

# Complete Dipole Strength Distributions from High-Resolution Polarized Proton Scattering at $0^\circ$



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- Complete electric dipole strength distributions  
- what can be learned
- High-resolution polarized proton scattering as a spectroscopic tool
- The case of  $^{208}\text{Pb}$

SFB 634



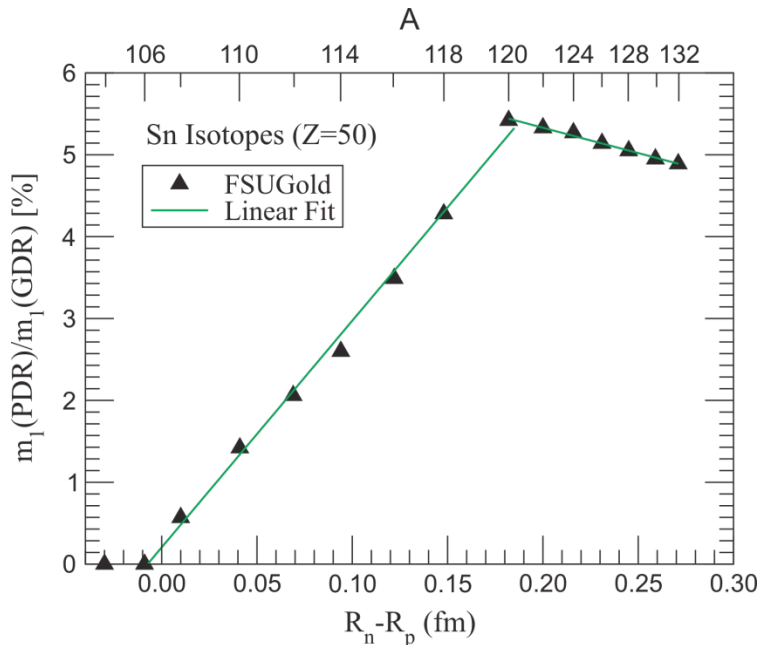
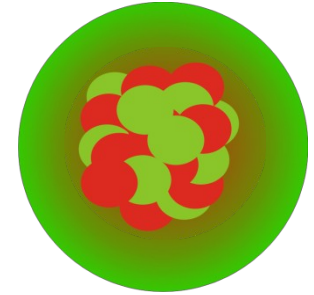
\*Supported by the DFG within SFB 634 and 446 JAP 113/267/0-2

# Complete Dipole Strength: What can be Learned?

- Pygmy dipole resonance (PDR)
  - Dipole polarizability
  - Level densities
  - Photon strength function
- Test of microscopic models
- Neutron skin and symmetry energy
- Test of Hauser-Feshbach approach in large-scale reaction network calculations
- Test of Axel-Brink hypothesis

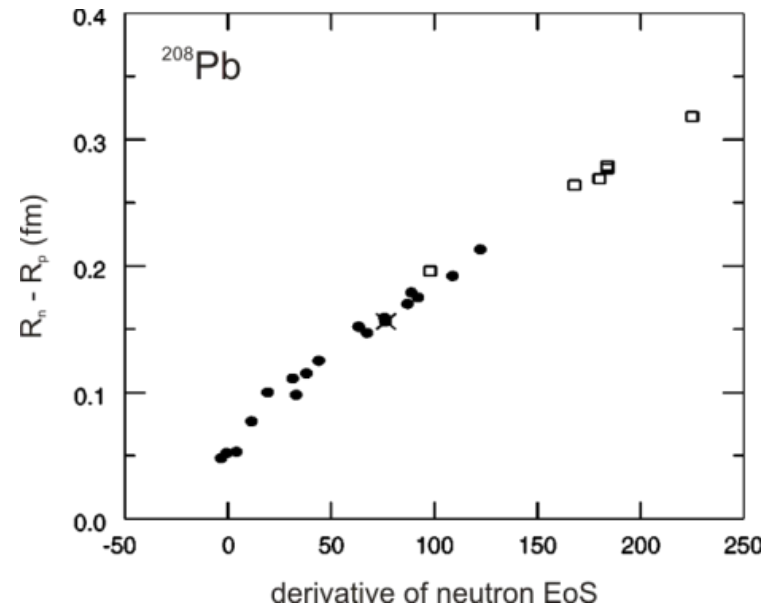
# Pygmy Dipole Resonance

- Soft E1 mode due to oscillation of neutron skin vs. approximately isospin-saturated core
- PDR strength related to neutron skin



J. Piekarewicz, PRC 73 (2006) 044325.

- Neutron skin related to neutron-matter EOS



S. Typel, B. A. Brown, PRC 64 (2001) 027302

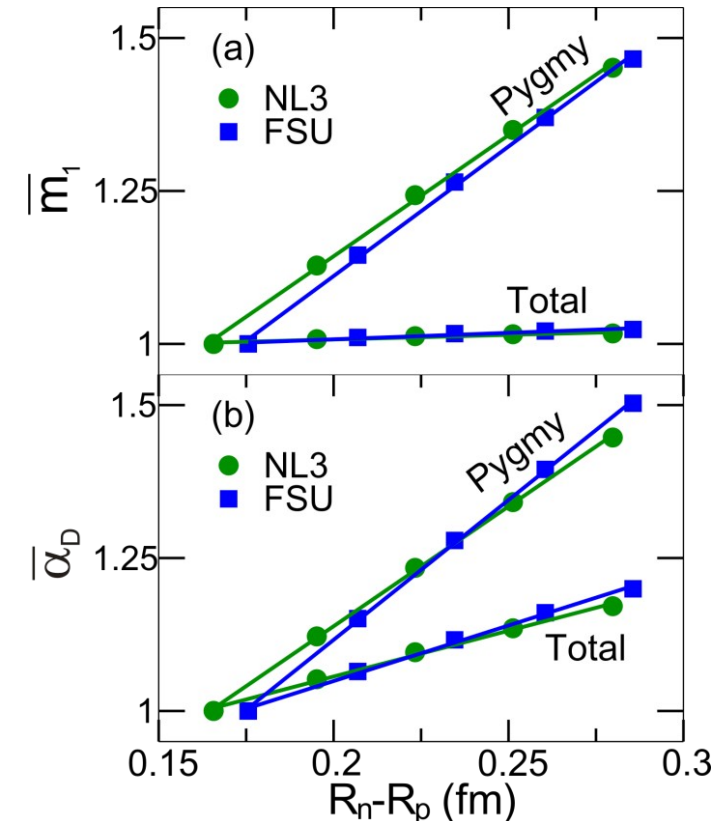
# Polarizability

- Static nuclear dipole polarizability

$$\alpha_D = \frac{\hbar c}{2\pi^2 e^2} \cdot \sigma_{-2} = \frac{\hbar c}{2\pi^2 e^2} \cdot \sum \frac{\sigma_{abs}(E_x)}{E_x^2} = \frac{8\pi}{9} \cdot \sum \frac{B(E1)(E_x)}{E_x} \left[ fm^3 / e^2 \right]$$

- $\alpha_D$  is measure of neutron skin

P.G. Reinhard, W. Nazarewicz,  
PRC 81 (2010) 051303 (R)



J. Piekarewicz, arXiv:1012.1803

- Statistical model approach to reaction cross sections in astrophysical large-scale network calculations
  
- Required input
  - Photon strength function
  - Level densities
  - Axel-Brink hypothesis (thermal population of excited states)

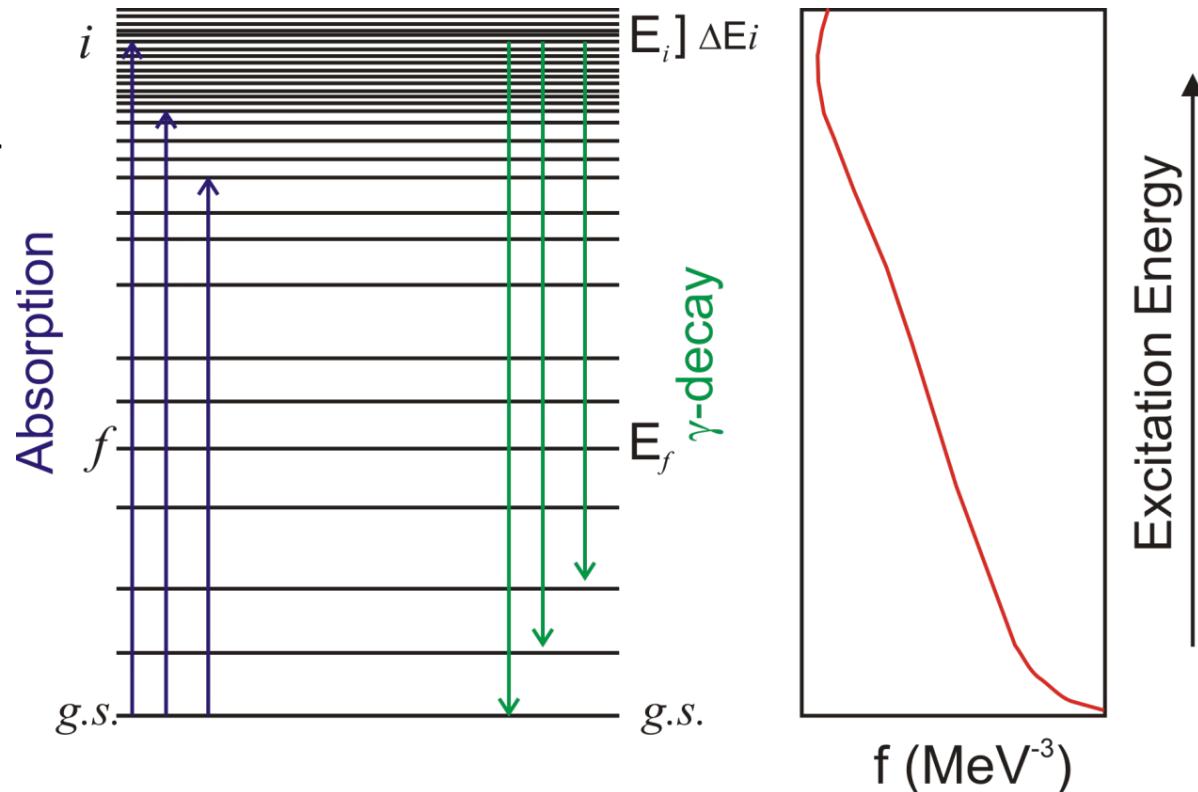
# Photon Strength Function (PSF)

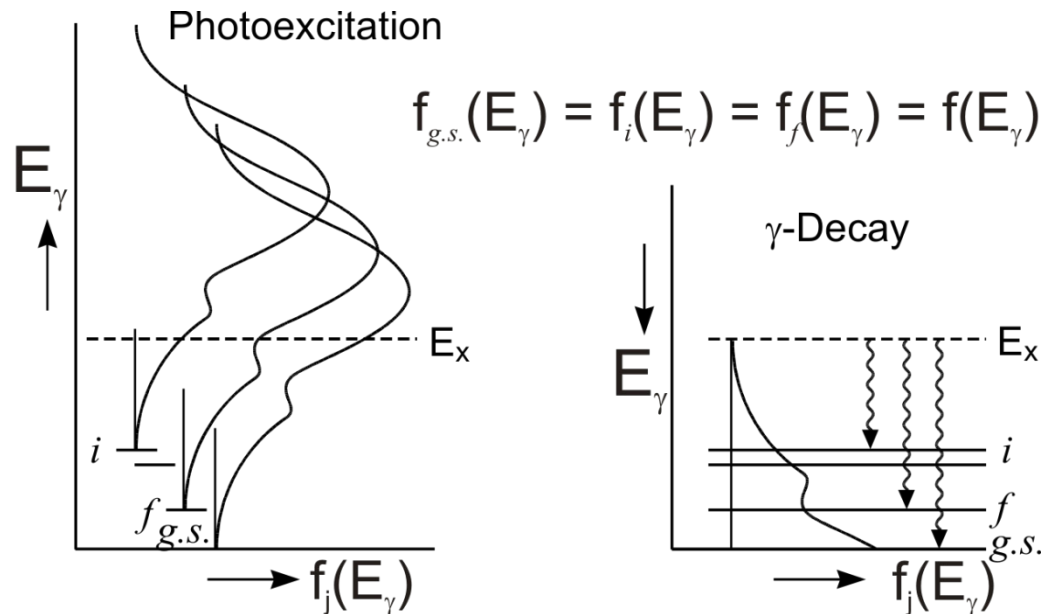
$$\langle \Gamma(E_i) \rangle = \frac{1}{\rho(E_i)} \cdot \int_0^{E_i} E_\gamma^3 f^{E1}(E_\gamma) \rho(E_i - E_\gamma) dE_\gamma$$

$$\langle \Gamma_{i \rightarrow g.s.} \rangle = \frac{f^{E1}(E_\gamma) \cdot E_\gamma^3}{\rho(E_i)}$$



