

# One- and two-phonon mixed-symmetry states in $^{94}\text{Mo}$ in high-resolution electron and proton scattering\*

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## Identification of Mixed-Symmetry States: Interacting **B**oson **M**odel - 2

- Pairing of nucleons to s-/ d-bosons

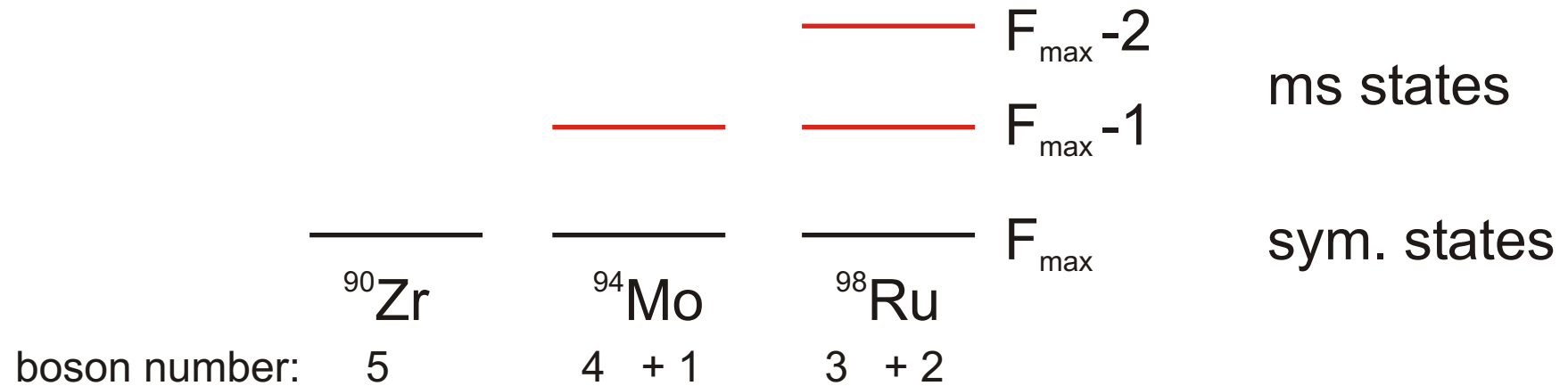
- F-Spin:      boson:  $F_0 = 1/2$        $\frac{|N - N|}{2}$        $F$        $F_{\max} = \frac{N + N}{2}$   
                  boson:  $F_0 = -1/2$

$F = F_{\max}$ : symmetric states

$F < F_{\max}$ : mixed-symmetry states (ms)

- Q-Phonon scheme:  $Q_s = Q + Q$        $| 2_1^+$        $Q_s | 0_1^+$   
 $Q_{ms} = \frac{N}{2} \left( \frac{Q}{N} - \frac{Q}{N} \right)$        $| 2_{ms}^+$        $Q_{ms} | 0_1^+$

## F-Spin Multiplet



## Why $^{94}\text{Mo}$ ?

- The low-energy spectrum of  $^{94}\text{Mo}$  is well studied and candidates for most one- and two-phonon states have been identified

N. Pietralla *et al.*, Phys. Rev. Lett. 83 (1999) 1303

N. Pietralla *et al.*, Phys. Rev. Lett. 84 (2000) 3775

C. Fransen *et al.*, Phys. Lett. B 508 (2001) 219

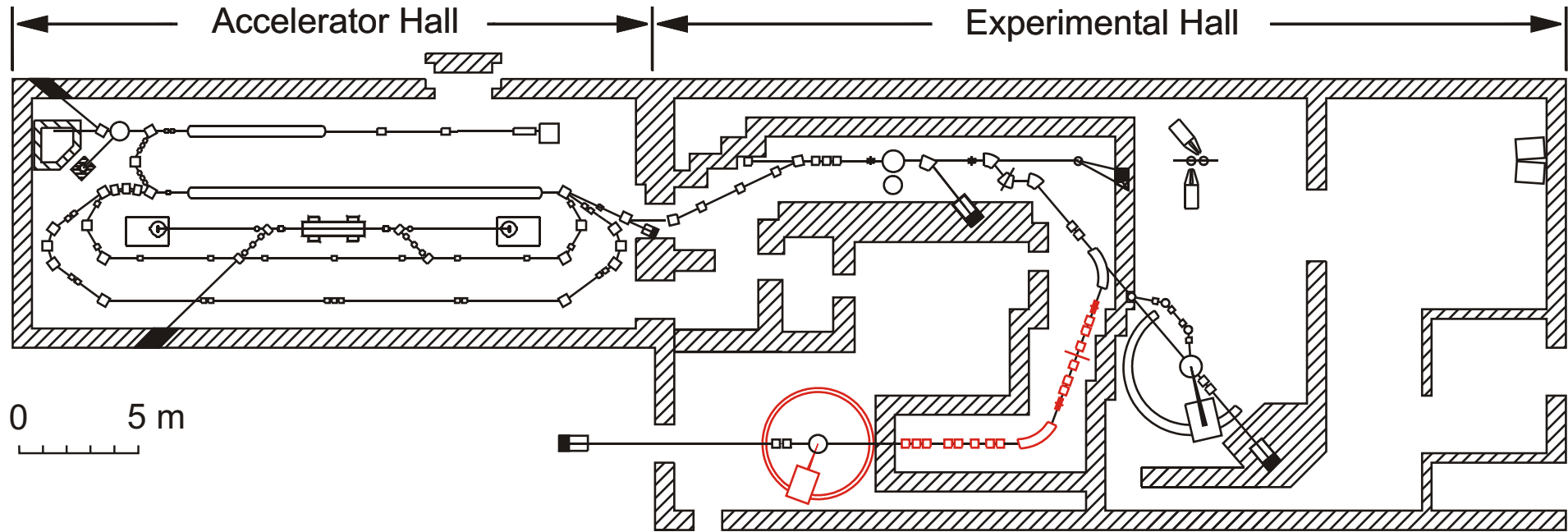
C. Fransen *et al.*, Phys. Rev. C 67 (2003) 024307

- Study of  $2^+$  states with  $(e,e')$  and  $(p,p')$ 
  - ⇒ sensitive to one-phonon components of the wave function
  - ⇒ test of fundamental phonon character
  - ⇒ isoscalar / isovector decomposition
  - ⇒ purity of two-phonon states

## Experiments

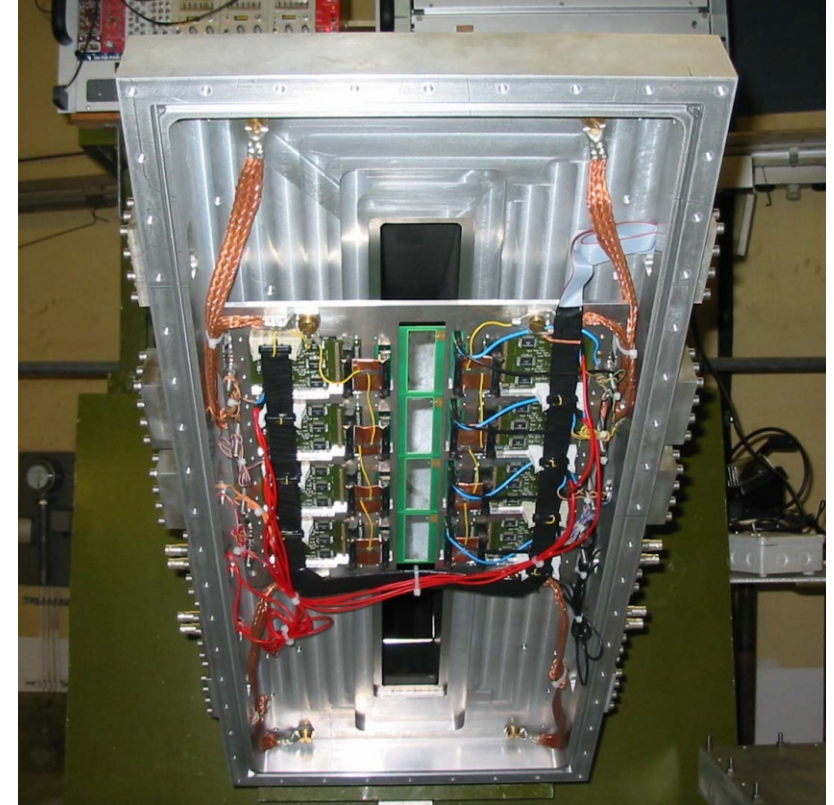
- High resolution required to resolve all  $2^+$  states below 4 MeV
- Lateral dispersion matching techniques
- $(e, e')$ :  
S-DALINAC, TU Darmstadt  
 $E_e = 70 \text{ MeV}$   
 $= 93^\circ - 165^\circ$   
 $E = 30 \text{ keV (FWHM)}$
- $(p, p')$ :  
SSC, iThemba LABS  
 $E_p = 200 \text{ MeV}$   
 $= 7^\circ - 26^\circ$   
 $E = 35 \text{ keV (FWHM)}$

