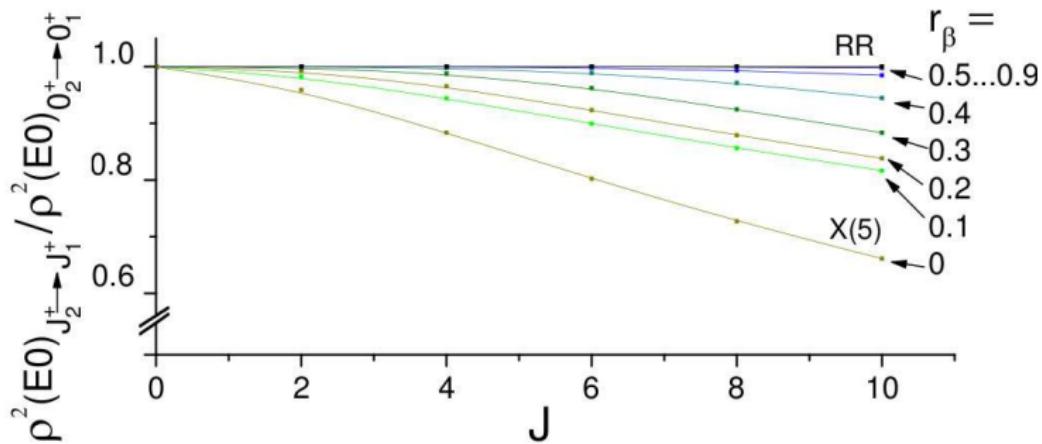
$$T(E0) = \frac{3}{4\pi} ZeR^2\beta^2$$

- ▶  $E0$  transition strength:

$$\rho^2(E0) = \left(\frac{3Z}{4\pi}\right)^2 |\langle\psi_f|\beta^2|\psi_i\rangle|^2$$

- ▶  $\rho^2(E0)$  is a dimensionless quantity
- ▶ The largest values are around  $100 \cdot 10^{-3} = 0.1$

# Angular momentum dependence of relative E0 transition strength

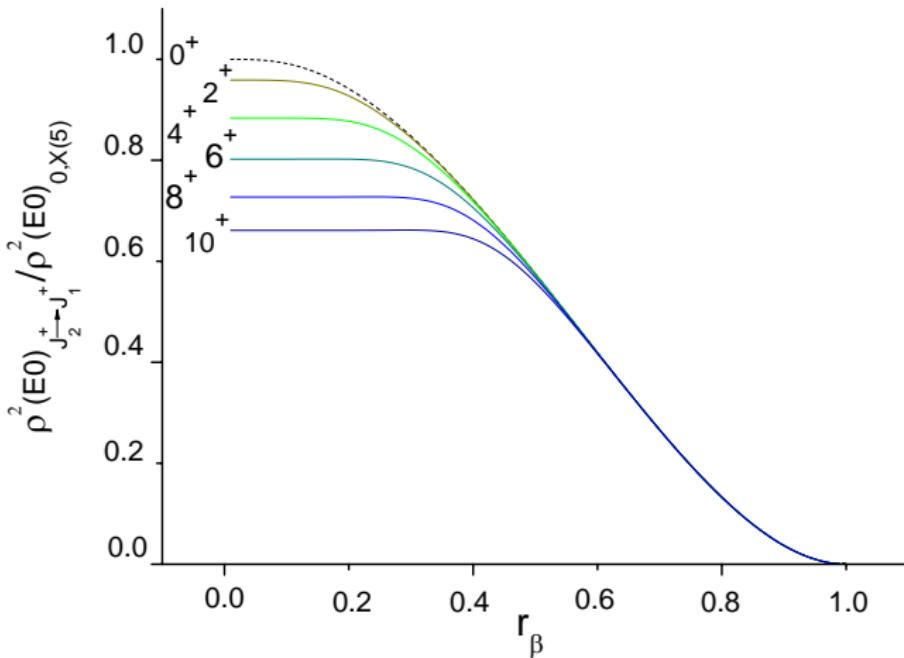


- ▶ For increasing angular momentum the model predicts a decreasing  $E0$  transition strength.
- ▶ Rising potential stiffness  $\rightarrow E0$  strength approach a constant value.