$$f^{E1}(E_\gamma) = \frac{\sigma_{abs}(E_i)}{3(\pi \hbar c)^2 \cdot E_\gamma}$$



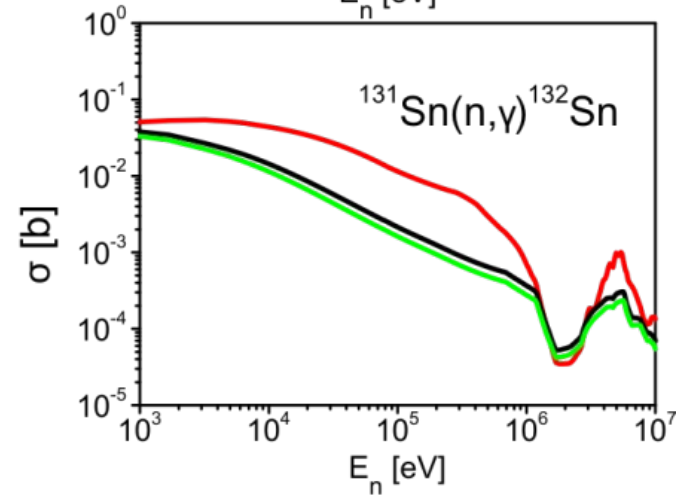
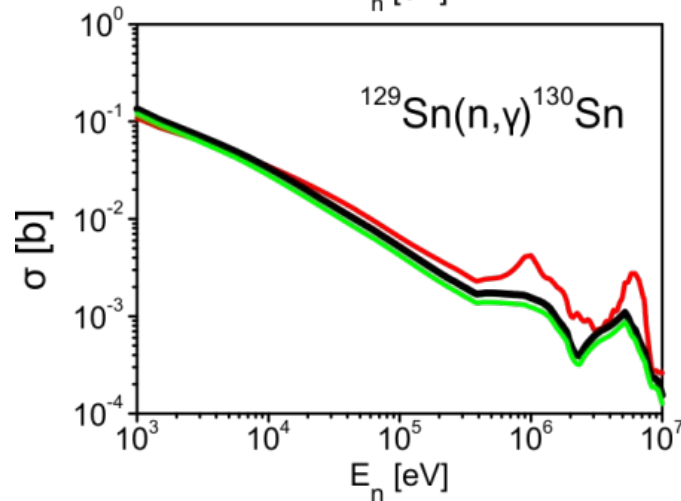
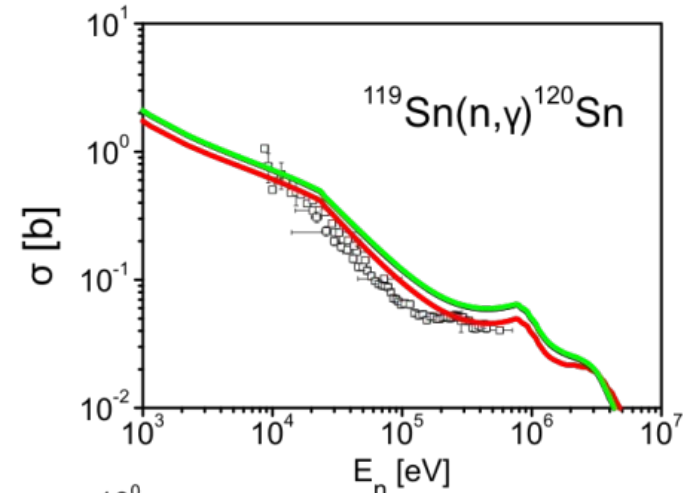
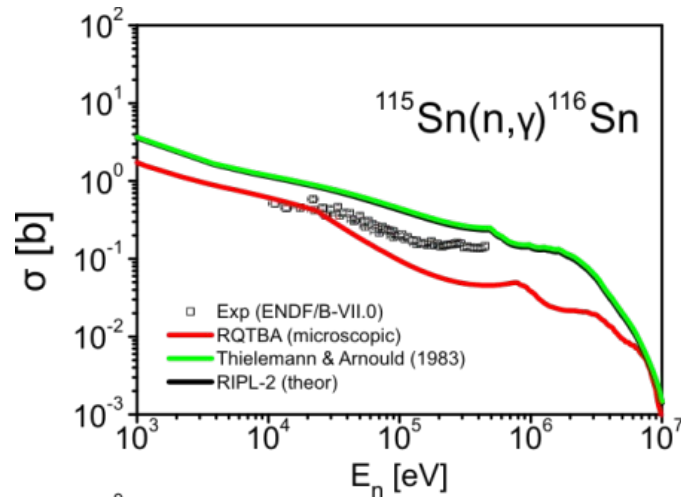


## ■ Strength

- depends only on  $E_\gamma$
- is independent of the initial state structure:  $E_x, J^\pi, \dots$

## ■ Same PSF for $\gamma$ absorption and emission

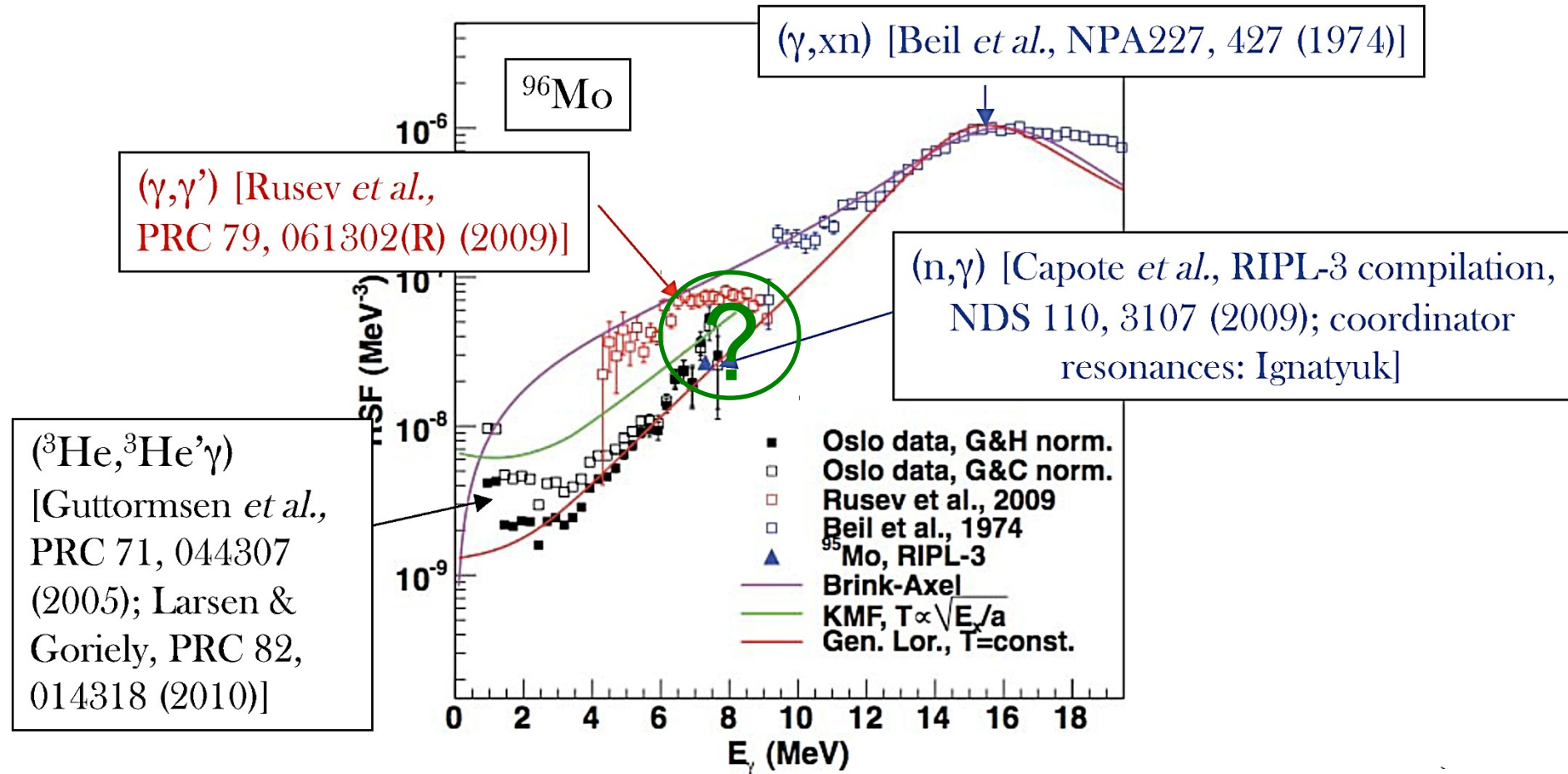
# Influence of the PDR



E. Litvinova, Workshop on Gamma Strength and Level Density, Dresden-Rossendorf, August 2010  
E. Litvinova et al., NPA 823 (2009) 26



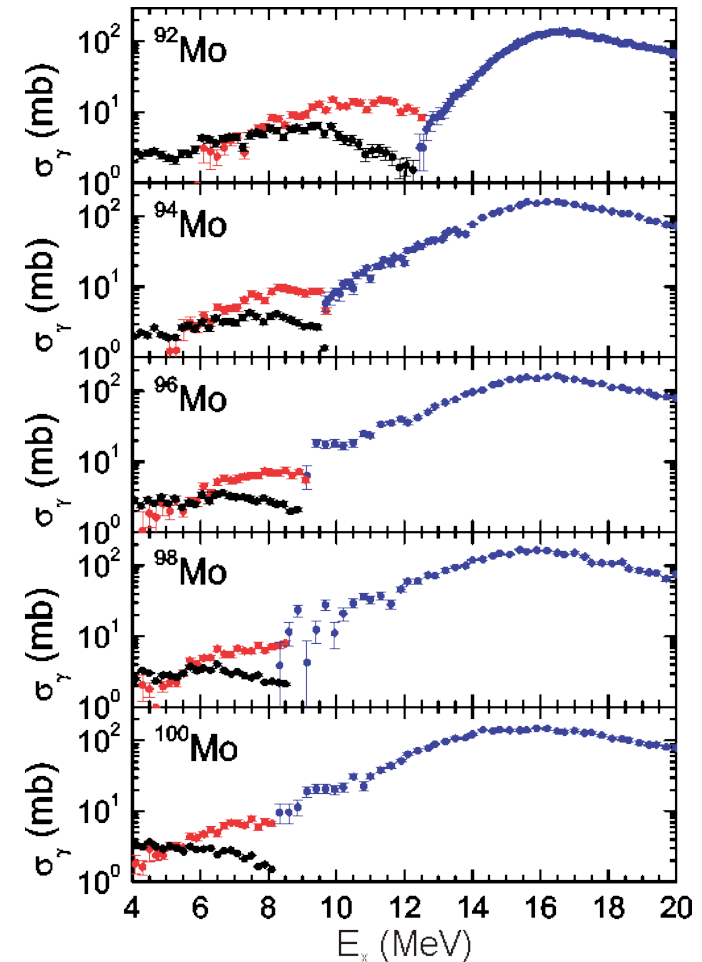
# Experimental Discrepancies in PSF



Ann-Cecilie Larsen, Workshop on Gamma Strength and Level Density, Dresden-Rossendorf, August 2010

# Problems

- Experimental:
  - $(\gamma, \gamma')$  reaction measures strength (roughly) up to threshold only
  - Experimental quantity  $\propto \Gamma_0 \cdot \frac{\Gamma_0}{\Gamma}$ 
    - assumption in most analyses
$$\frac{\Gamma_0}{\Gamma} = 1 \rightarrow \text{lower limit}$$
    - alternatively correction with statistical model calculation → upper limit



G. Rusev et al., PRC 79 (2009) 061302

- $(\gamma, xn)$  reactions provide information above threshold only and little sensitivity close to threshold
- Decay of compound nuclei
  - normalization at  $S_n$
  - level densities needed