## S-DALINAC



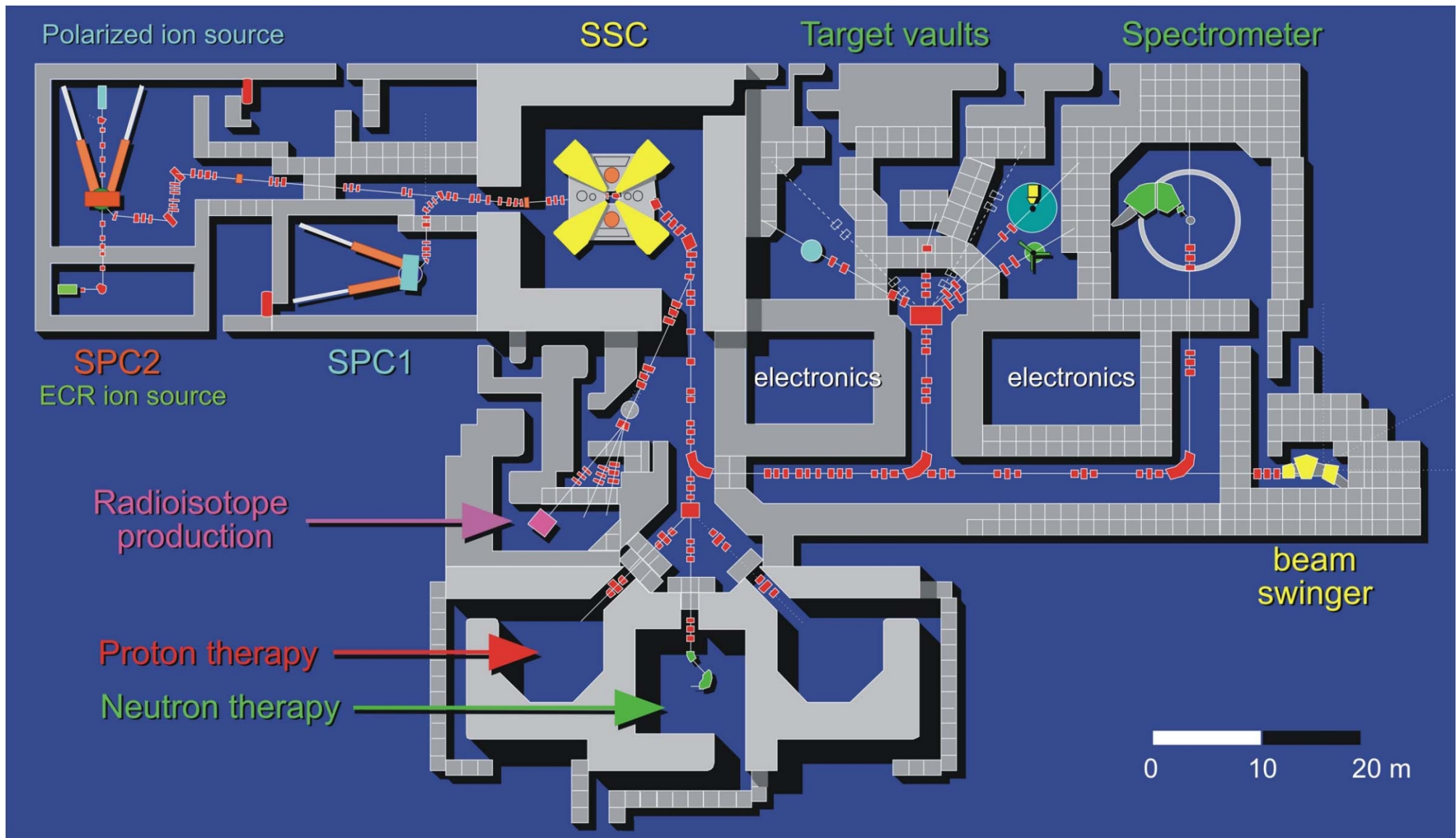
- High-resolution ( $e, e'$ ) experiments

# LINTOTT Spectrometer and Focal Plane Detector System



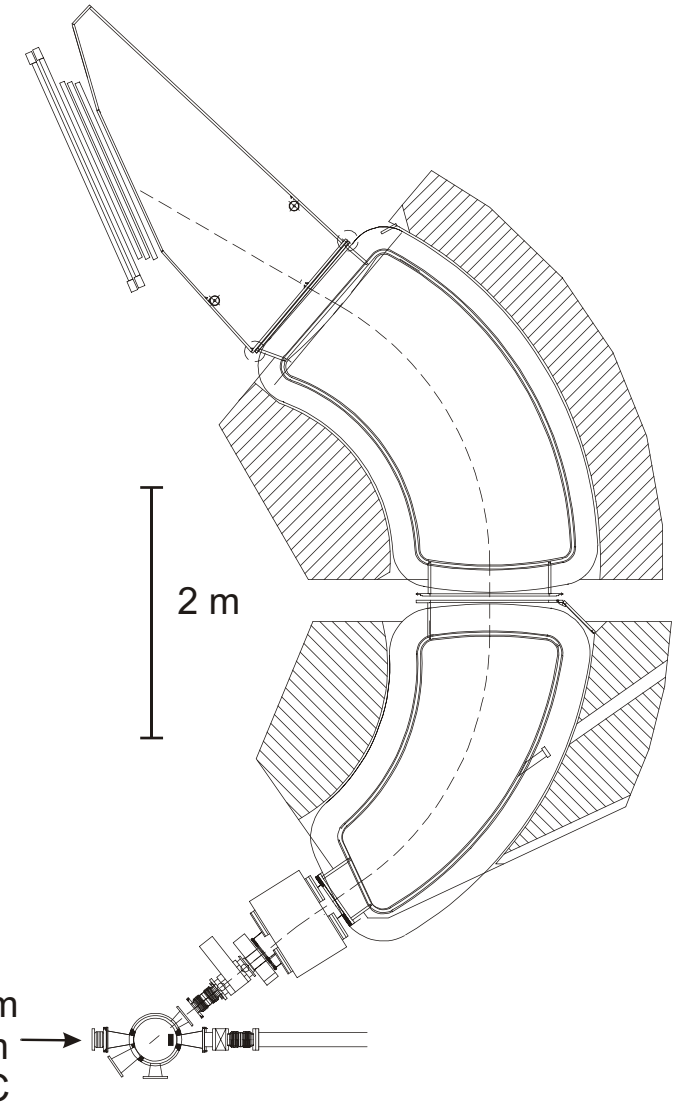
- New Si microstrip detector system: 4 modules, each contains 96 strips with active width of 500  $\mu\text{m}$
- Resolution:  $E/E = 4 \times 10^{-4}$
- Data rates up to 100 kHz

