

Fine Structure of Giant Resonances Revisited Experimentally and Theoretically

- Nature of the pygmy dipole resonance: the case of ^{208}Pb
- M2 and spin dipole modes
- Fine structure and characteristic scales
 - ISGQR at shell closures
 - GT resonance in ^{90}Nb

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A. Richter, N. Ryezayeva, A. Shevchenko, J. Wambach

Darmstadt / Groningen / iThembaLAB / Münster / Osaka Collaborations

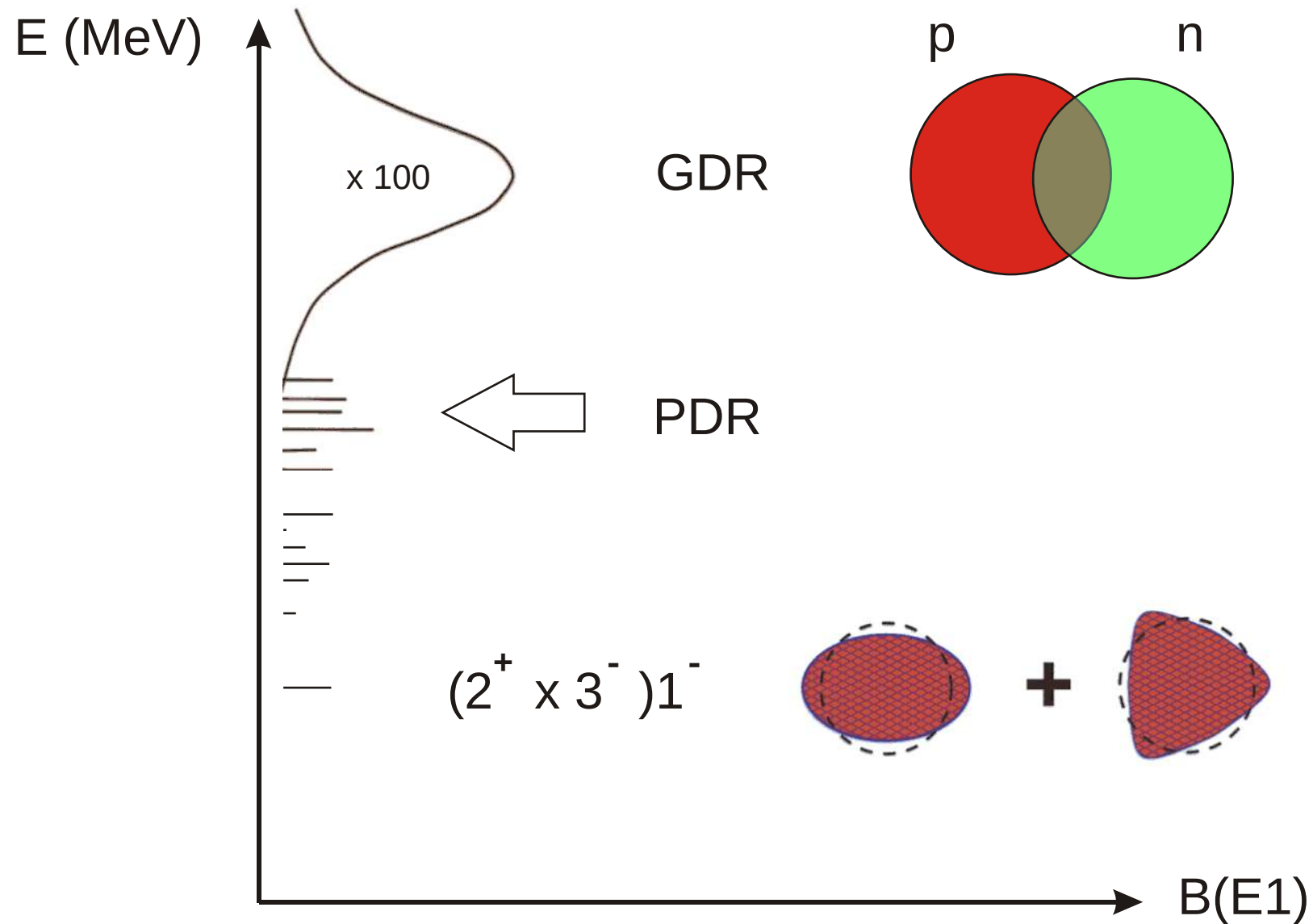
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Nature of the pygmy dipole resonance: the case of ^{208}Pb