# Evolution of absolute $E0$ transition strength



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## $E2 - E0$ correlation observables

- ▶ Rasmussen introduced the  $Z$ -independent quantity

$$X_{Rasm} = \frac{\rho^2(E0; 0_2^+ \rightarrow 0_1^+) e^2 R^4}{B(E2; 0_2^+ \rightarrow 2_1^+)}$$

- ▶ In the rigid rotor limit he obtained:  $X_{Rasm} = 4\beta^2$
- ▶ In the CBS model we get the expression:

$$X_{CBS} = \frac{\langle \Psi_{0_1^+} | T(E0) | \Psi_{0_2^+} \rangle^2 \beta_M^2}{\langle \Psi_{2_1^+} | T(E2) | \Psi_{0_2^+} \rangle^2}$$

- ▶ With the CBS model, we can trace the evolution of  $X$  as a function of nuclear stiffness!
- ▶ But still dependence of scaling factor  $\beta_M$

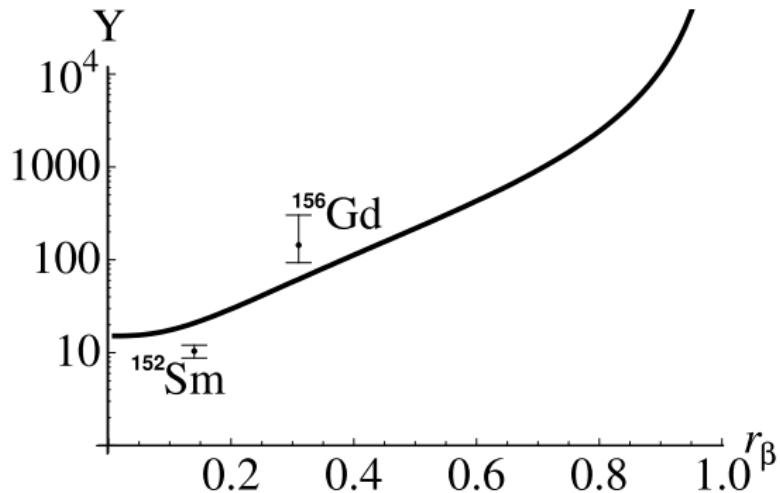
# New scaling-factor independent quantity $Y$



$$\begin{aligned} Y &= \frac{\rho^2(0_2^+ \rightarrow 0_1^+) (e^2 R^4 Z)^2 (\frac{3}{4\pi})^2}{B(E2, 0_2^+ \rightarrow 2_1^+)^2} \\ &= \frac{\langle \Psi_{0_1^+} | T(E0) | \Psi_{0_2^+} \rangle^2}{\langle \Psi_{2_1^+} | T(E2) | \Psi_{0_2^+} \rangle^4} \end{aligned}$$

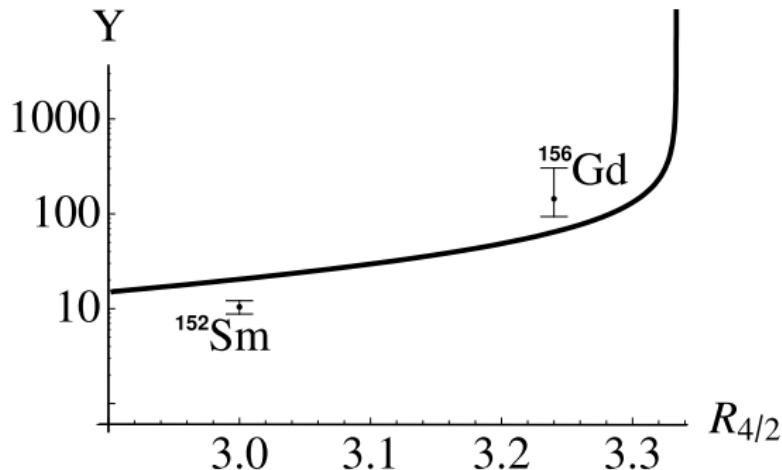
- ▶  $Y$  theoretically depends **only** on the stiffness parameter  $r_\beta$ .