# Separated-Sector Cyclotron Facility

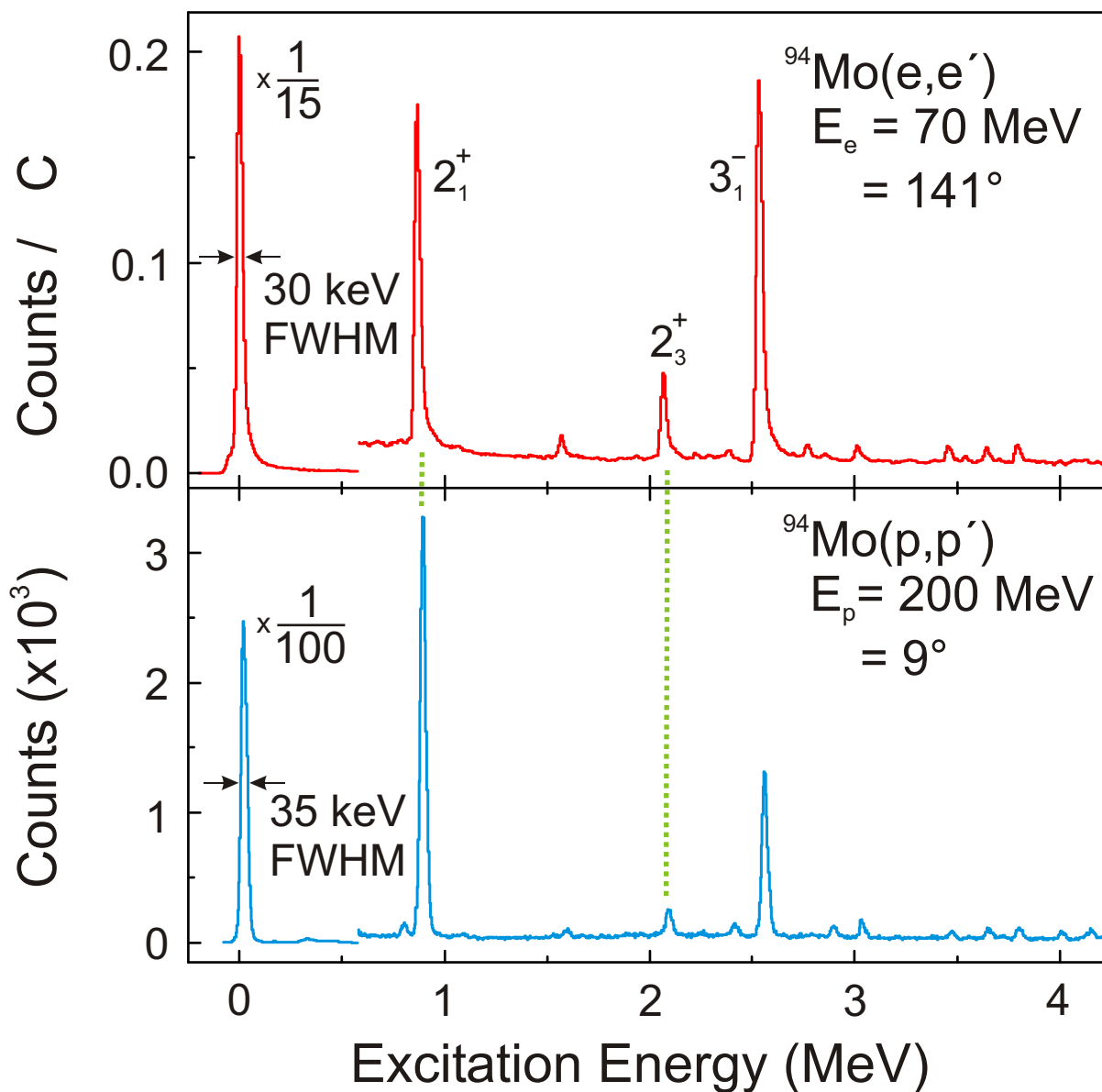




# K600 Magnetic Spectrometer and Detector System



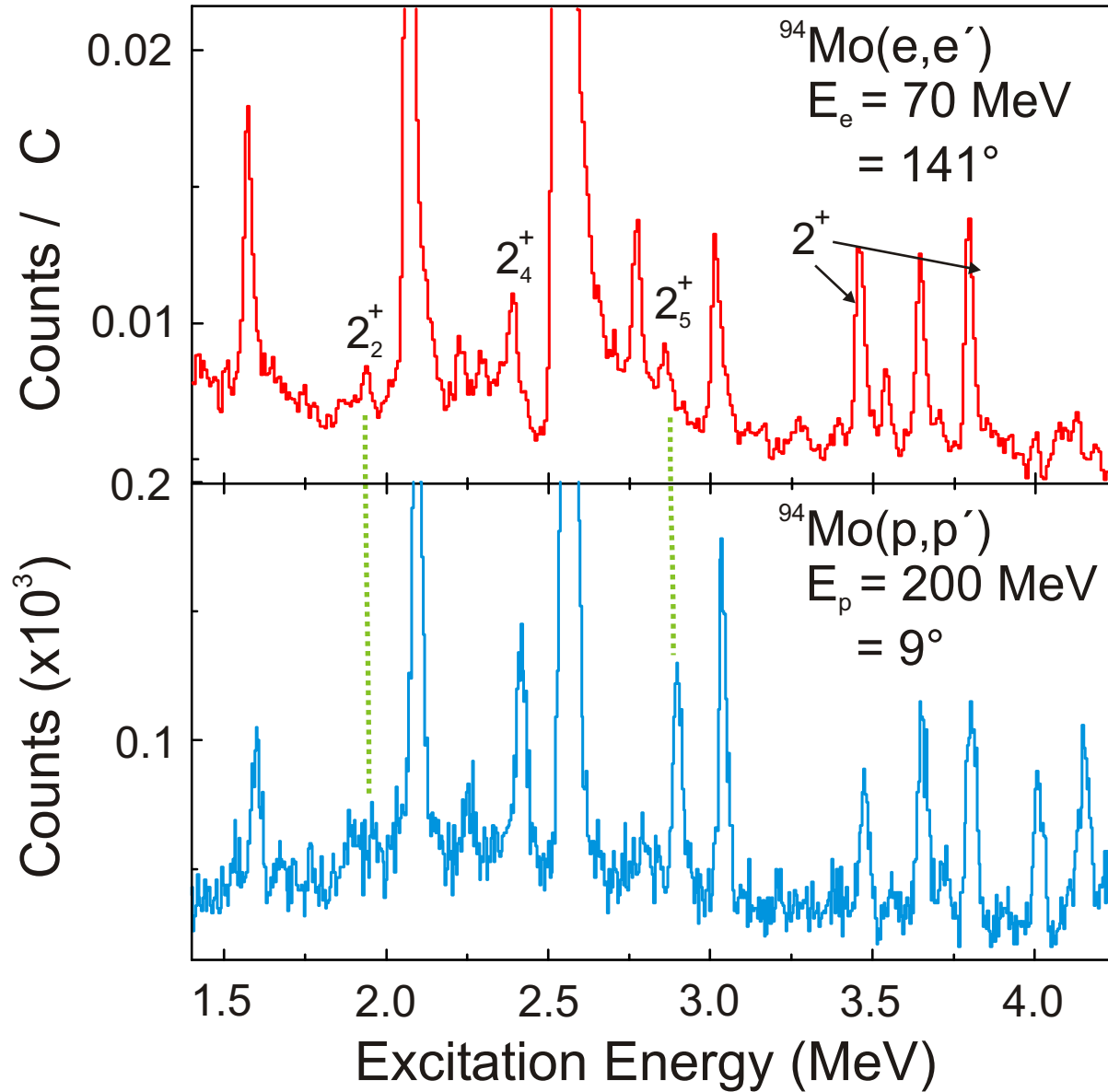