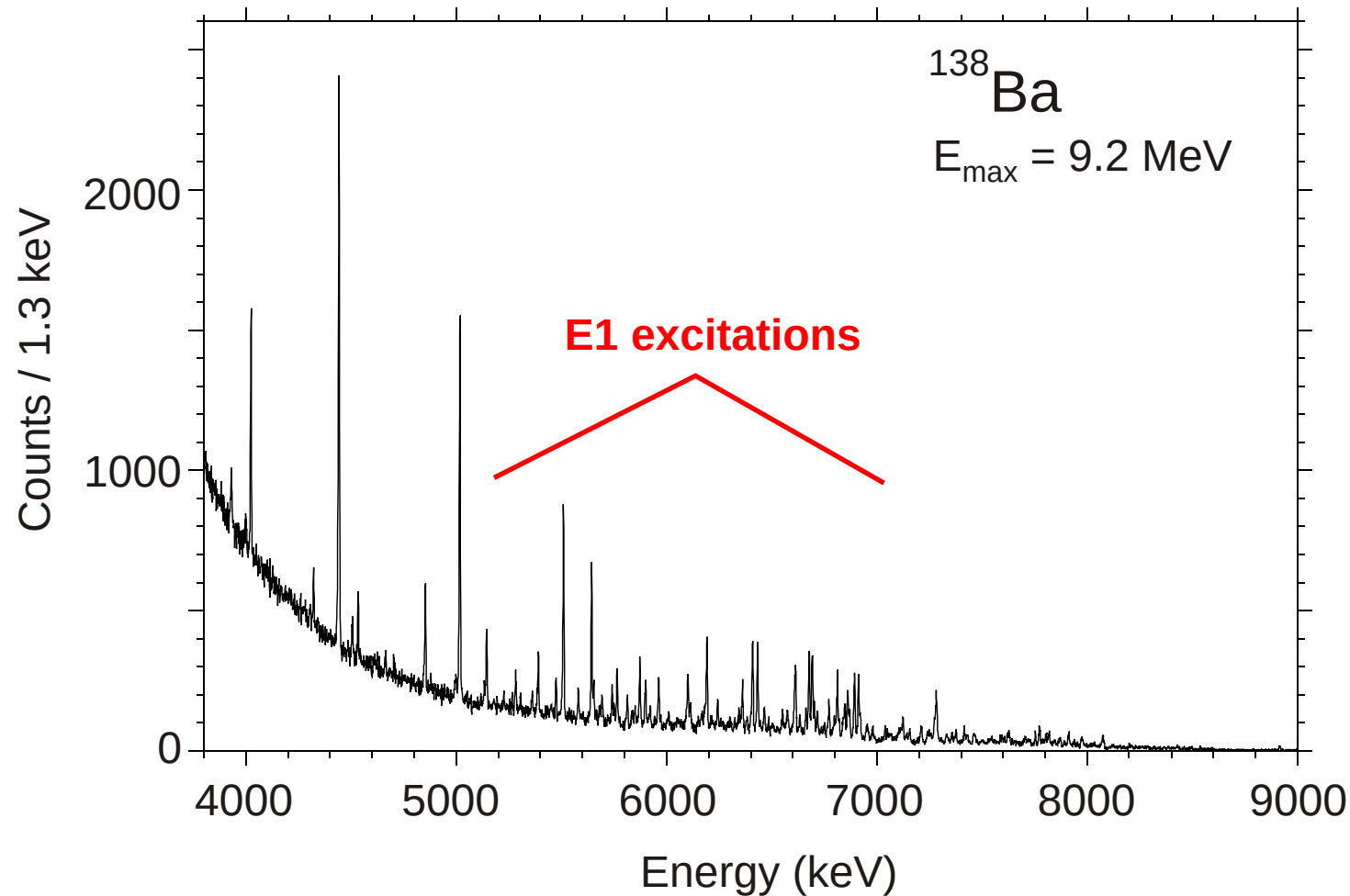


E1 Response in Nuclei





Photon Scattering off ^{138}Ba



- A. Zilges et al., Phys. Lett. B 542, 43 (2002)