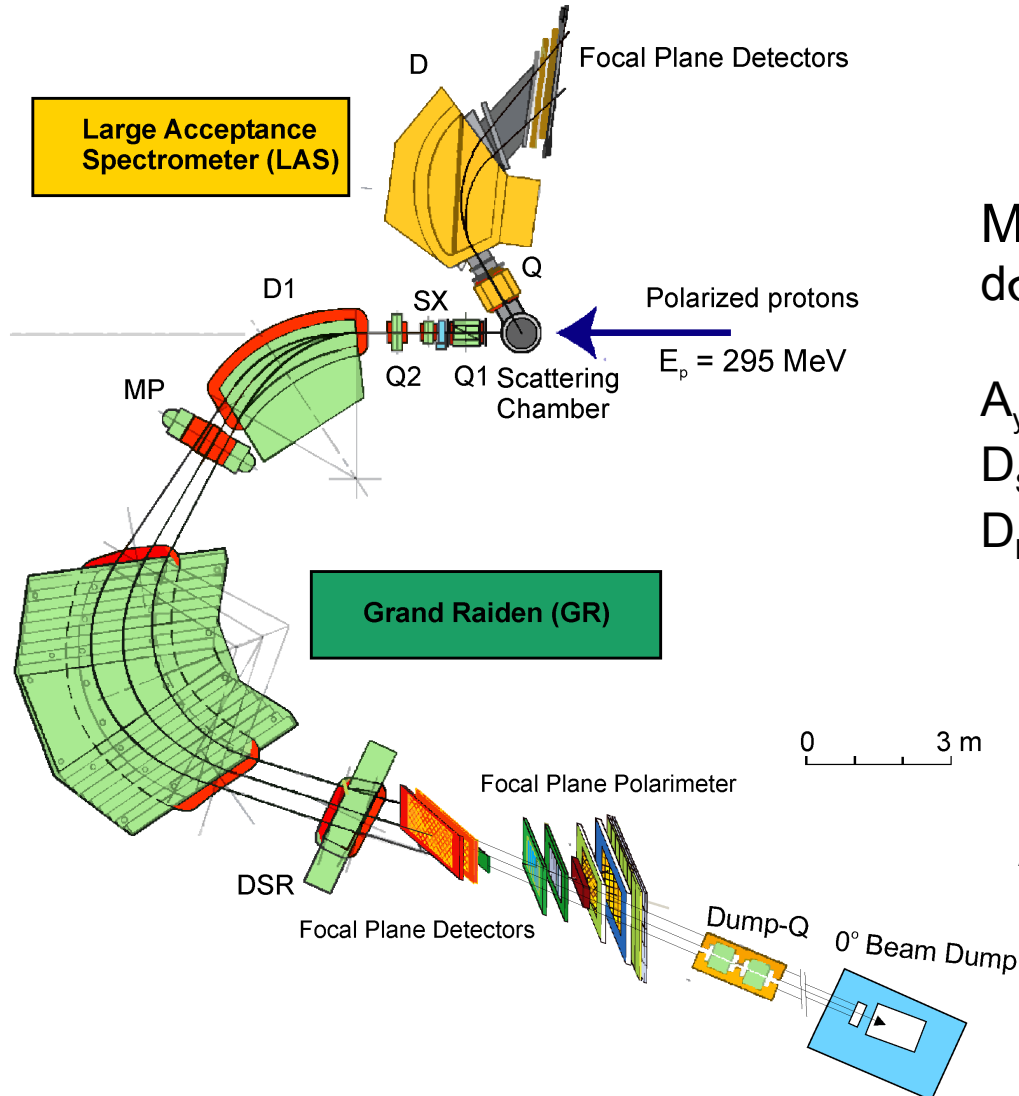
Consistent data on E1 strength below and above the neutron threshold highly important

# A New Experimental Tool for Complete Dipole Strength Distributions



- Polarized proton scattering at  $0^\circ$ 
  - intermediate energy: **300 MeV** optimal for spin/isospin excitations
  - Coulomb excitation of  $1^-$  states
  - high resolution:  $\Delta E =$  **25 keV** (FWHM)
  - angular distributions: **E1 / M1** separation
  - polarization observables: **spinflip / non-spinflip** separation
  
- $^{208}\text{Pb}$  as a reference case

# 0° Setup at RCNP



Measured observables

$d\sigma/d\Omega$  - angular distributions  
( $0^\circ \leq \Theta \leq 10^\circ$ )

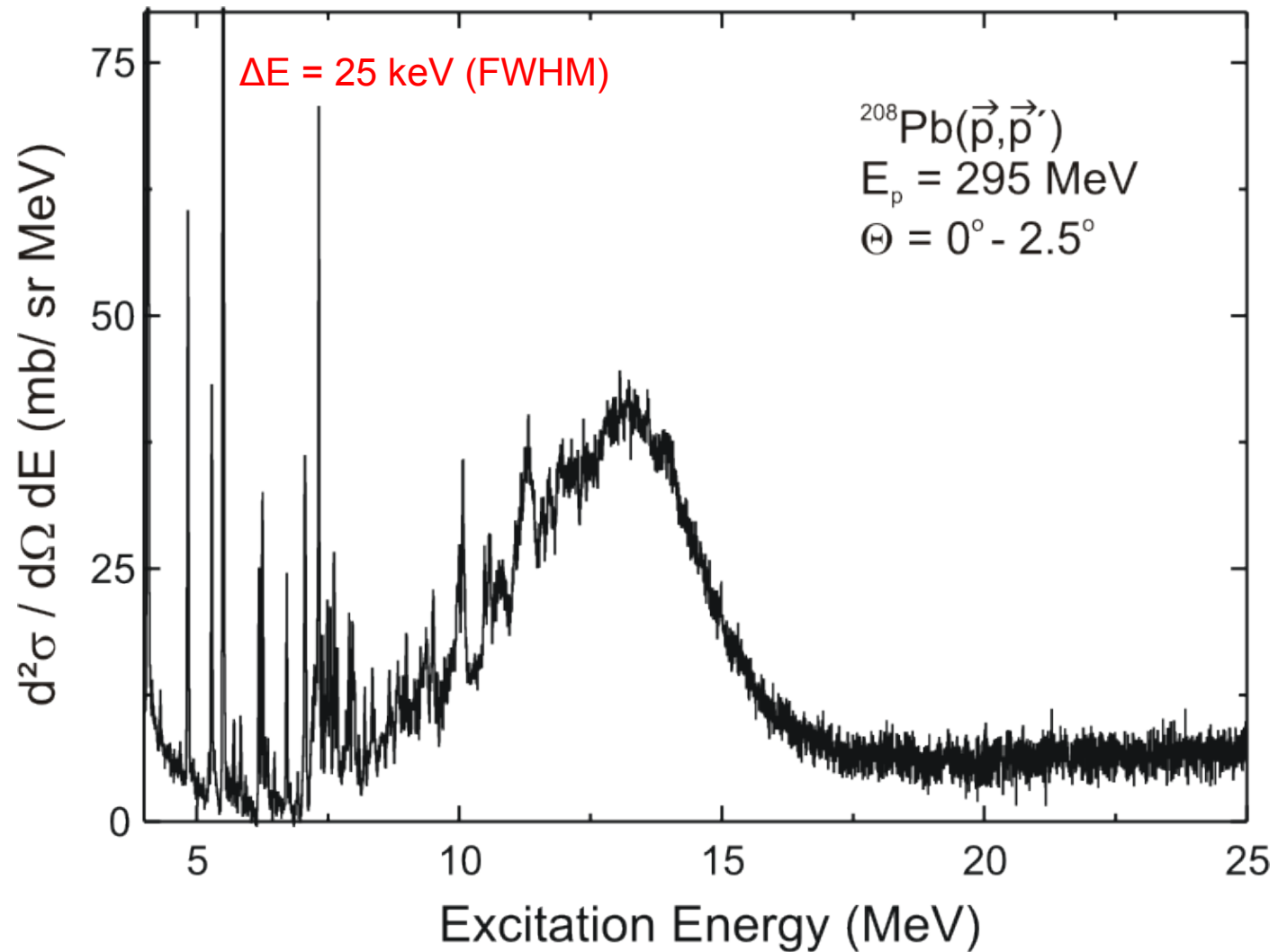
$A_y$  - asymmetry

$D_{SS}$  at  $0^\circ$  - sideways polarization

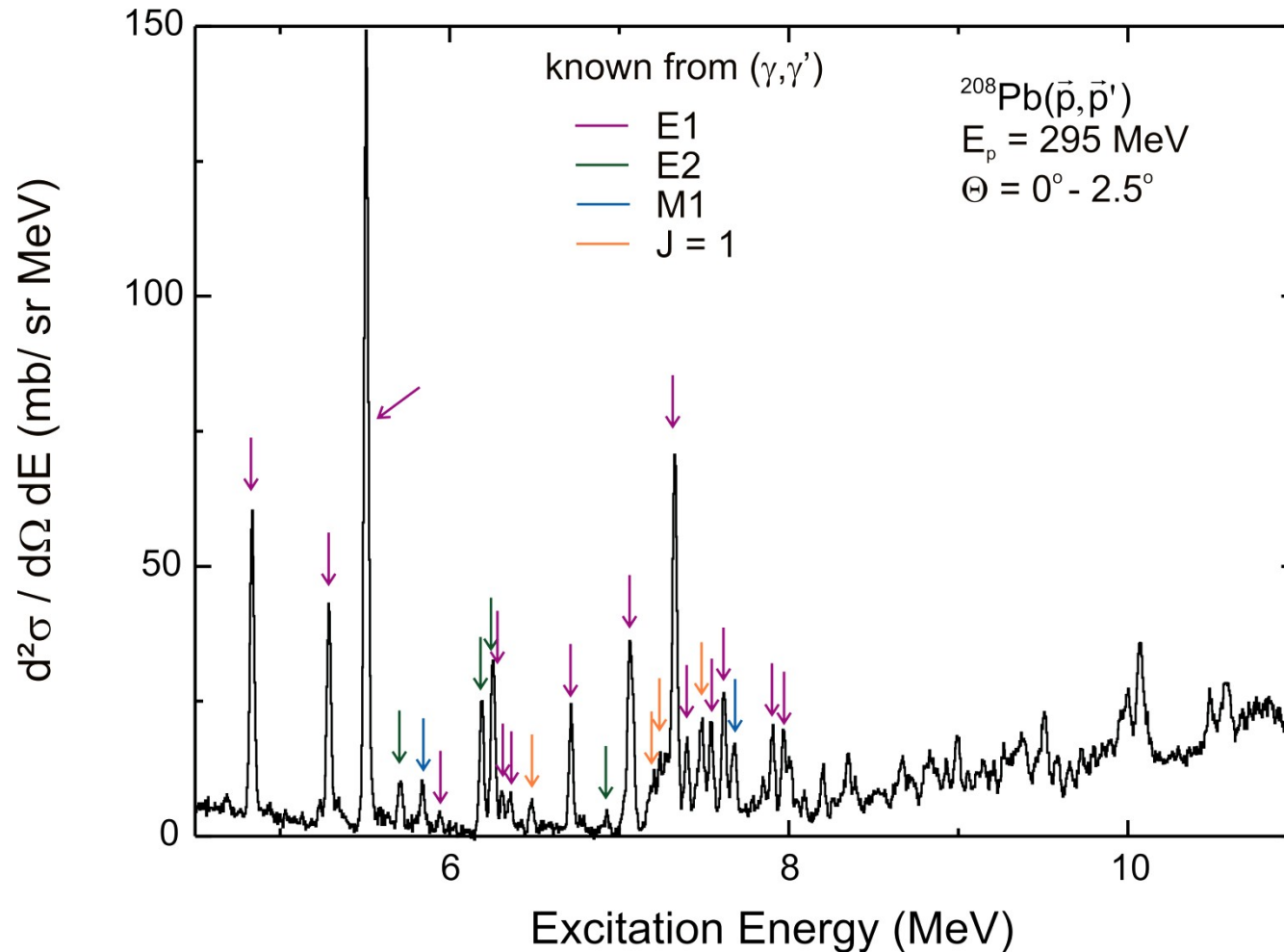
$D_{LL}$  at  $0^\circ$  - longitudinal polarization

A. Tamii et al., NIMA 605 (2009) 326

# Measured Spectrum



# Measured Spectrum: Low-Energy Part



- All dipole transitions known from  $(\gamma, \gamma')$  are observed

# E1/M1 Decomposition by Spin Observables

Polarization observables at  $0^\circ$   $\longrightarrow$  **spinflip / non-spinflip separation\***  
(model-independent)

$$D_{SS} + D_{NN} + D_{LL} = \begin{cases} -1 & \text{for } \Delta S=1, \text{ M1 excitations} \\ 3 & \text{for } \Delta S=0, \text{ E1 excitations} \end{cases}$$