## Measured Spectra



S-DALINAC

iThemba LABS

## Measured Spectra



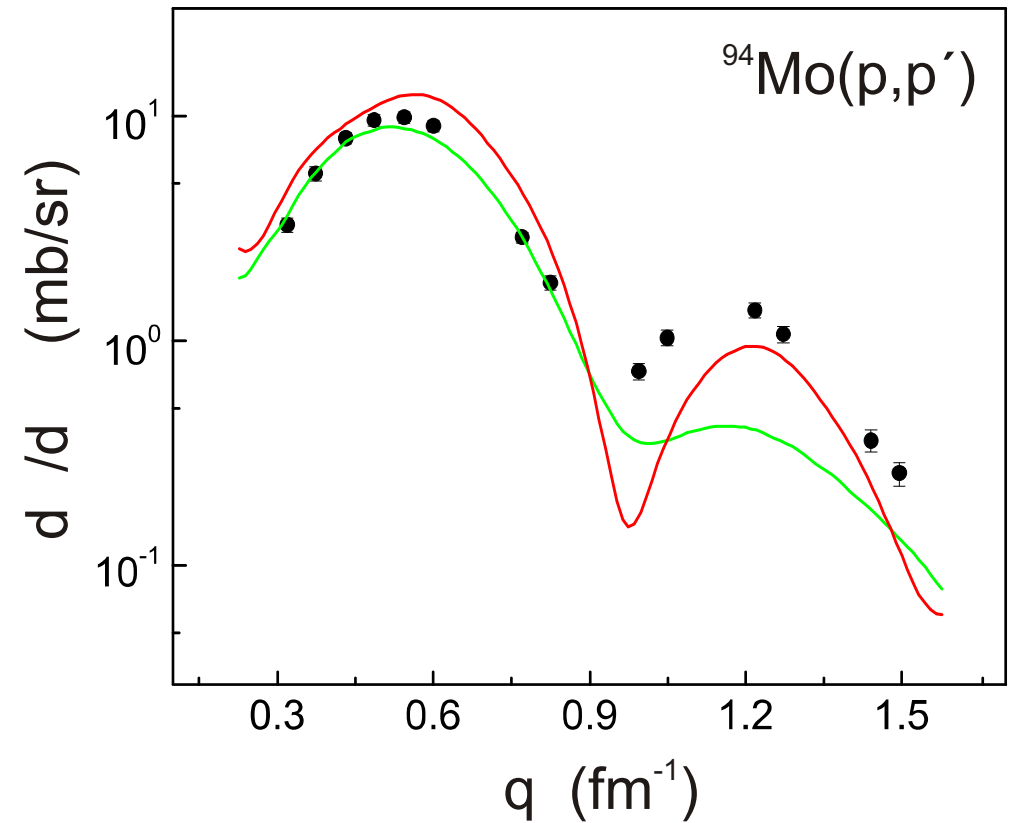
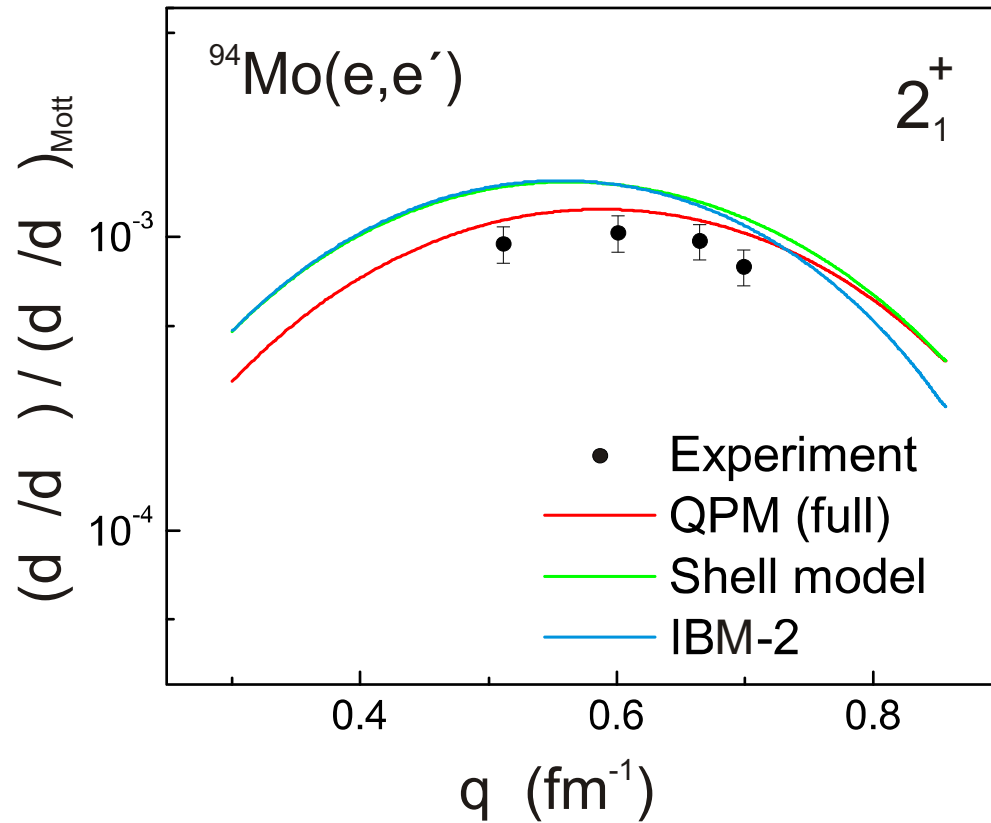
S-DALINAC