Pygmy dipole resonances in the relativistic random phase approximation

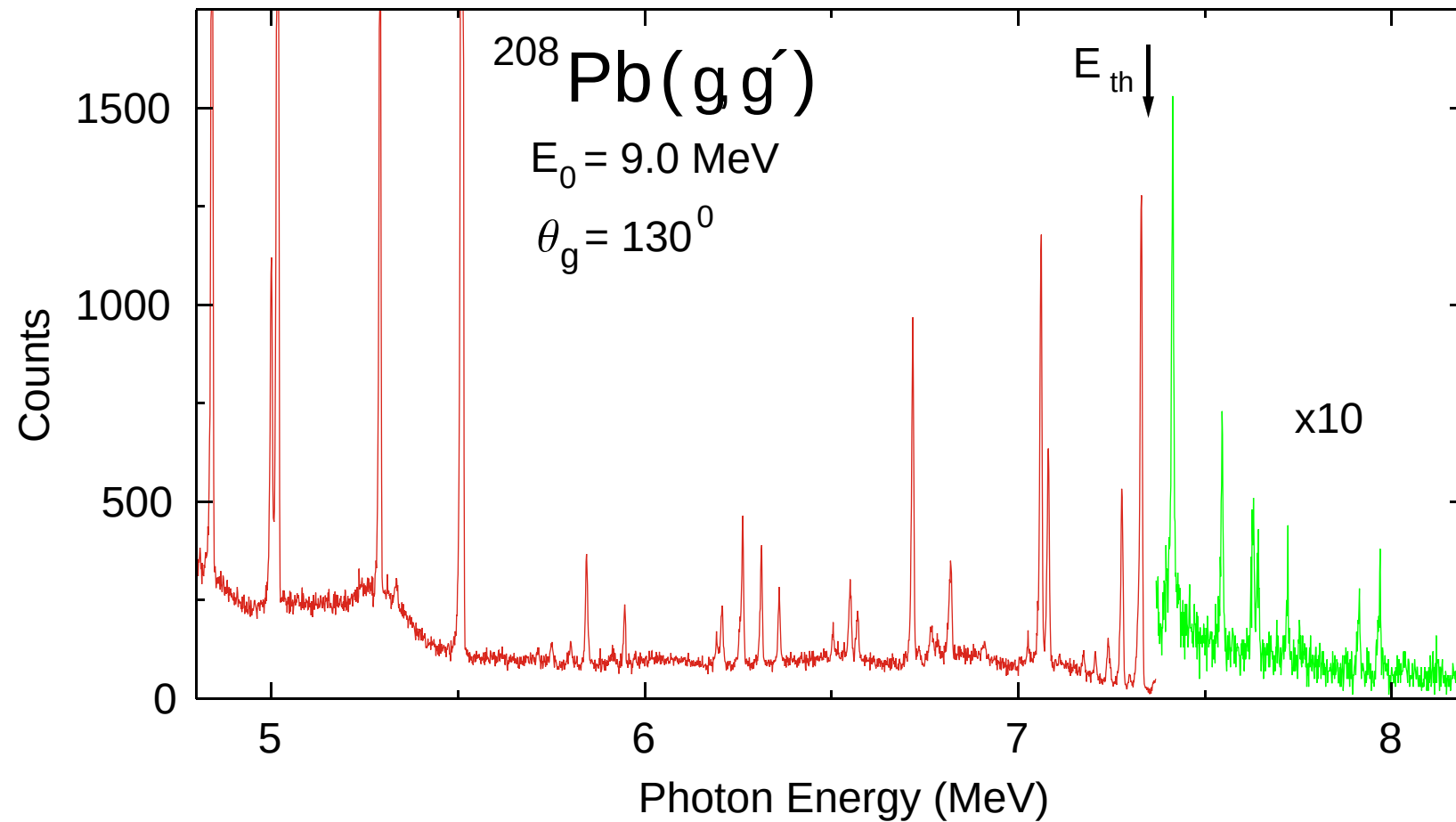
D. Vretenar,^{1,2} N. Paar,¹ P. Ring,¹ and G. A. Lalazissis^{1,3}

The isovector dipole response in ^{208}Pb is described in the framework of a fully self-consistent relativistic random phase approximation. The NL3 parameter set for the effective mean-field Lagrangian with nonlinear meson self-interaction terms, used in the present calculations, reproduces ground state properties as well as the excitation energies of giant resonances in nuclei. In addition to the isovector dipole resonance in ^{208}Pb , the present analysis predicts the occurrence of low-lying $E1$ peaks in the energy region between 7 and 11 MeV. In particular, a collective state has been identified whose dynamics correspond to that of a dipole pygmy resonance: the vibration of the excess neutrons against the inert core composed of an equal number of protons and neutrons.

... Experimental information on the fragmentation of $E1$ strength in ^{208}Pb is, however, only available in the energy window 8–12 MeV [11–13], and below 6.5 MeV [14]. In order to test the predictions of the present analysis, it would be important to obtain experimental data also in the energy region between 6 and 8 MeV.