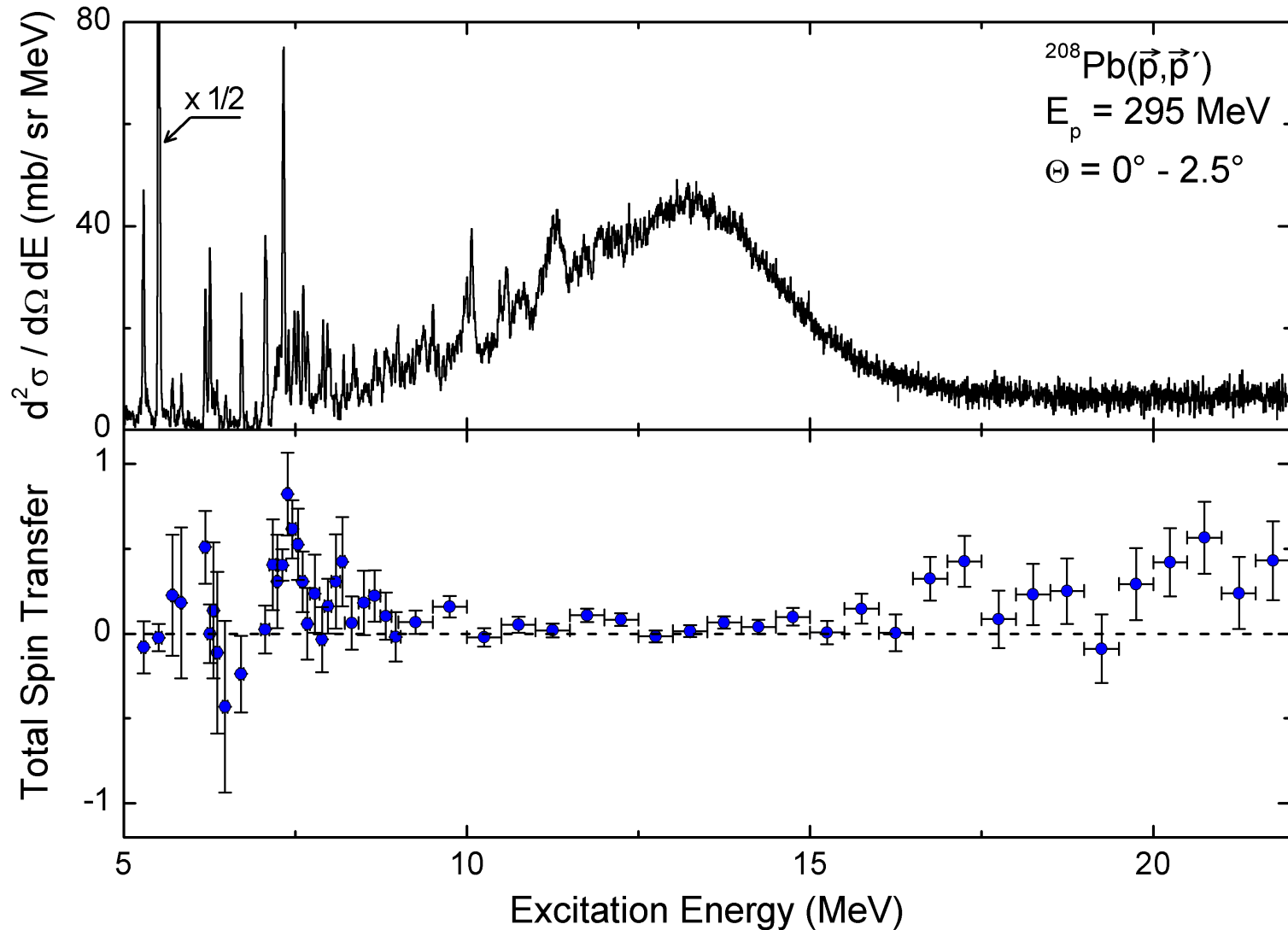
$\longrightarrow$  E1 and M1 cross sections can be decomposed

$$\text{At } 0^\circ \quad D_{SS} = D_{NN}$$

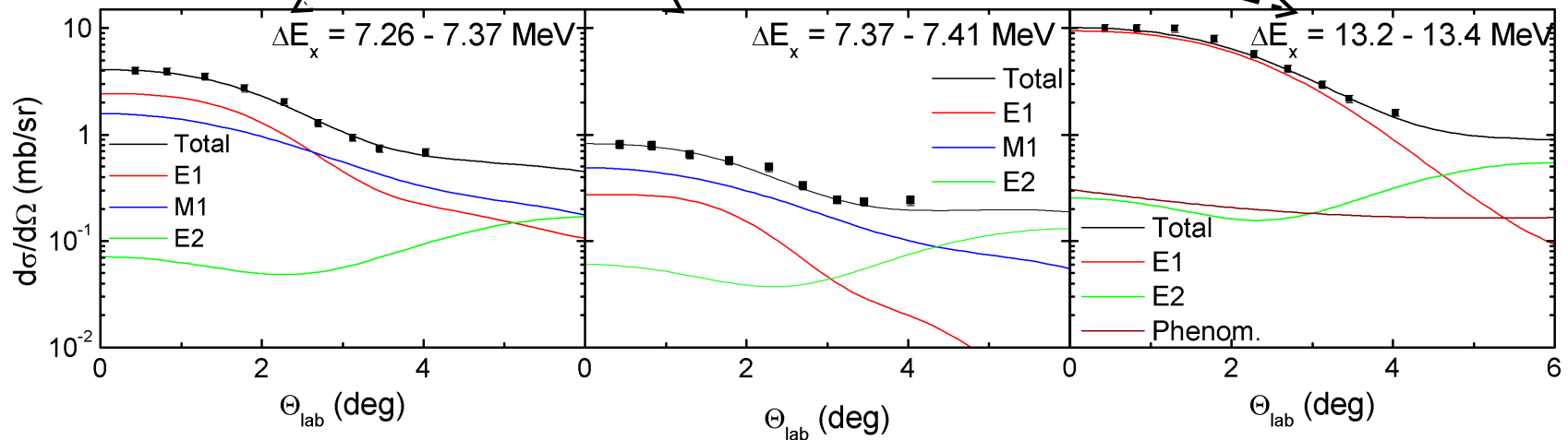
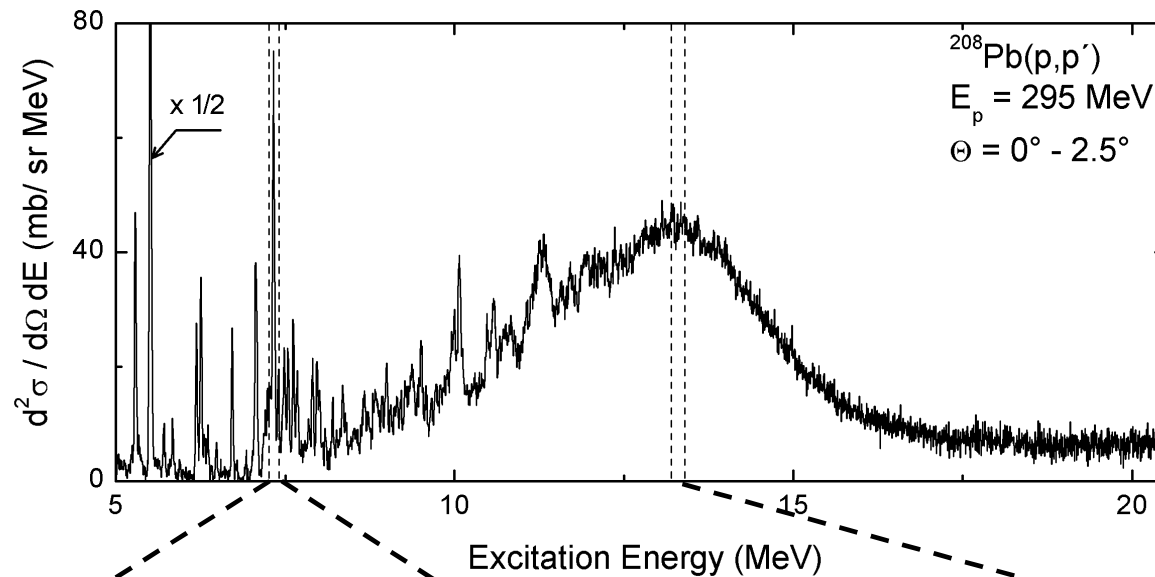
$$\text{Total Spin Transfer } \Sigma \equiv \frac{3 - (2 D_{SS} + D_{LL})}{4} = \begin{cases} 1 & \text{for } \Delta S = 1 \\ 0 & \text{for } \Delta S = 0 \end{cases}$$



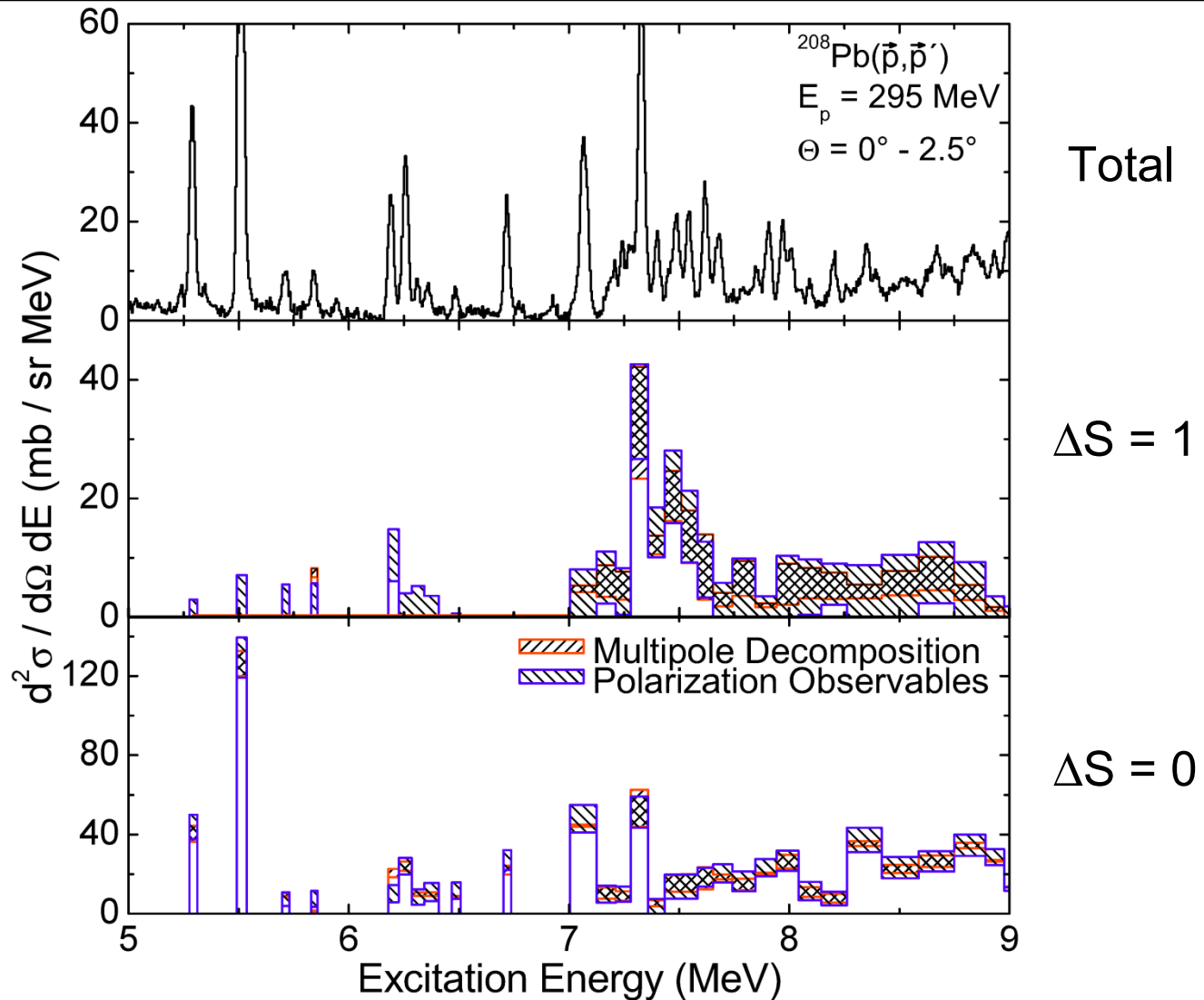
# Decomposition into Spinflip / Non-Spinflip Cross Sections



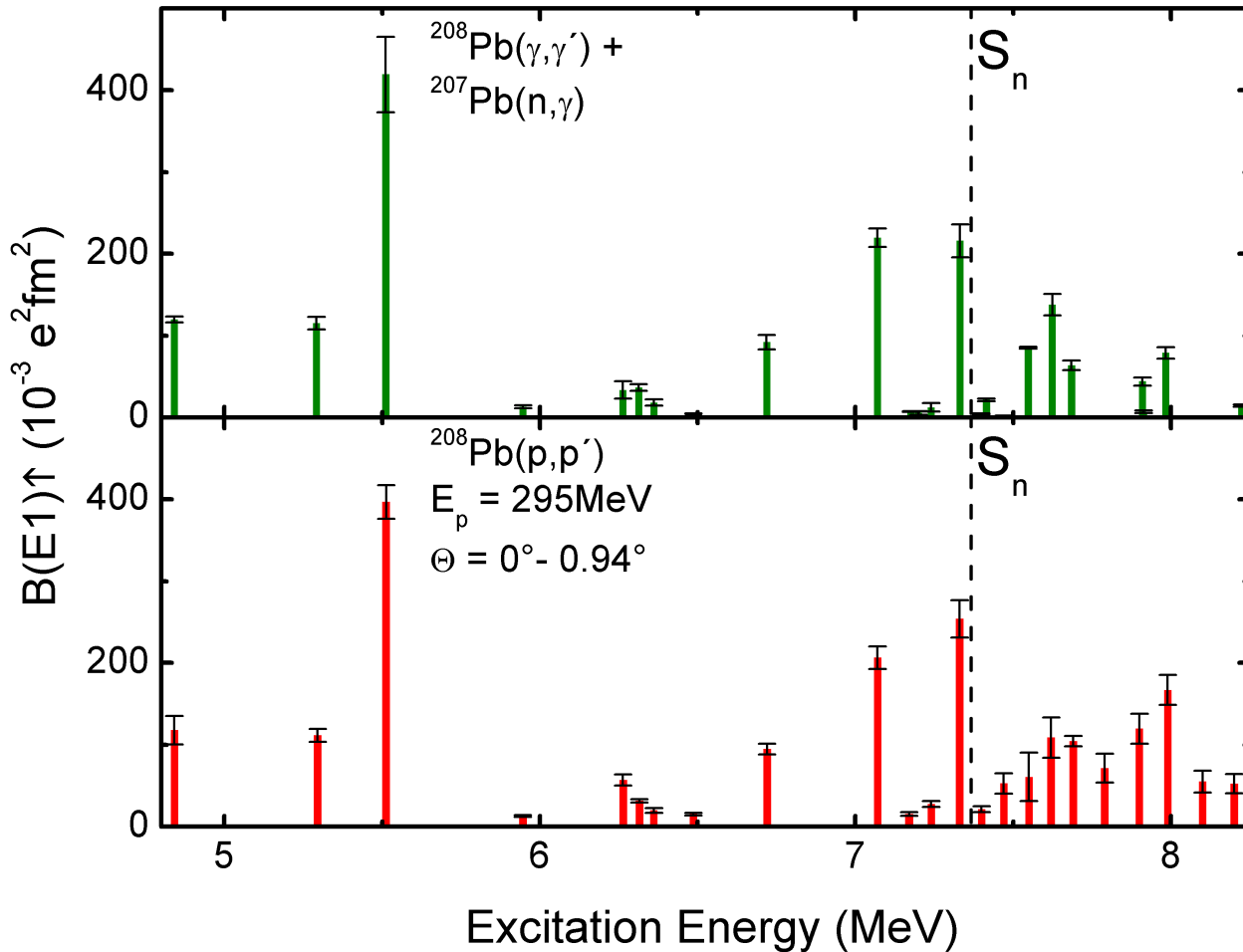
# Multipole Decomposition of Angular Distributions