iThemba LABS

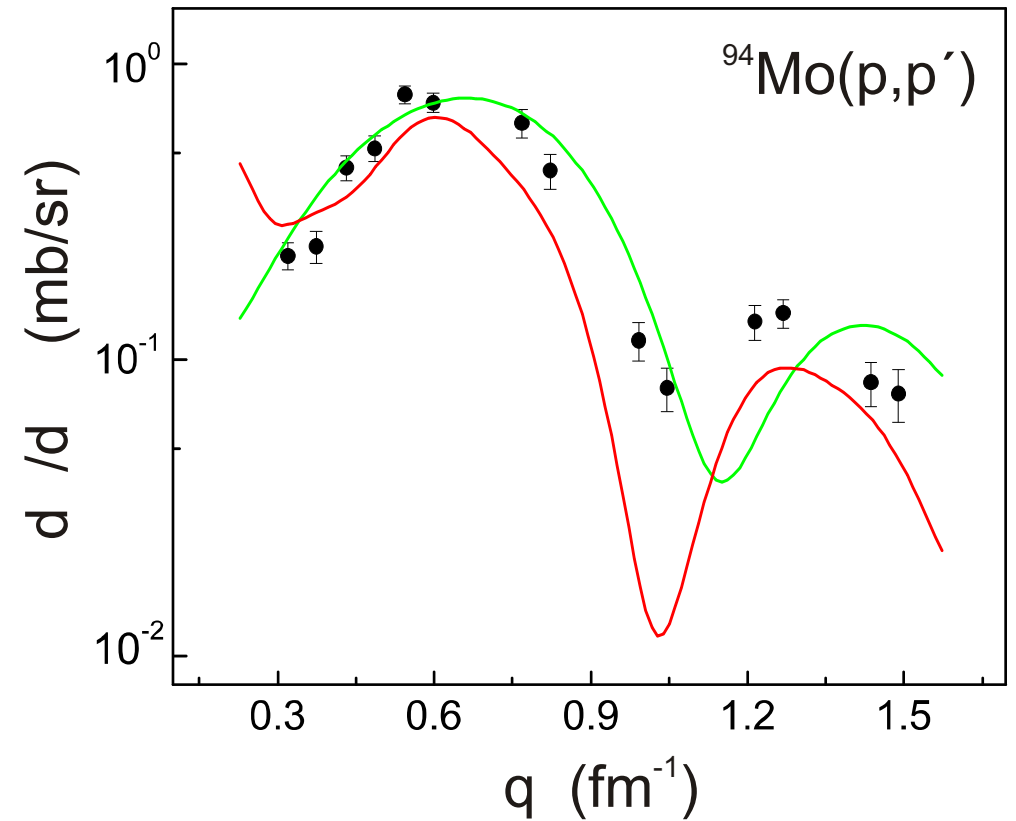
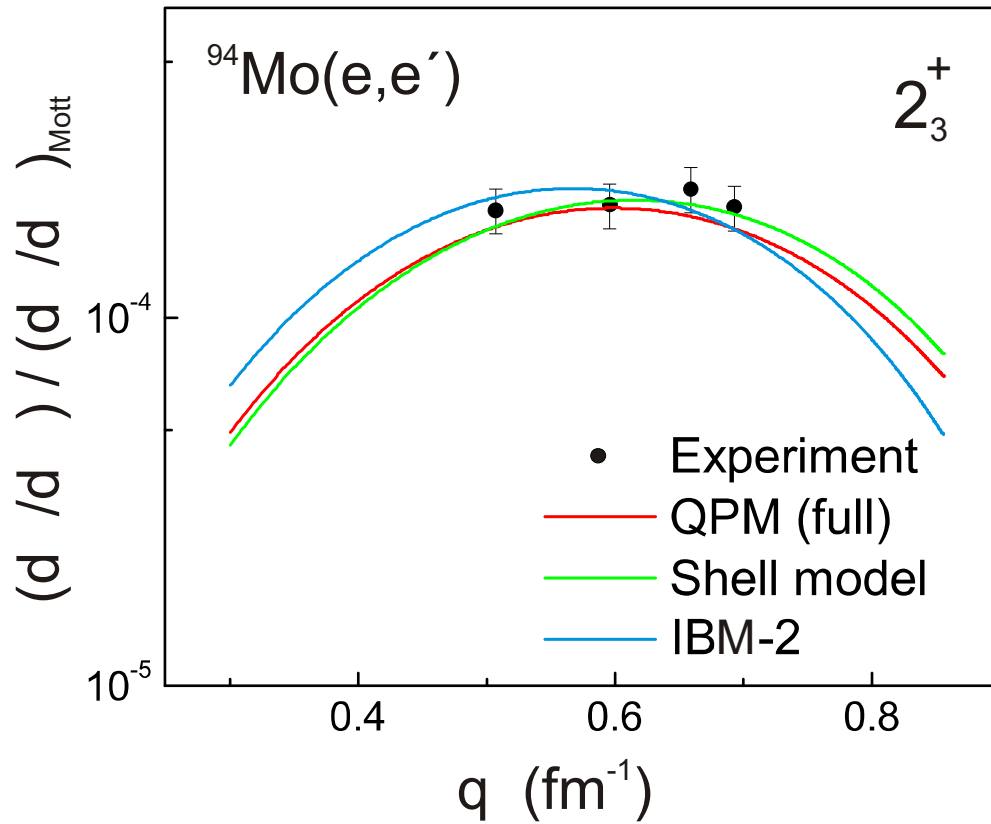
## Theoretical Calculation

- Quasi-Particle Phonon Model
  - ⇒ coupling up to 3 phonons
- Shell Model
  - ⇒  $^{88}\text{Sr}$  core / Surface Delta Interaction
- IBM-2
- Cross Sections
  - ⇒ DWBA / Love-Franey effective nucleon-target interaction for  $(p,p')$