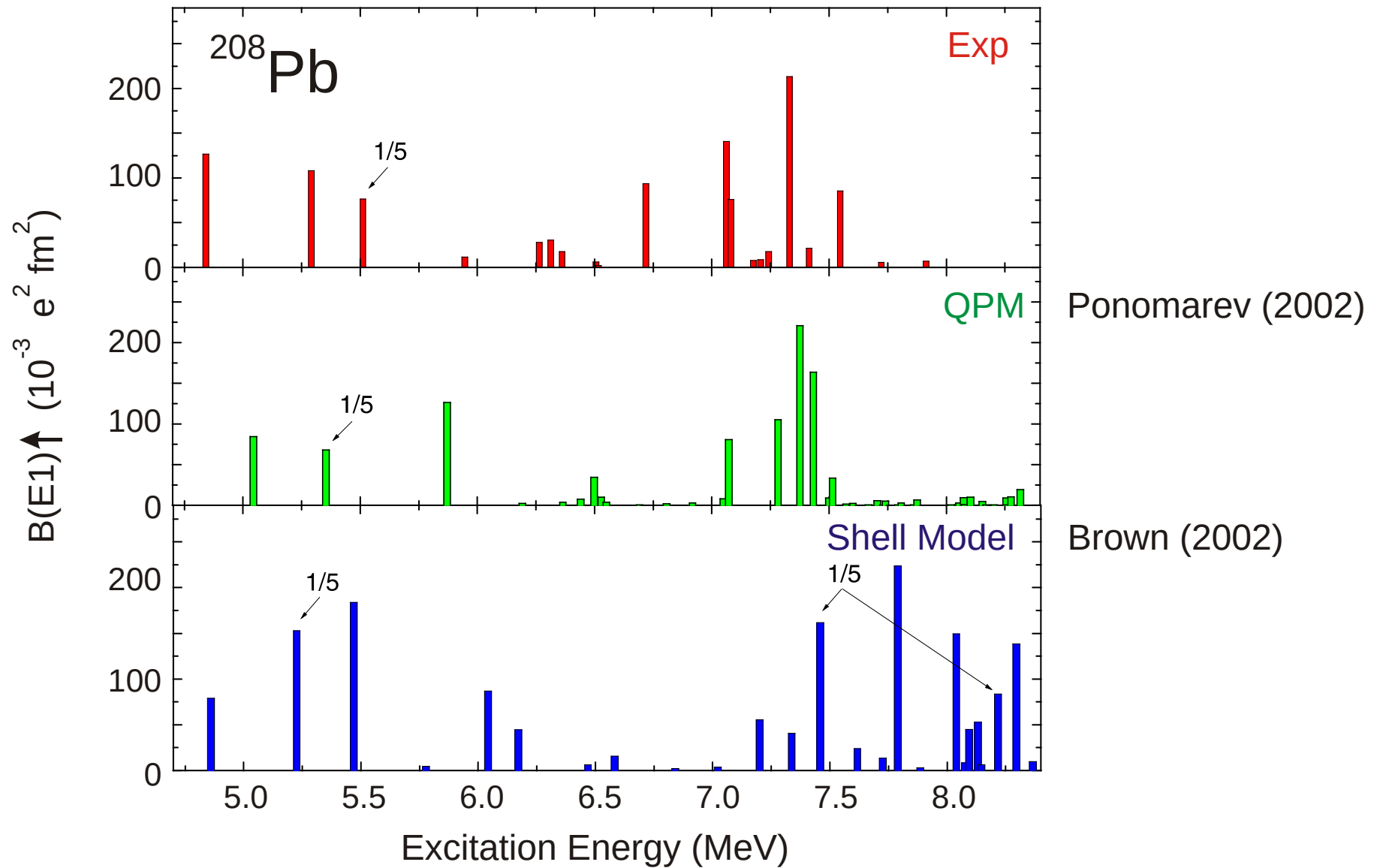
NRF Spectrum



- N. Ryezayeva et al., Phys. Rev. Lett. 89, 272502 (2002)