# Comparison of Both Methods



# B(E1) Strength: Low-Energy Region



$$\sum_{E_x=6.2\text{MeV}}^{8.2\text{MeV}} B(E1) \uparrow = 1.10 \pm 0.11 \text{ e}^2\text{fm}^2$$

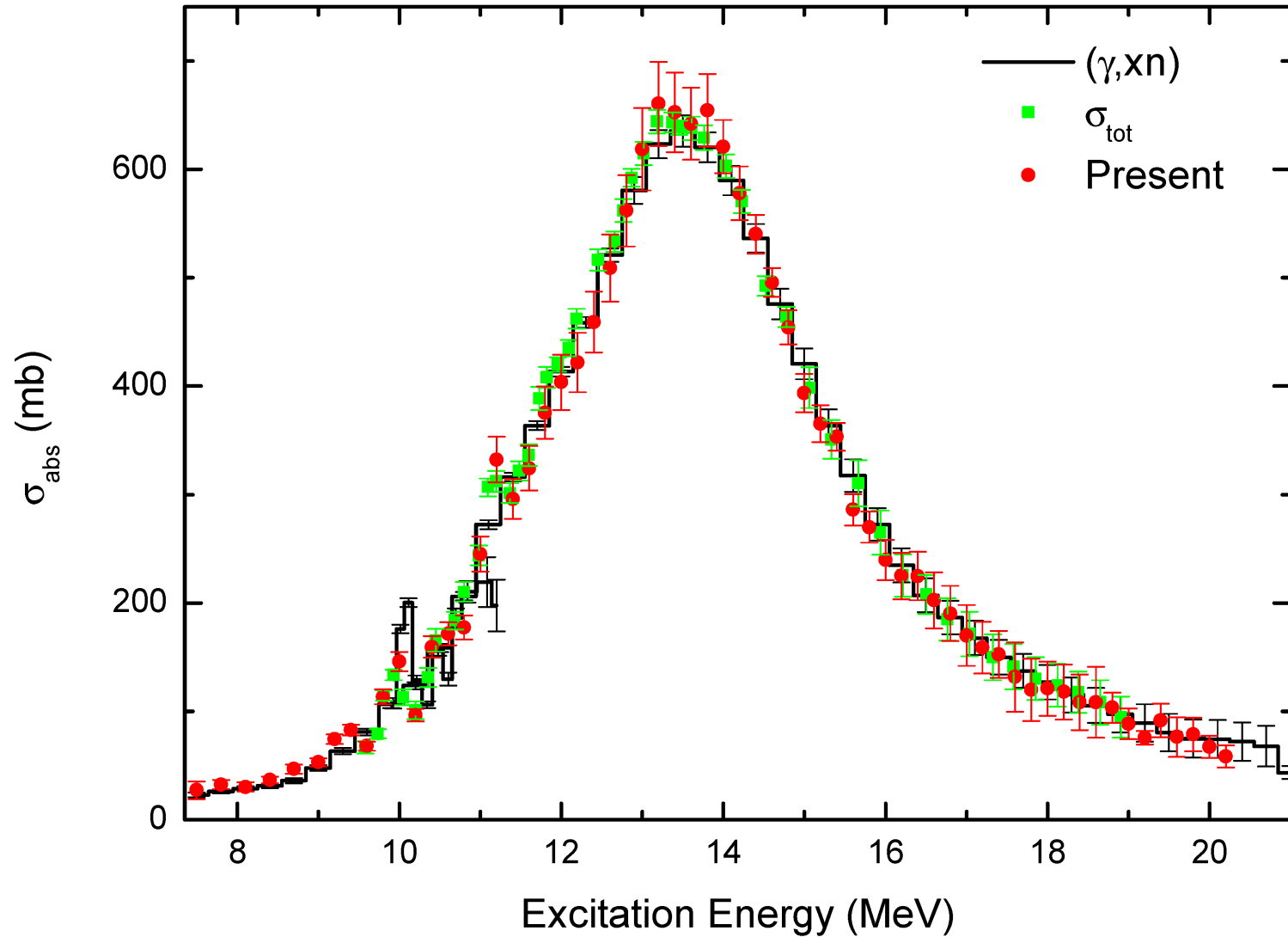
$$E_c = 7.30 \pm 0.03 \text{ MeV}$$

$$\sum_{E_x=6.2\text{MeV}}^{8.2\text{MeV}} B(E1) \uparrow = 1.54 \pm 0.16 \text{ e}^2\text{fm}^2$$

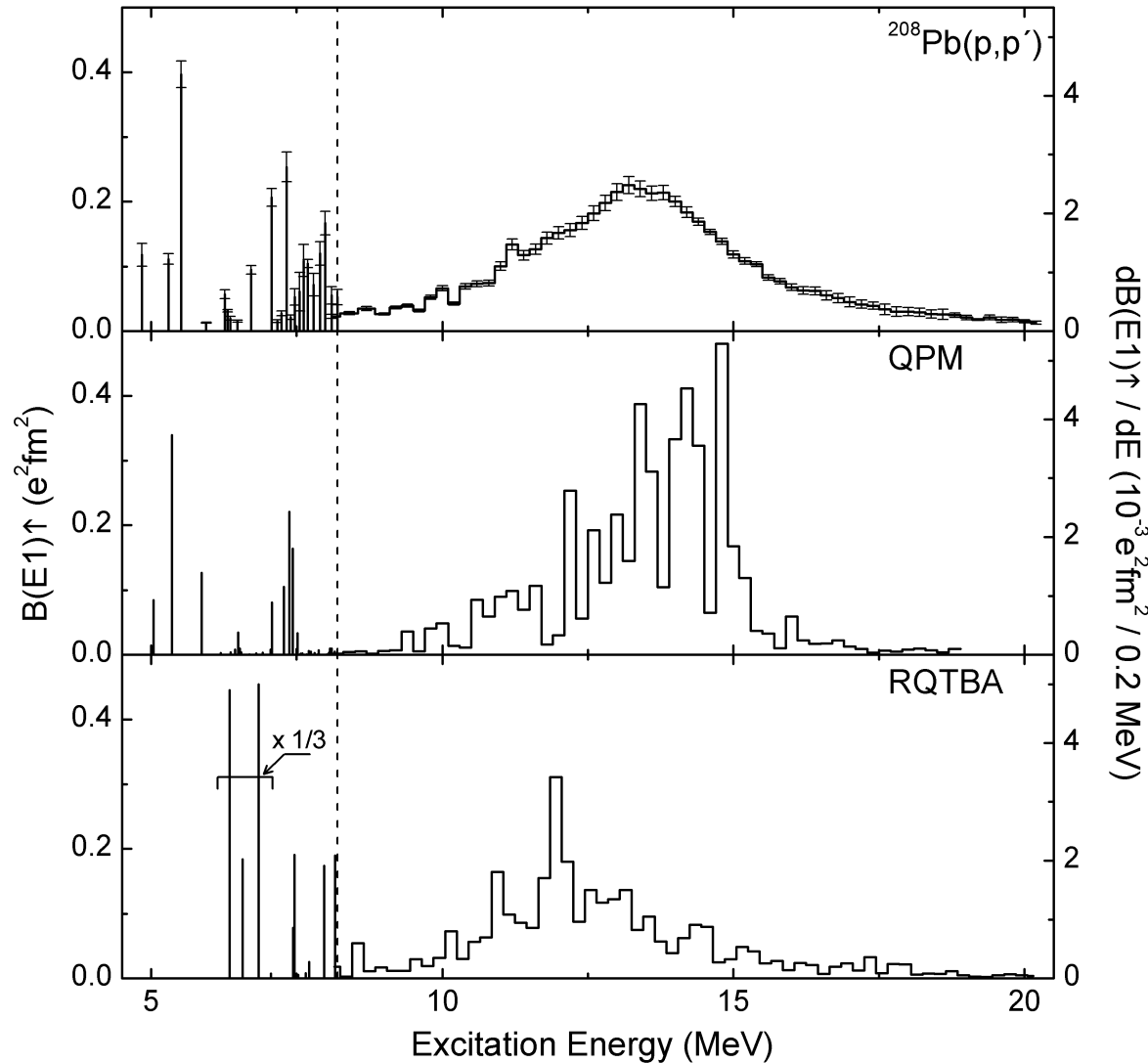
$$E_c = 7.43 \pm 0.02 \text{ MeV}$$

- Extracted assuming semiclassical Coulomb excitation

# B(E1) Strength: GDR



# E1 Response in $^{208}\text{Pb}$ : Experiment vs. Theory



V.Yu. Ponomarev  
3p3h ( $E_x \leq 10 \text{ MeV}$ ), 2p2h for GDR

N. Ryezayeva et al., PRL 89 (2002)  
272502

E. Litvinova  
1p1h  $\otimes$  phonon

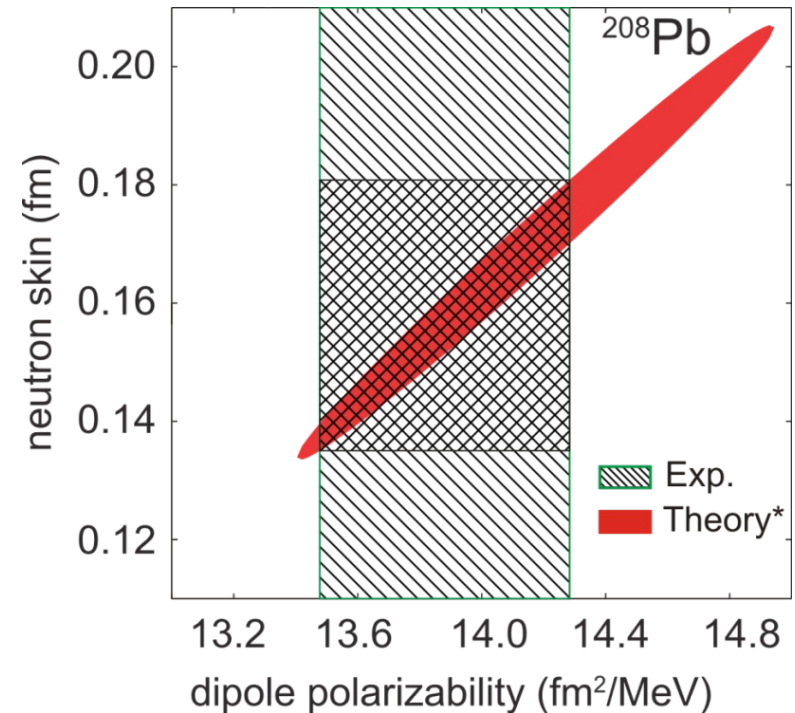
E. Litvinova et al., PRC 78 (2008)  
014312, PRC 79 (2009) 054312

# Polarizability and neutron skin

- Precision value:  $\alpha_D(^{208}\text{Pb}) = 19.98(58) \text{ fm}^3/\text{e}^2 = 13.88(41) \text{ fm}^2/\text{MeV}$