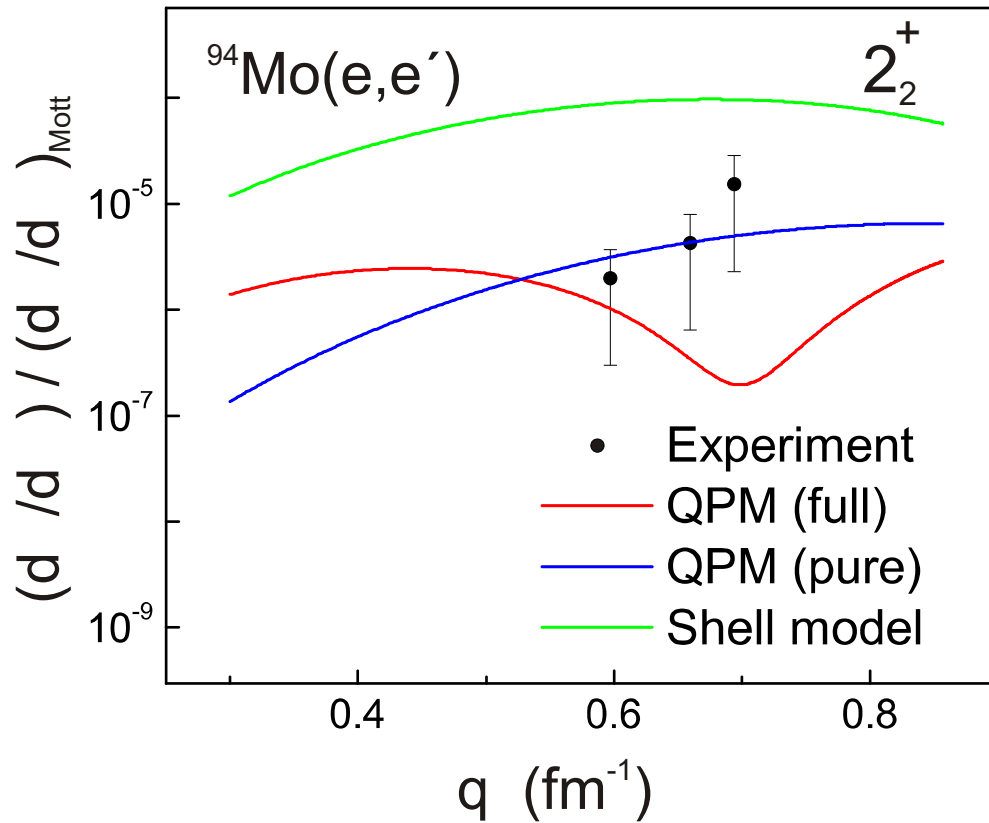
## One-Phonon Symmetric State



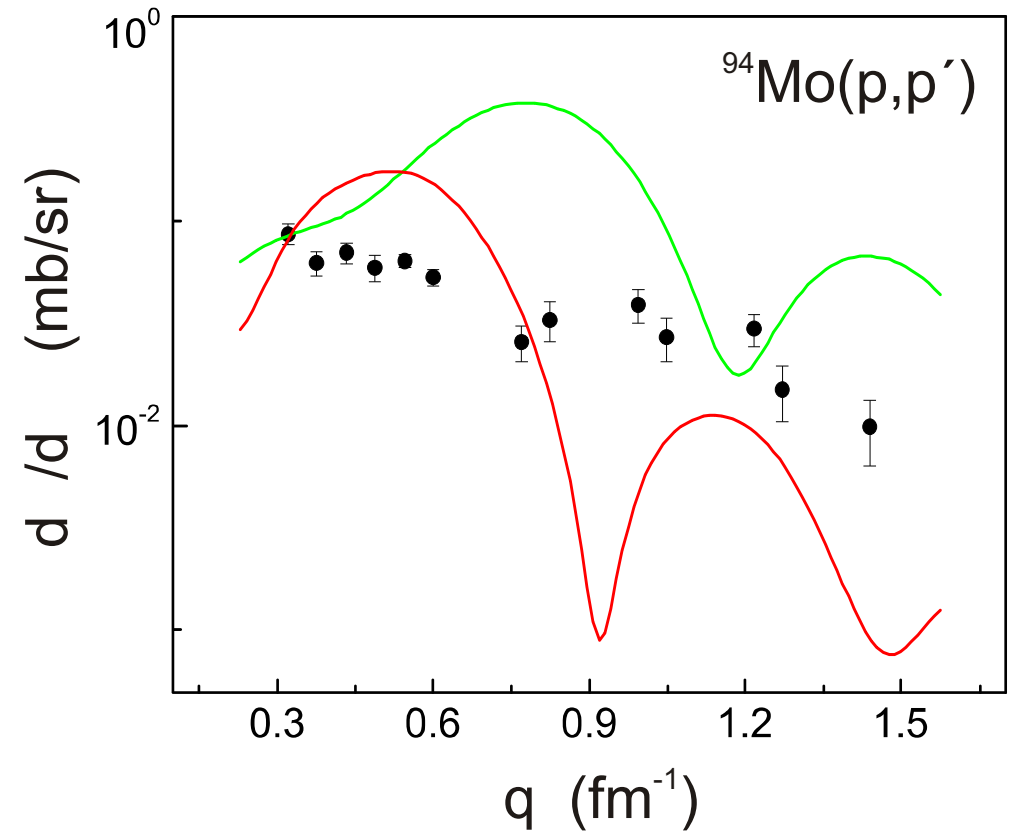
# One-Phonon MS State



## Two-Phonon Symmetric State

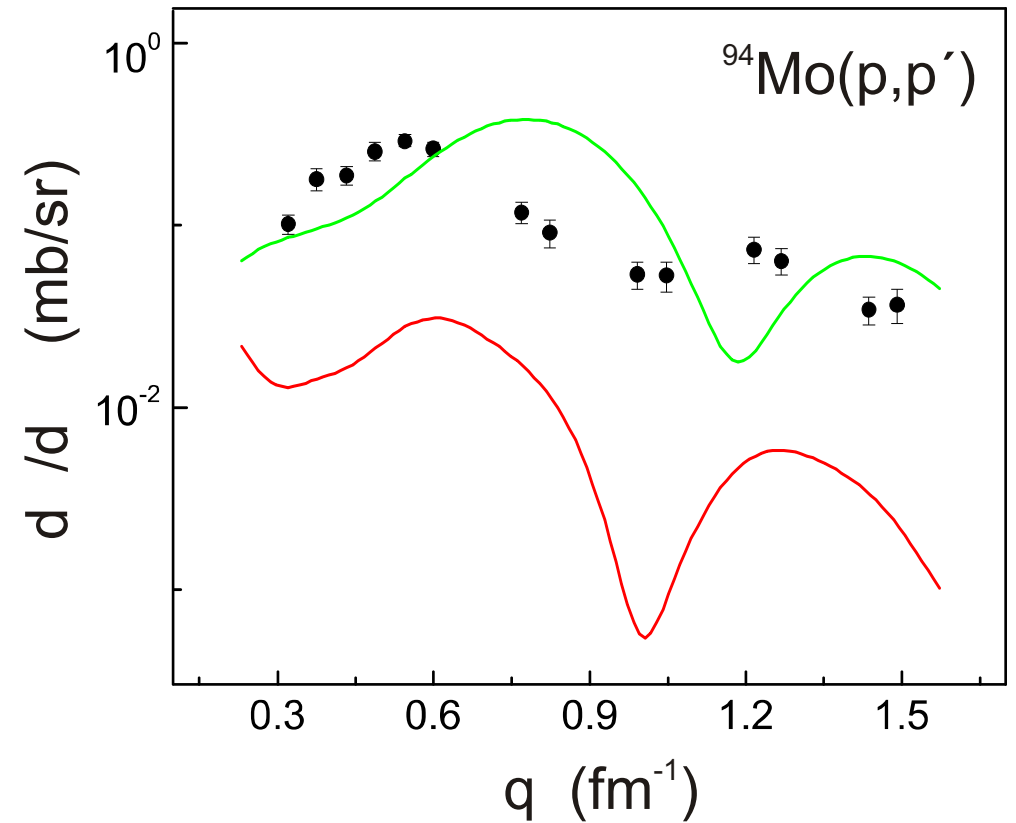
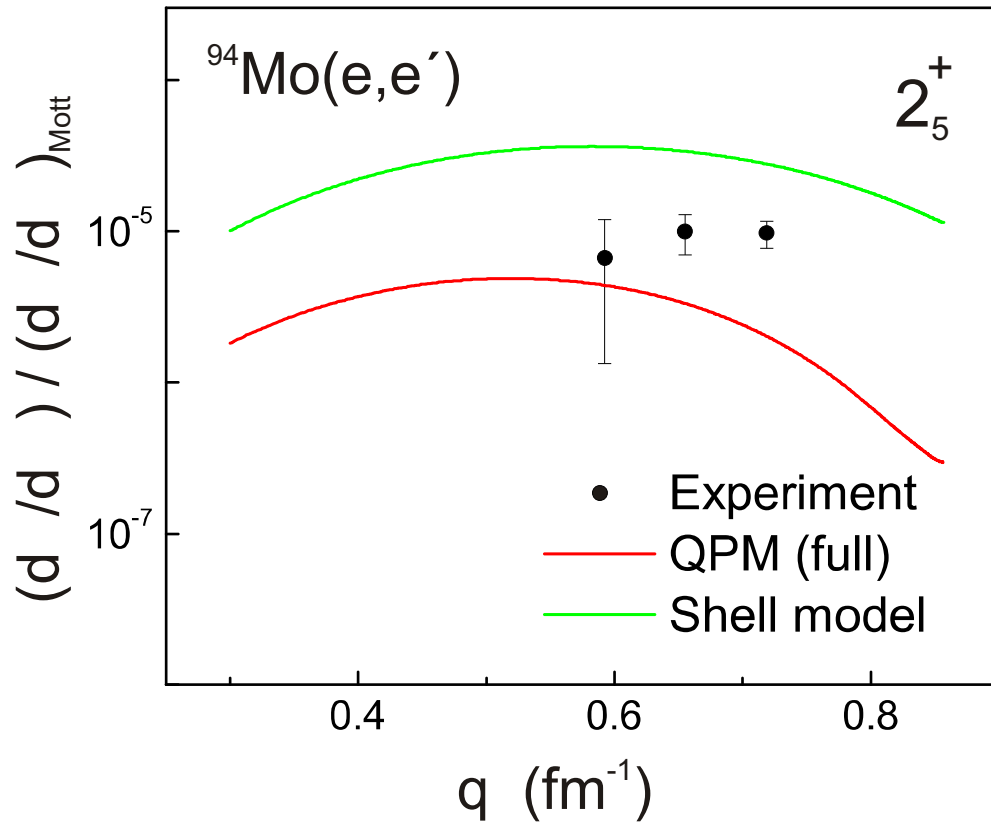


- pure two-phonon state



- two-step contributions?

## Two-Phonon MS State



- 7-10% one-phonon admixture

- two-step contributions?