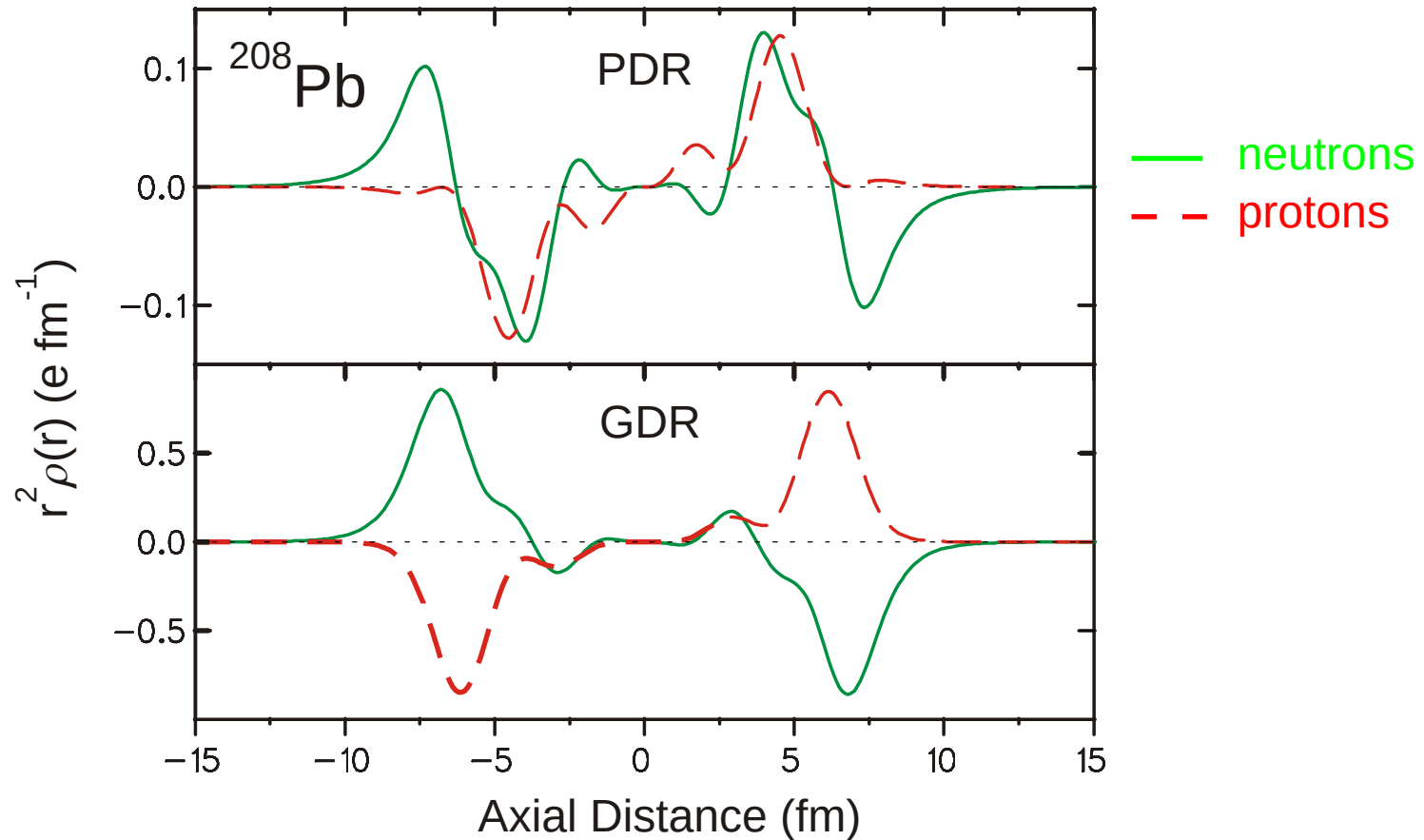


$B(E1)\uparrow$ in ^{208}Pb





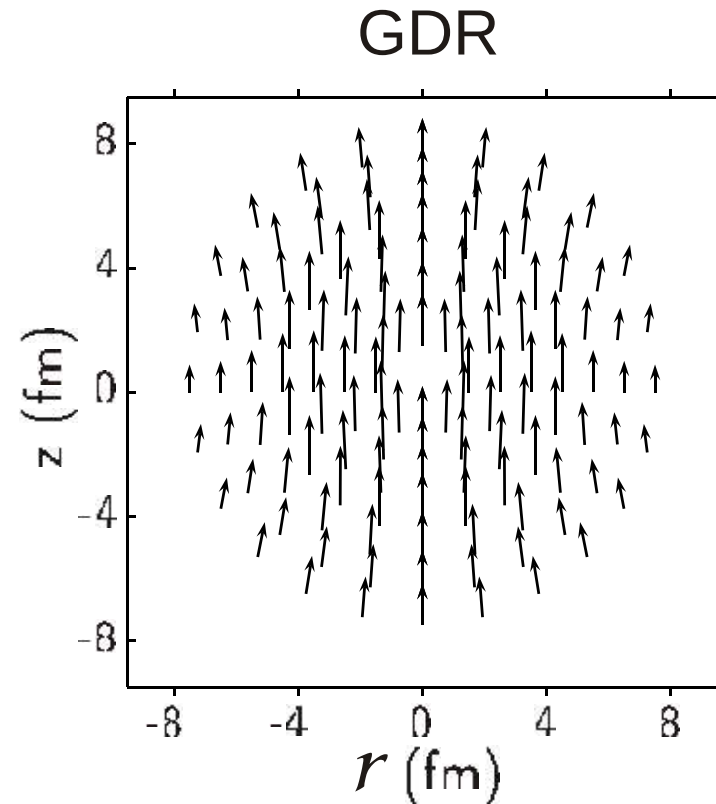
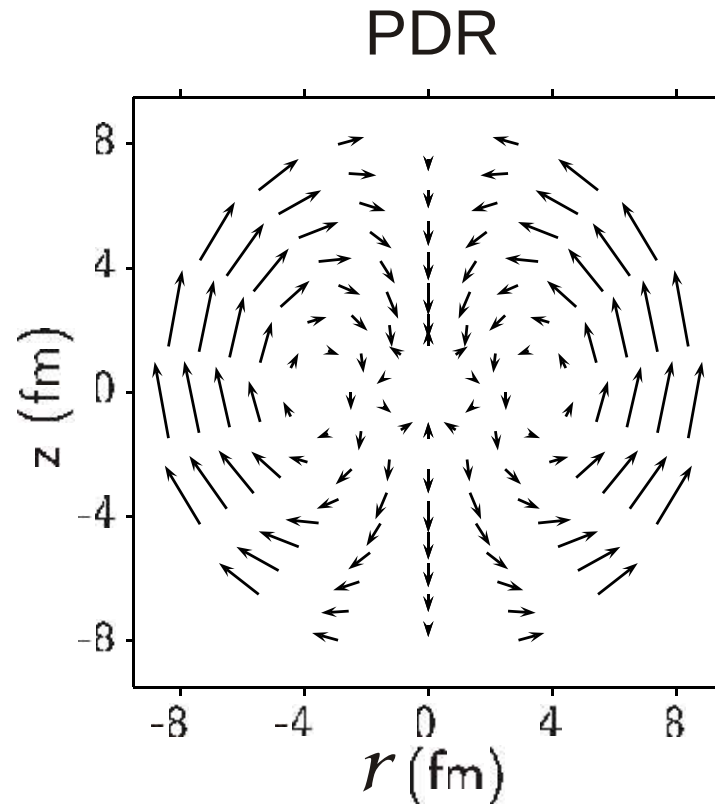
Electric Dipole Response of Neutrons and Protons