- Within the model of P.G. Reinhard and W. Nazarewicz, PRC 81 (2010) 051303

$\Rightarrow r_{\text{skin}} = 0.155(23) \text{ fm}$

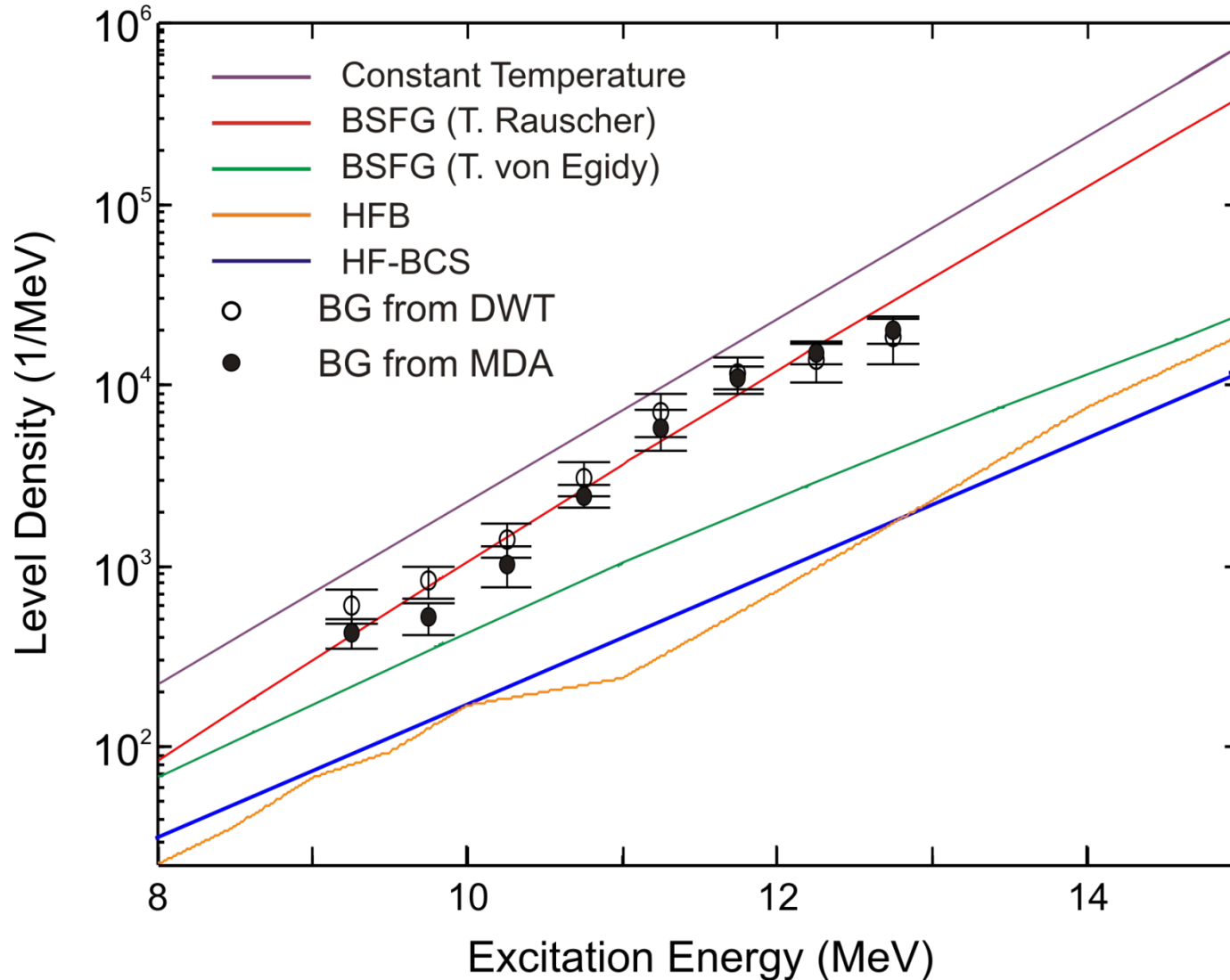


- Combined with model-independent measurement of  $r_{\text{skin}}$  by PREX  
 $\Rightarrow$  true constraint for isovector properties of any microscopic interaction

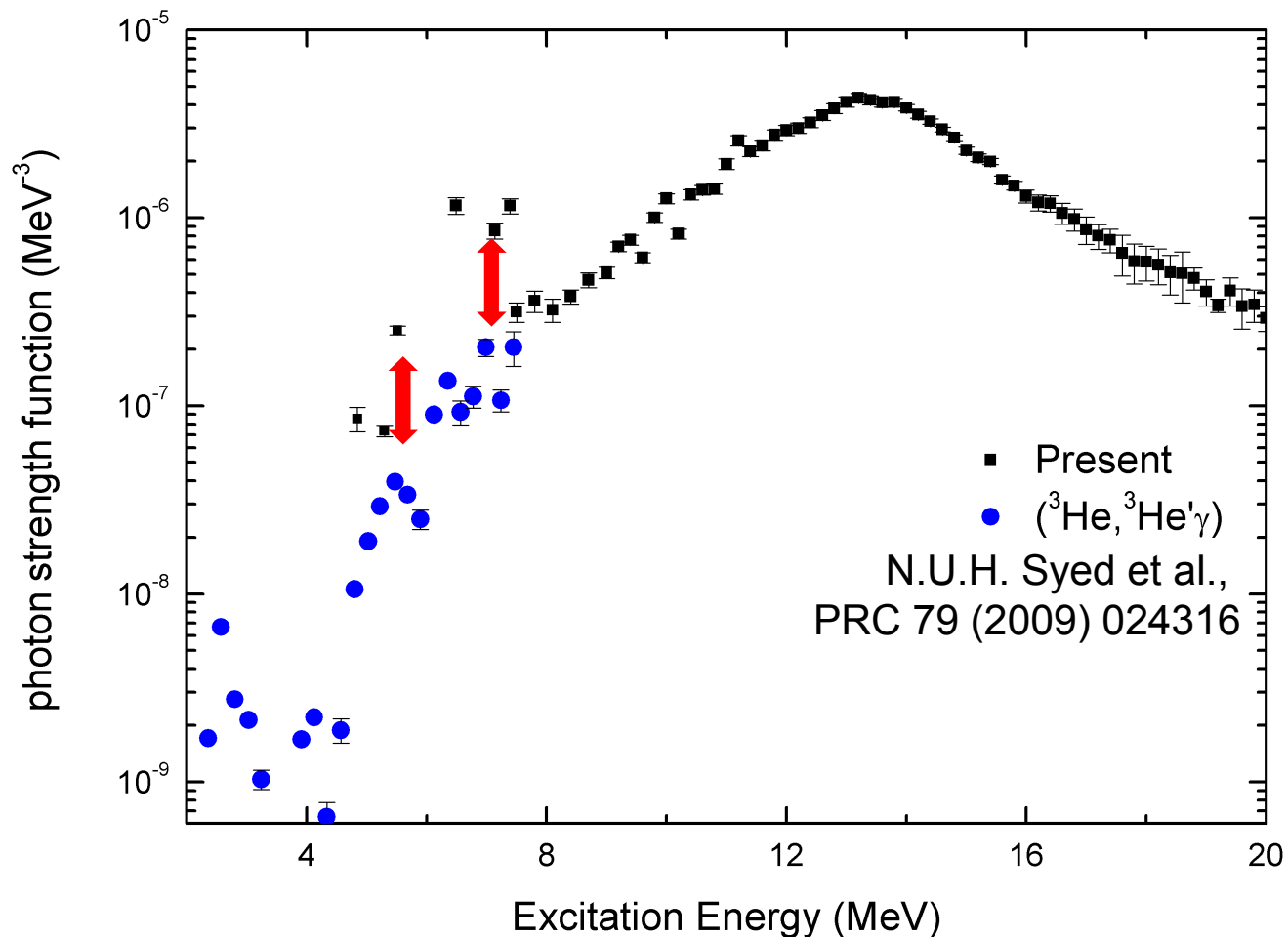
- Extracted from a fluctuation analysis of the fine structure of the GDR
  - S. Müller, F. Beck, D. Meuer, and A. Richter, PLB 113 (1982) 362
  - P.G. Hansen, B. Jonson, and A. Richter, NPA518 (1990) 13
  
- Depends on the background determined from
  - multipole decomposition analysis
  
  - discrete wavelet analysis of the spectrum
    - Y. Kalmykov et al., PRL 96 (2006) 012502



# $1^-$ states level densities in $^{208}\text{Pb}$



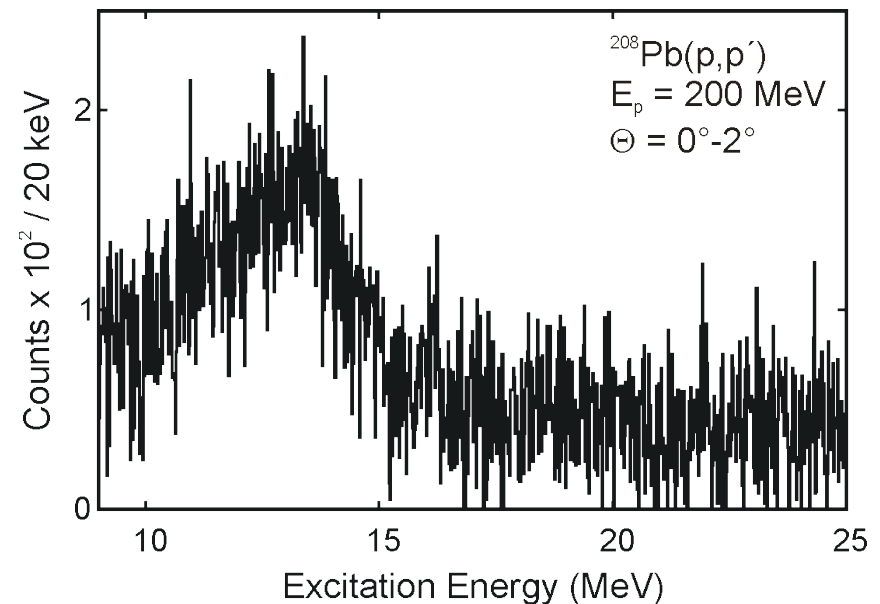
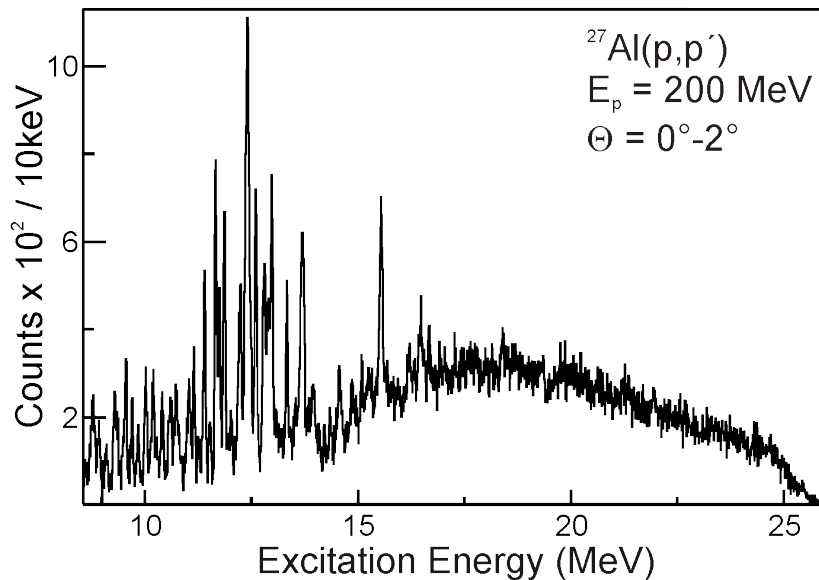
# Photon Strength Function in $^{208}\text{Pb}$



- Polarized intermediate energy proton scattering at  $0^\circ$ :  
a new tool to extract the complete dipole response in nuclei
  - Spinflip / non-spinflip cross section separation
  - B(E1) strength
  - Dipole polarizability
  - Level Densities of  $1^-$  states
  - Photon Strength Function
- Experiment on  $^{120}\text{Sn}$ : extraction of complete PDR strength
- Experiment on  $^{154}\text{Sm}$ : PDR in a heavy deformed nucleus

# First 0° Proton Scattering Experiments at iThemba LABS, South Africa

U Cape Town / TU Darmstadt / iThemba LABS / U Osaka / RCNP Osaka /  
U Witwatersrand collaboration