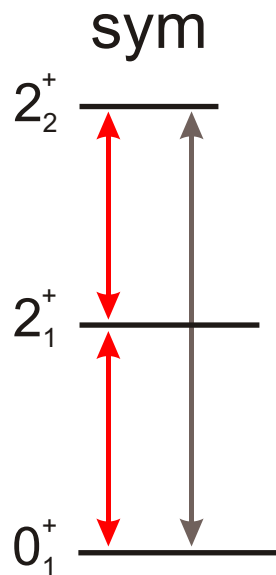
## Coupled-Channel Analysis

- Collective model

$$\Rightarrow U_{fi}(r) = - \frac{{}_L R_0}{2L+1} \frac{d}{dr} U(r), \quad L \quad 2$$

$$\Rightarrow \frac{{}_L 2}{L} = \left( \frac{d}{d} \right)_L^{\text{exp}} / \left( \frac{d}{d} \right)_L^{\text{DWBA}}$$

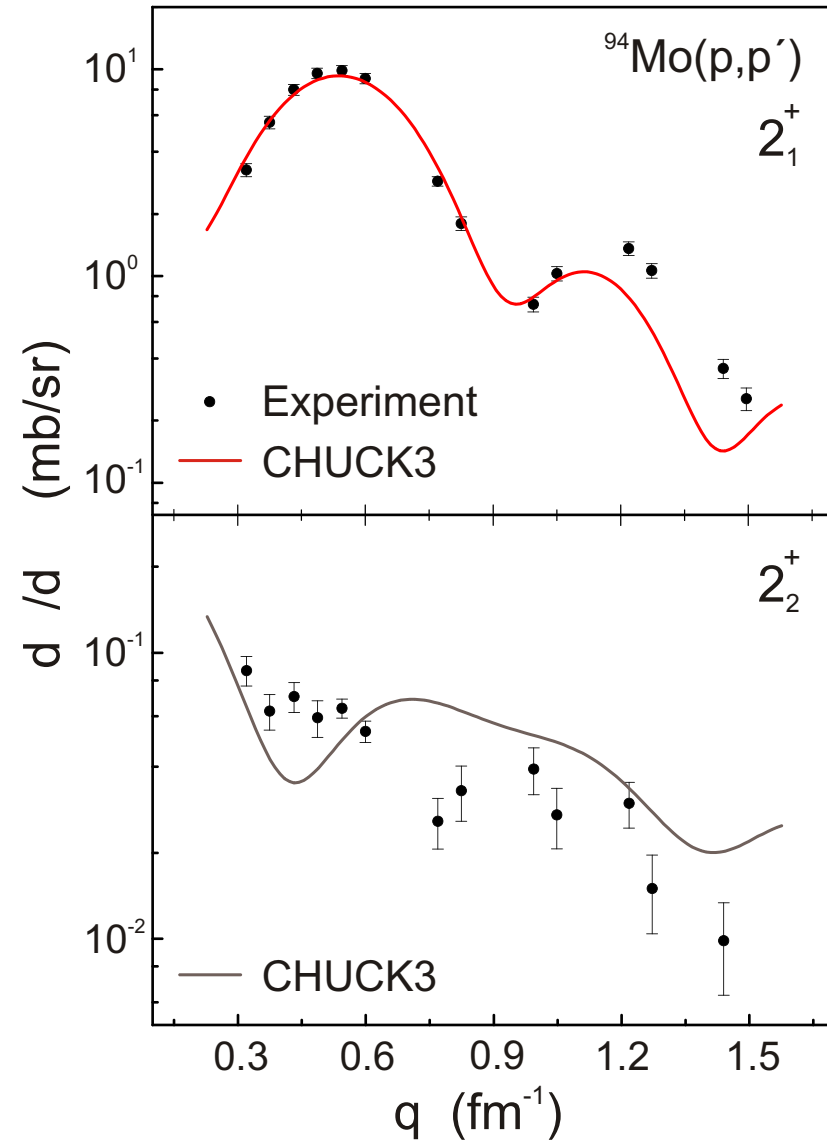
# Coupled-Channel Analysis: One and Two-Phonon Symmetric States