- PDR largely isoscalar
- Evidence for surface neutron density oscillations
- Similar results from the Milano and Munich groups



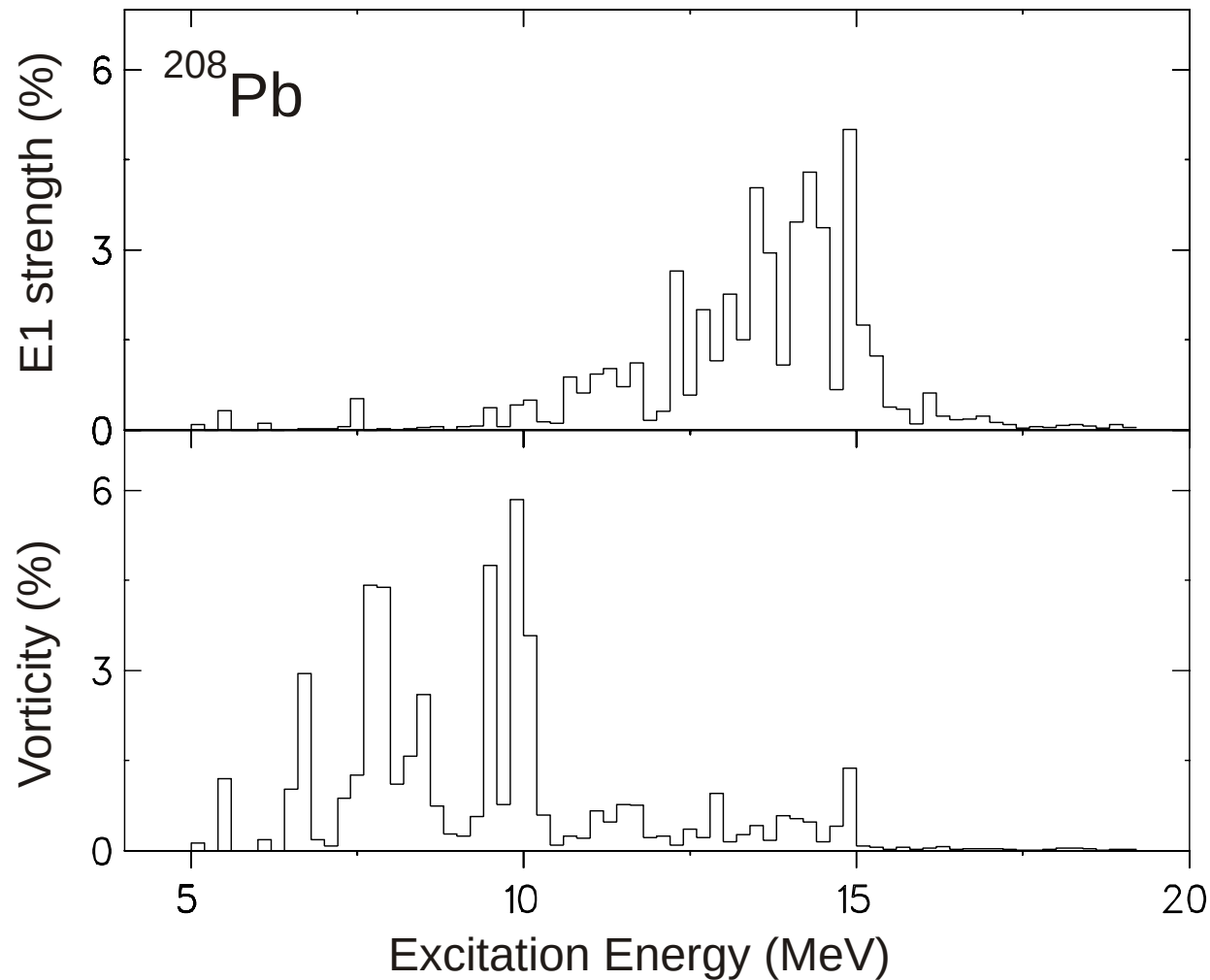
“Snapshots” of Velocity Distribution in ^{208}Pb