# Ratio $Y$ as a function of $r_\beta$



- ▶  $Y$  increases monotonically with the stiffness parameter  $r_\beta$ ...

# Ratio $Y$ as a function of the $R_{4/2}$ ratio



- ... and increases with the  $R_{4/2}$  ratio too.

# Summary

- ▶ Successful investigation of E0 transition strength in the CBS model
- ▶ Relative  $E0$  strength (for a given  $r_\beta$ ) decrease with angular momentum.
- ▶ Absolute  $E0$  transition strength decrease with increasing potential stiffness  $r_\beta$ .
- ▶ A new observable  $Y \propto \rho^2(E0; 0_2^+ \rightarrow 0_1^+)/B(E2; 0_2^+ \rightarrow 2_1^+)^2$  has been proposed
  - ▶ is independent of the absolute nuclear deformation
  - ▶ solely depends on the nuclear stiffness.
- ▶ The few available data are in reasonable agreement with the CBS model.

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- ▶ The few available data are in reasonable agreement with the CBS model.
- ▶ **Outlook:** More data needed!  
Measure E0 matrix elements with inelastic electron scattering at S-DALINAC

# Thank you for your attention!



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- ▶ Thanks to J. Bonnet, N. Pietralla, R. V. Jolos, J. Beller, F. Iachello, K. Heyde, P. von Brentano, G. Rainovski, and O. Möller.
- ▶ Supported by the DFG under Grant No. SFB 634 and by the Helmholtz International Center for FAIR

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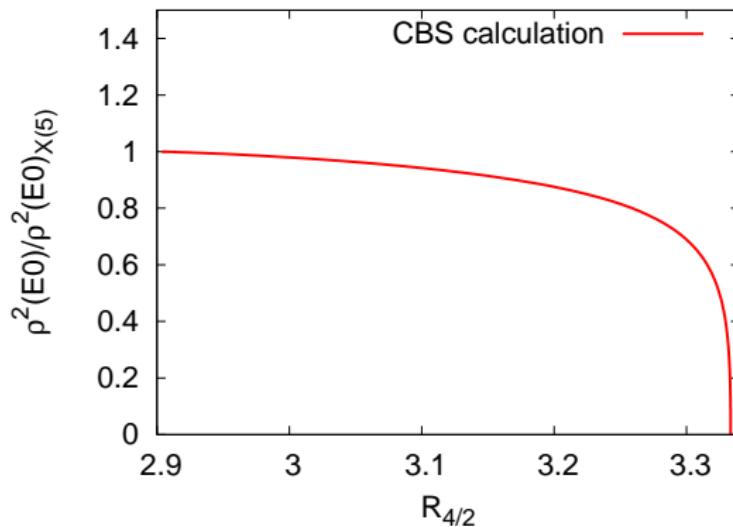
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# Additional content

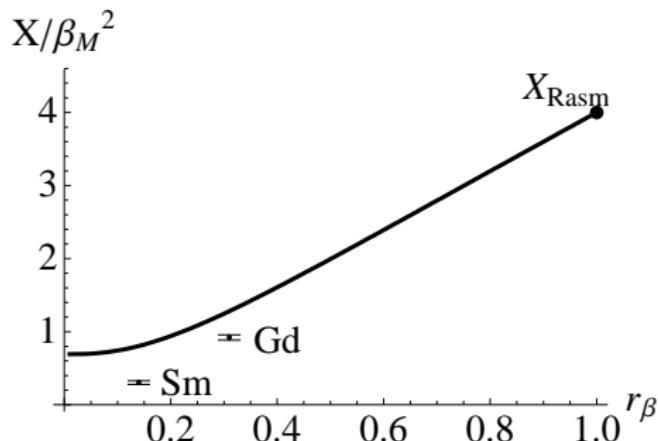
# Absolute E0 strength as a function of $R_{4/2}$



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# Evolution of $X$ as a function of nuclear stiffness



- ▶ Verification of Rasmussens prediction in the rigid rotor limit:  $X_{Rasm} = 4\beta^2$
- ▶ But still dependence of scaling factor  $\beta_M$

# Stiffness dependence of relative $E0$ strength



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