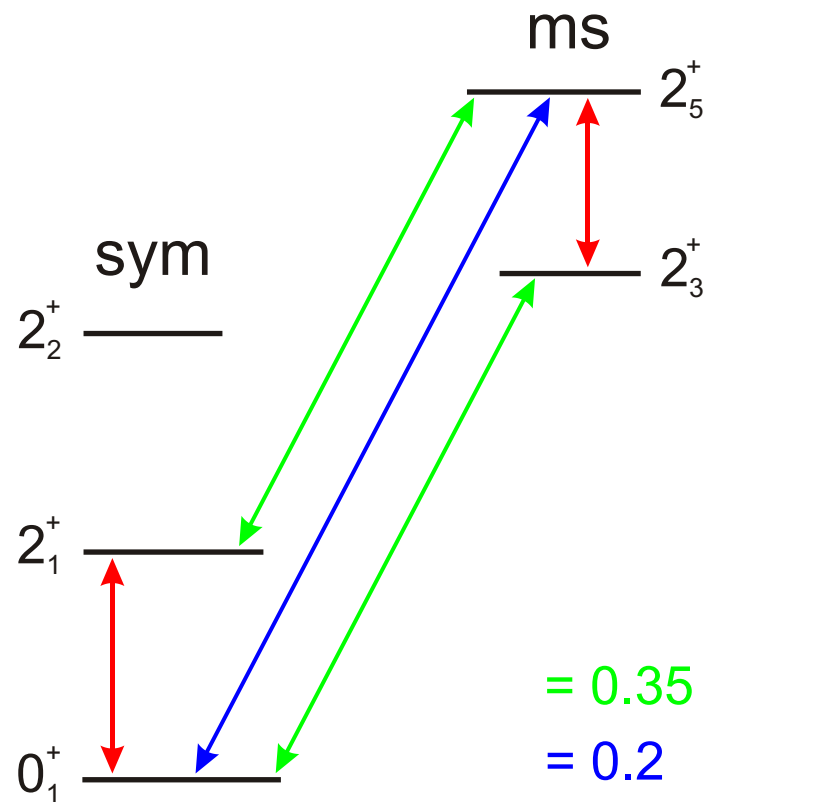
$$= 1.23$$

$$= 0.0$$

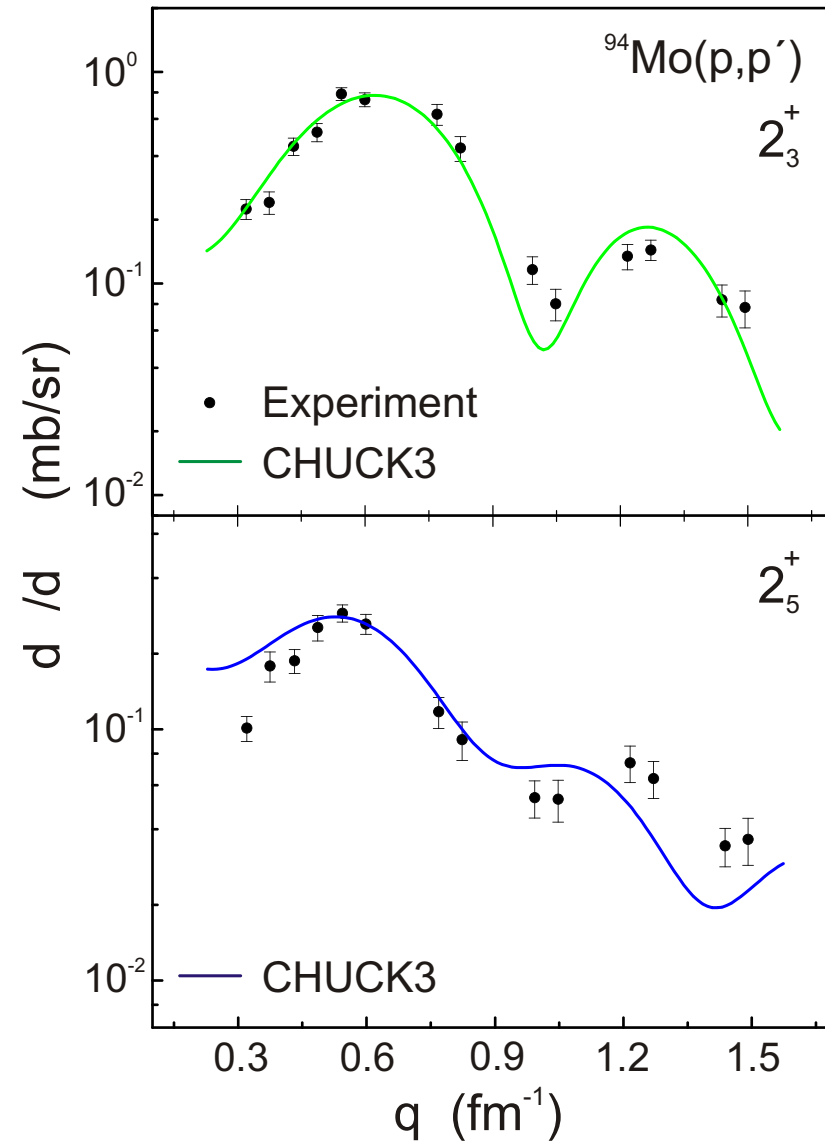
- pure two-phonon symmetric state confirmed



# Coupled-Channel Analysis: One and Two-Phonon MS States



- one-phonon admixtures to two-phonon ms state confirmed



## Summary

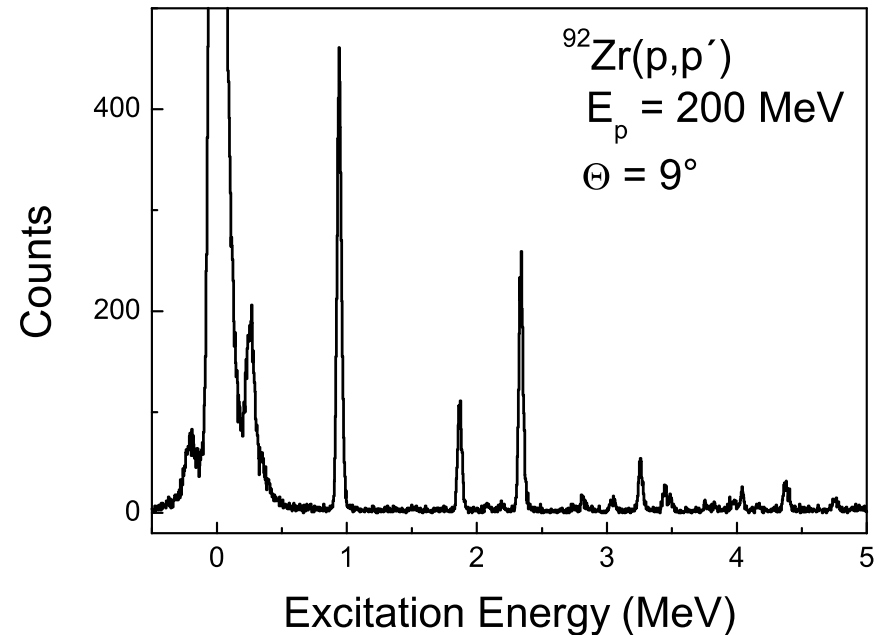
- Study of one- and two-phonon  $2^+$  states in  $^{94}\text{Mo}$  with high-resolution  $(e,e')$  and  $(p,p')$  experiments
- Combined analysis with microscopic models reveals:
  - symmetric and ms character of one-phonon states
  - two-phonon symmetric state extremely pure
  - about 25% admixtures in the two-phonon ms wave function (mostly 3-phonon)
  - quantitatively consistent results after inclusion of two-step processes in  $(p,p')$

## Outlook

- The case of  $^{92}\text{Zr}$ : Mixed-symmetry concept seems to fail  
C.Fransen *et al.*, Phys. Rev. C 71 (2005) 054304

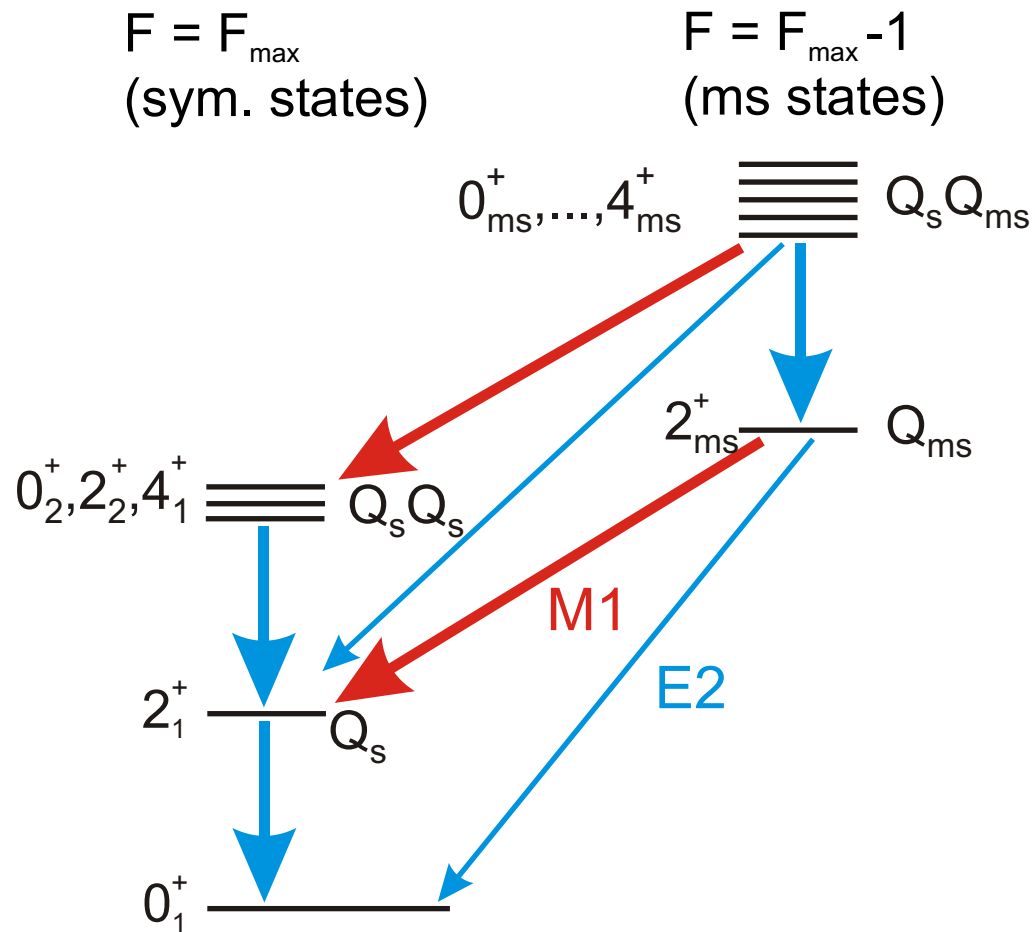
⇒ Experiments:

- (p,p') at iThemba LABS
- (e,e') at S-DALINAC





## Identification of Mixed-Symmetry States: Q-Phonon Scheme



- Strong **E2** transitions for decay of sym. Q-phonon
- Weak **E2** transitions for decay of ms Q-phonon
- Strong **M1** transitions for decay of ms states to sym. states