- Toroidal (current) mode: zero sound wave
- Restoring force is not of hydrodynamic nature but elastic
- Vibrational mode



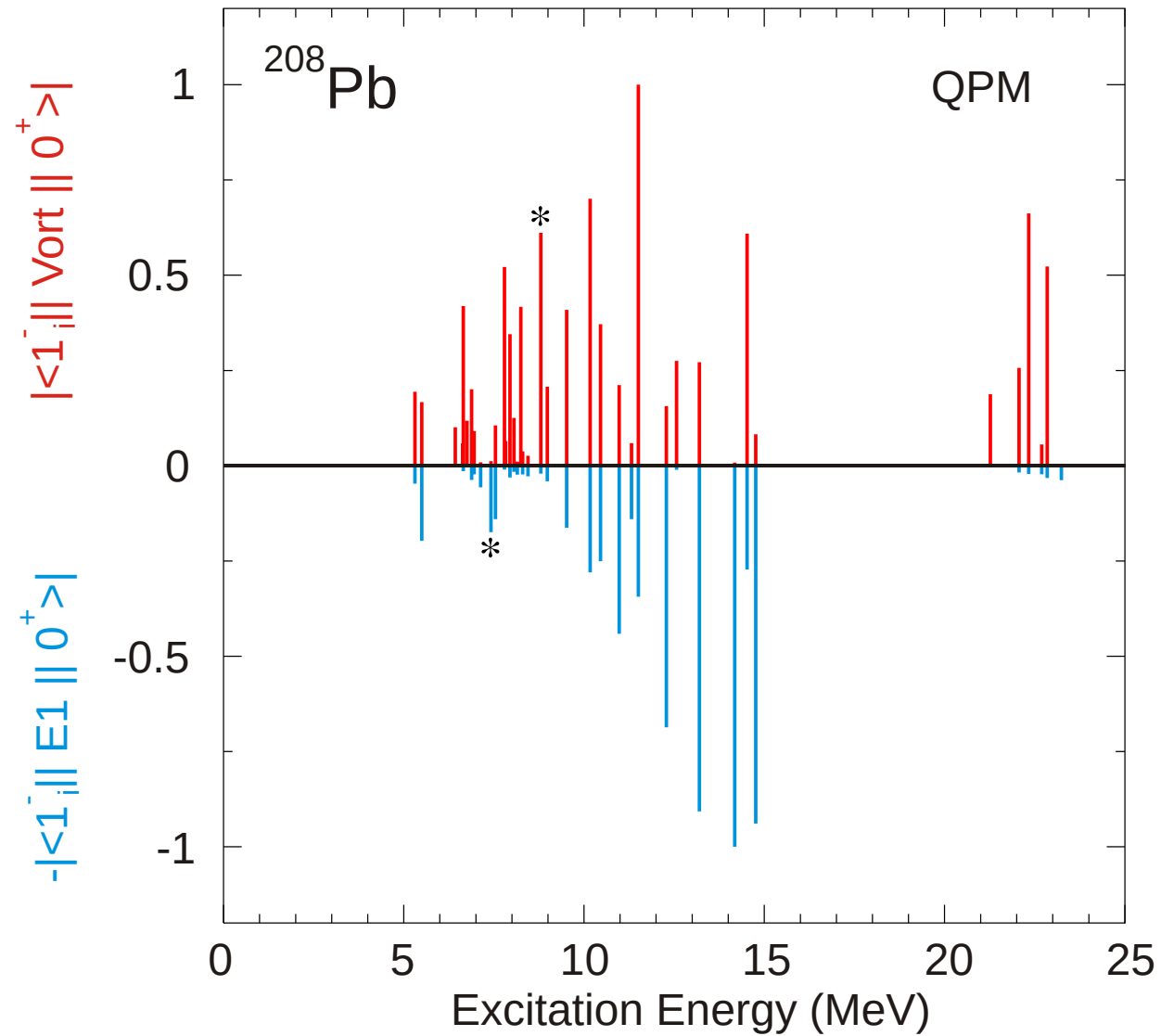
Electric Dipole Strength and Vorticity