R. Neveling et al., NIMA (submitted)

# Collaboration

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A. Richter, J. Wambach

# Multipole Decomposition of Angular Distributions

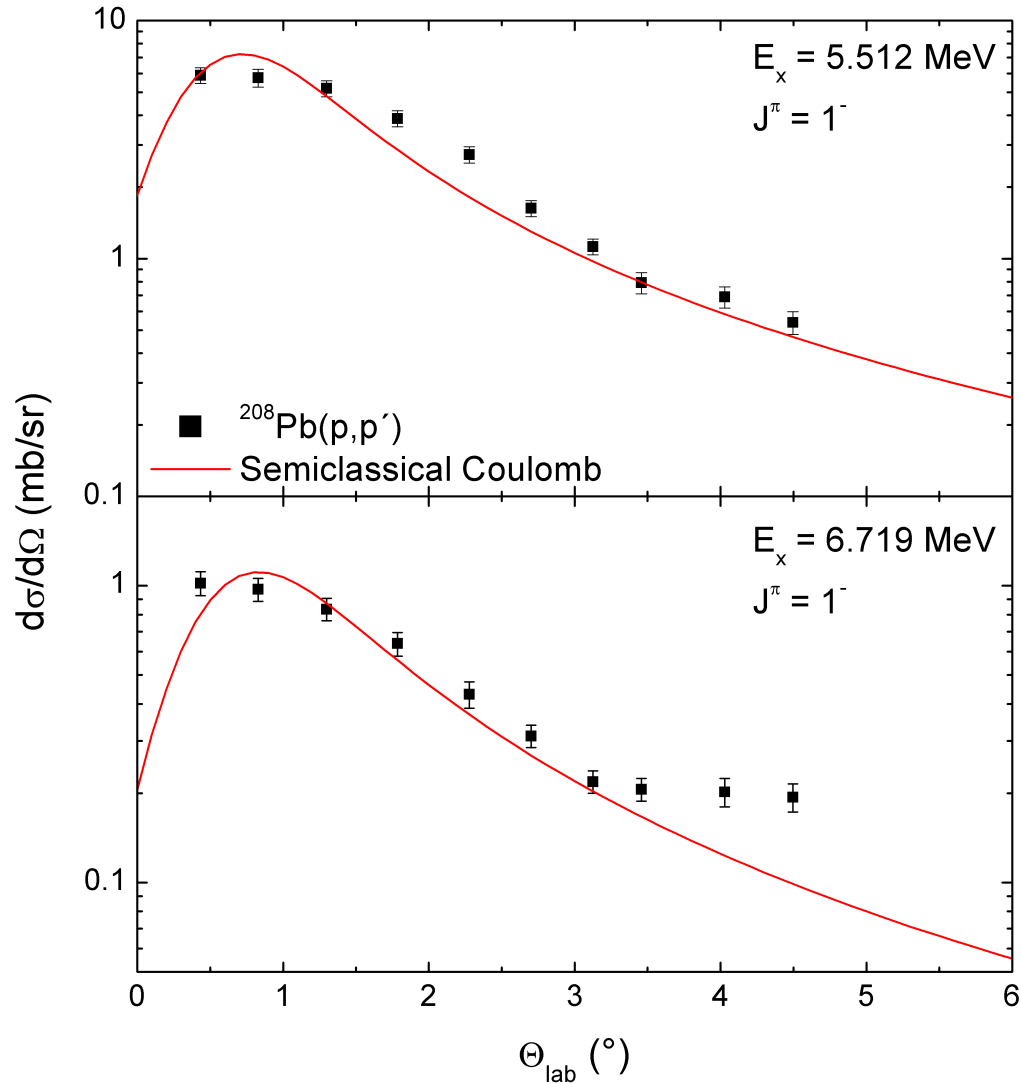
$$\left. \frac{d\sigma(\Theta_{lab}, E_x)}{d\Omega} \right|_{data} = \sum_{J^\pi} a_{J^\pi} \cdot \left. \frac{d\sigma(\Theta_{lab}, E_x, J^\pi)}{d\Omega} \right|_{DWBA}$$

DWBA07  
QPM wave functions  
Love&Franey effective interaction

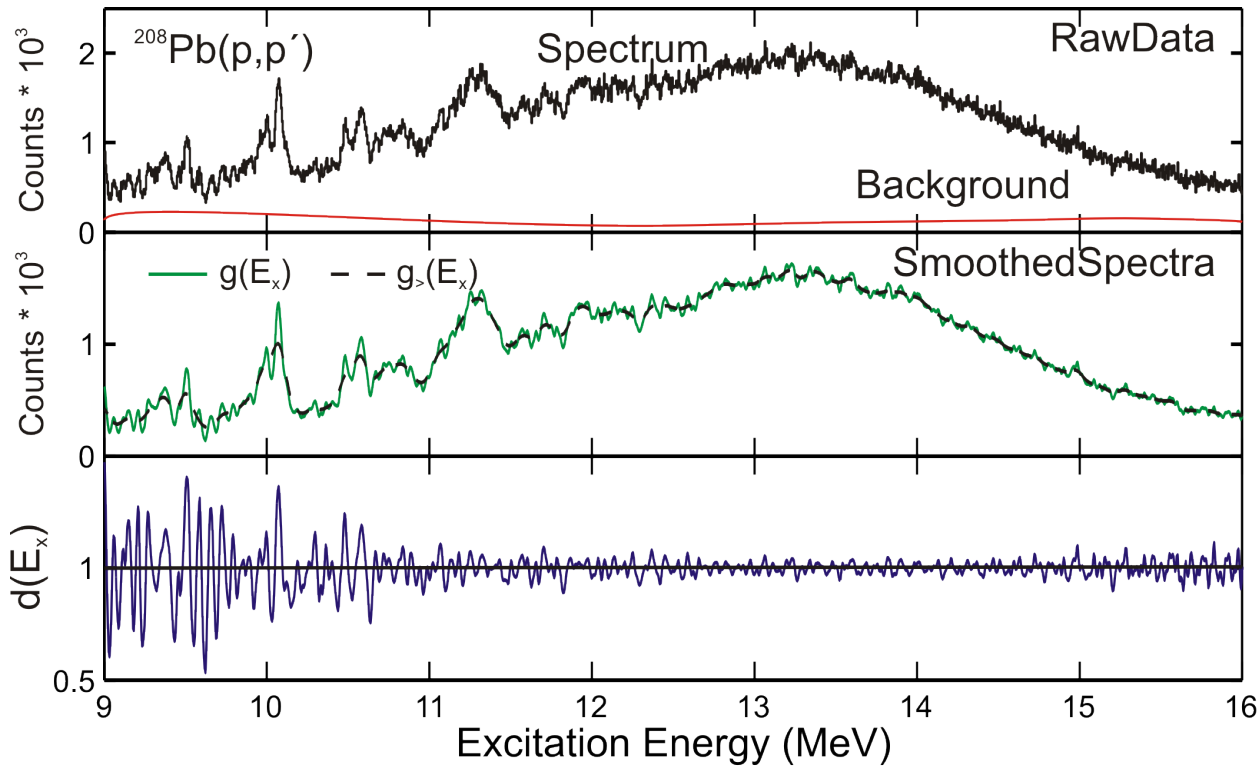
$$\left. \begin{array}{l} \text{DWBA07} \\ \text{QPM wave functions} \\ \text{Love\&Franey effective interaction} \end{array} \right\} \rightarrow \left. \frac{d\sigma(\Theta_{lab}, E_x, J^\pi)}{d\Omega} \right|_{DWBA}$$

- Restrict angular distribution to  $\Theta \leq 4^\circ$ 
  - too complex response at larger angles
- Low-energy region ( $E_x \leq 9$  MeV)
  - Isovector M1  $\rightarrow \Delta L = 0$
  - Coulomb dominated  $d\sigma/d\Omega$  for E1  $\rightarrow \Delta L = 1$
  - E2 (alternatively E3) substitute for  $\Delta L > 1$
- GDR region:
  - $\Delta L = 0$  replaced by Phenomenological background

# Coulomb Excitations of $1^-$ States

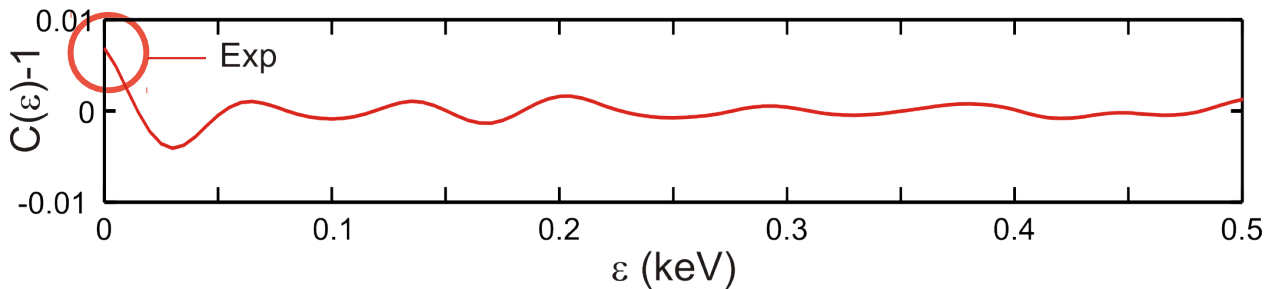


# Fluctuation Analysis



■ Background from MDA

■ Stationary spectrum  $\frac{g(E_x)}{g_{>}(E_x)}$



■ Autocorrelation function



# Autocorrelation Function and Mean Level Spacing

- $$C(\varepsilon) = \frac{\langle d(E_x) \cdot d(E_x + \varepsilon) \rangle}{\langle d(E_x) \rangle \cdot \langle d(E_x + \varepsilon) \rangle}$$

autocorrelation function

- $$C(\varepsilon = 0) - 1 = \frac{\langle d^2(E_x) \rangle - \langle d(E_x) \rangle^2}{\langle d(E_x) \rangle^2}$$

variance

- $$C(\varepsilon = 0) - 1 = \frac{\alpha \langle D \rangle}{2\sigma \sqrt{\pi}}$$

level spacing  $\langle D \rangle$

- $$\alpha = \alpha_{PT} + \alpha_W$$

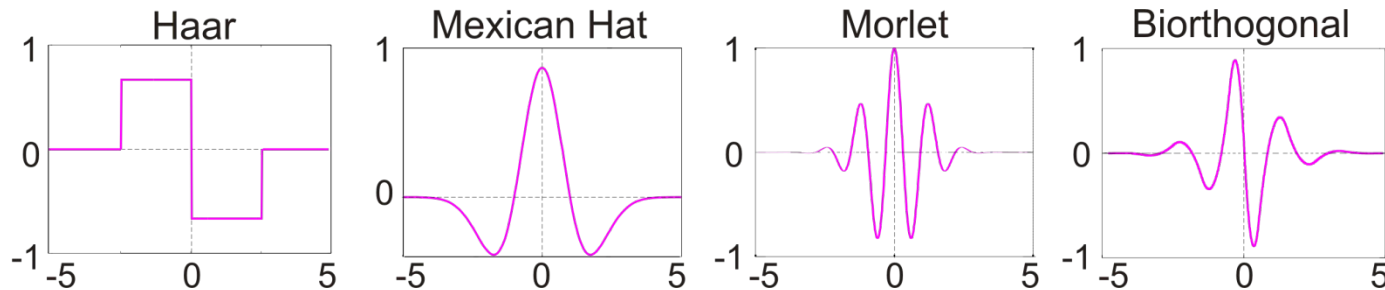
statistical properties

- $$\sigma$$

resolution

# Wavelets

- Wavelets:  $d \int_{-\infty}^{\infty} \Psi^*(x)x = 0$

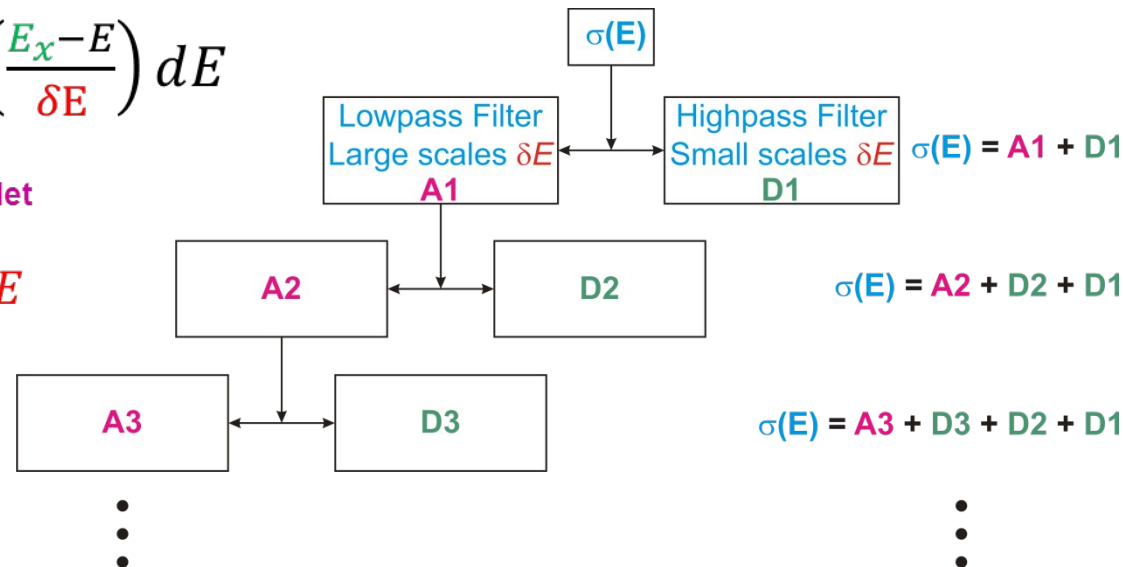


- Wavelet coefficients:

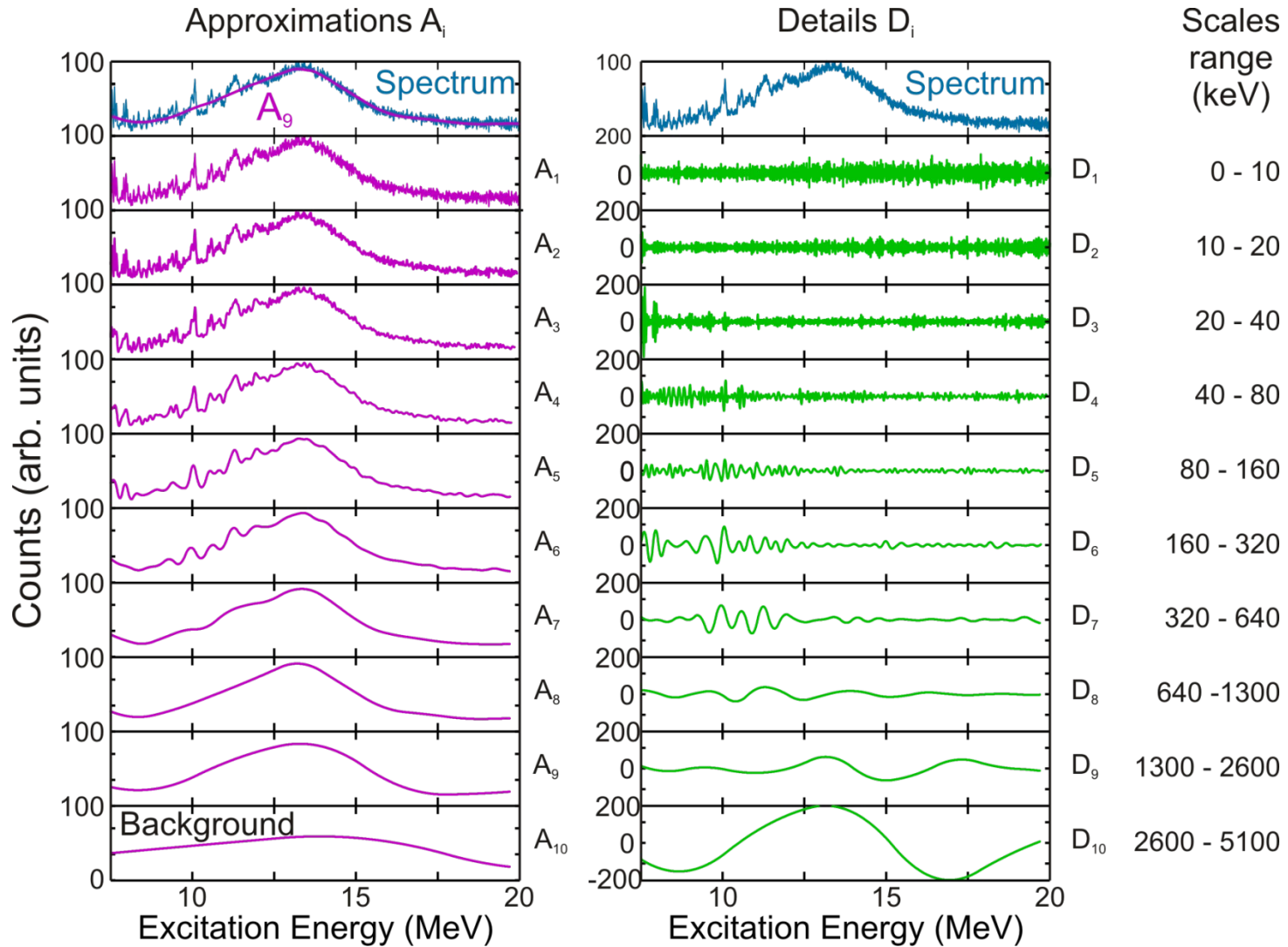
$$C(\delta E, E_x) = \frac{1}{\sqrt{\delta E}} \int \sigma(E) \Psi^* \left( \frac{E_x - E}{\delta E} \right) dE$$

↑ ↑ ↑ ↑  
scale position spectrum wavelet

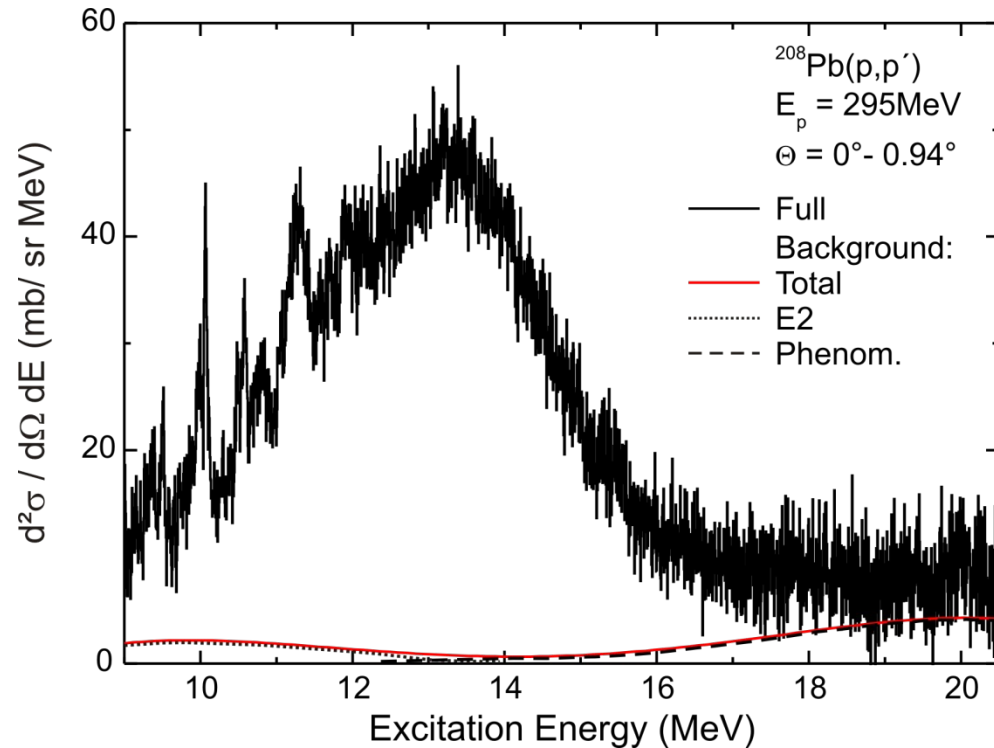
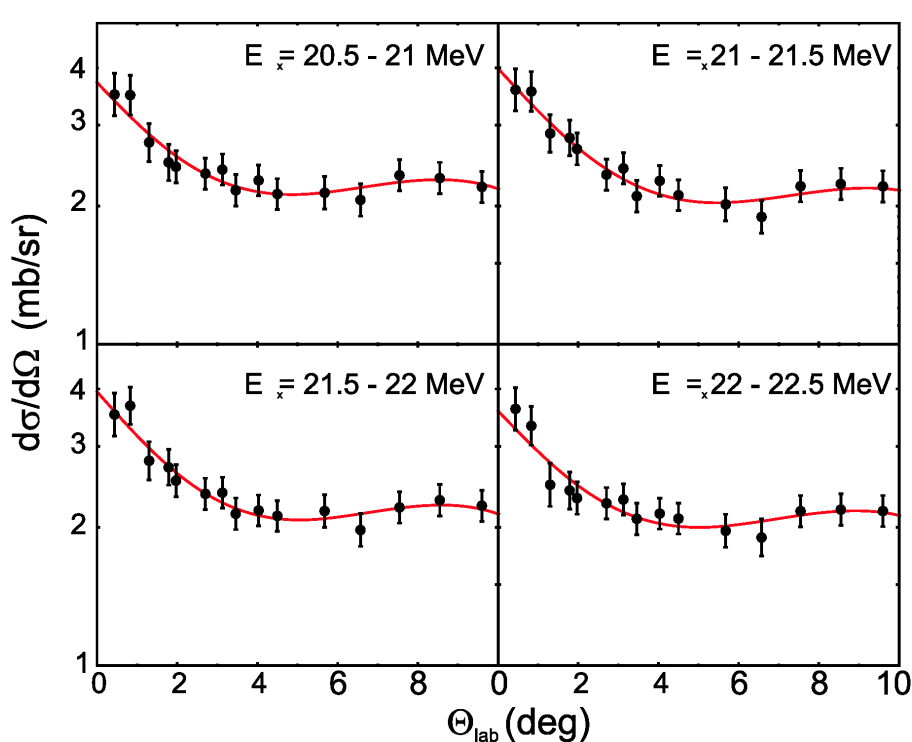
- Discrete:  $\delta E = 2^j$  and  $E_x = k\delta E$   
with  $k, j = 1, 2, 3, \dots$



# DWT of $^{208}\text{Pb}$ spectrum

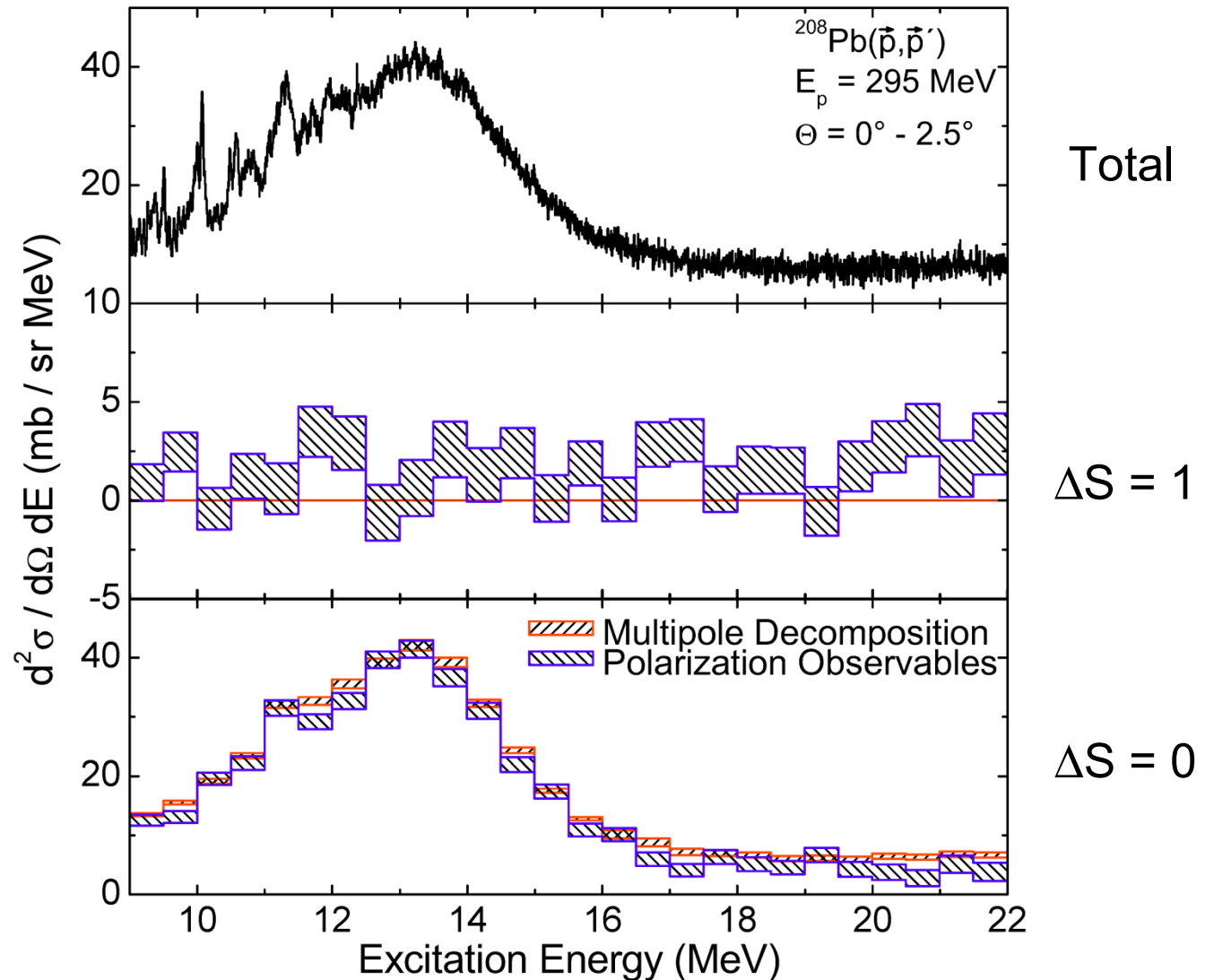


# Multipole Decomposition in the GDR Region



- identical angular distributions
- determines phenomenological background

# Comparison of Both Methods II



- Isovector part: analog of GT modes with  $T = T_0$
- Spinflip M1 resonance is quenched
  - in fp-shell nuclei similar to GT strength
  - in heavy nuclei – little data →  $^{208}\text{Pb}$  as a test case
- Problem studied in the 80's but:
  - large experimental uncertainties
  - improved model calculations
- new experimental access by  $(p,p')$ 
  - intermediate energy region optimal for spin-isospin excitations
  - at  $0^\circ$  → selectivity on  $\Delta L=0$  transitions
  - isovector spinflip M1 transitions enhanced