- Vorticity density: measure for the strength of the transverse current

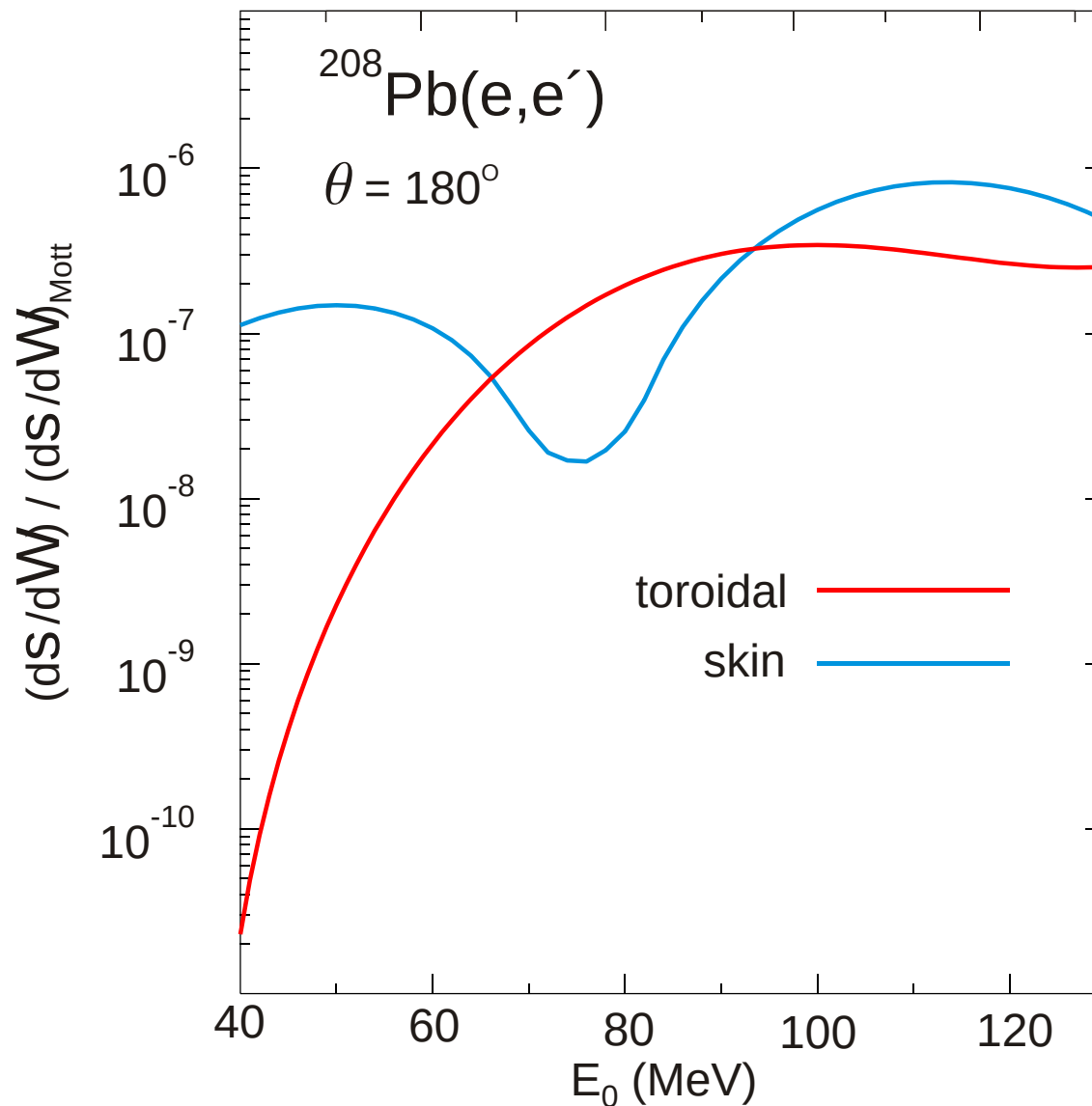


E1 Strength vs. Vorticity





Form Factors of Toroidal and Skin Modes

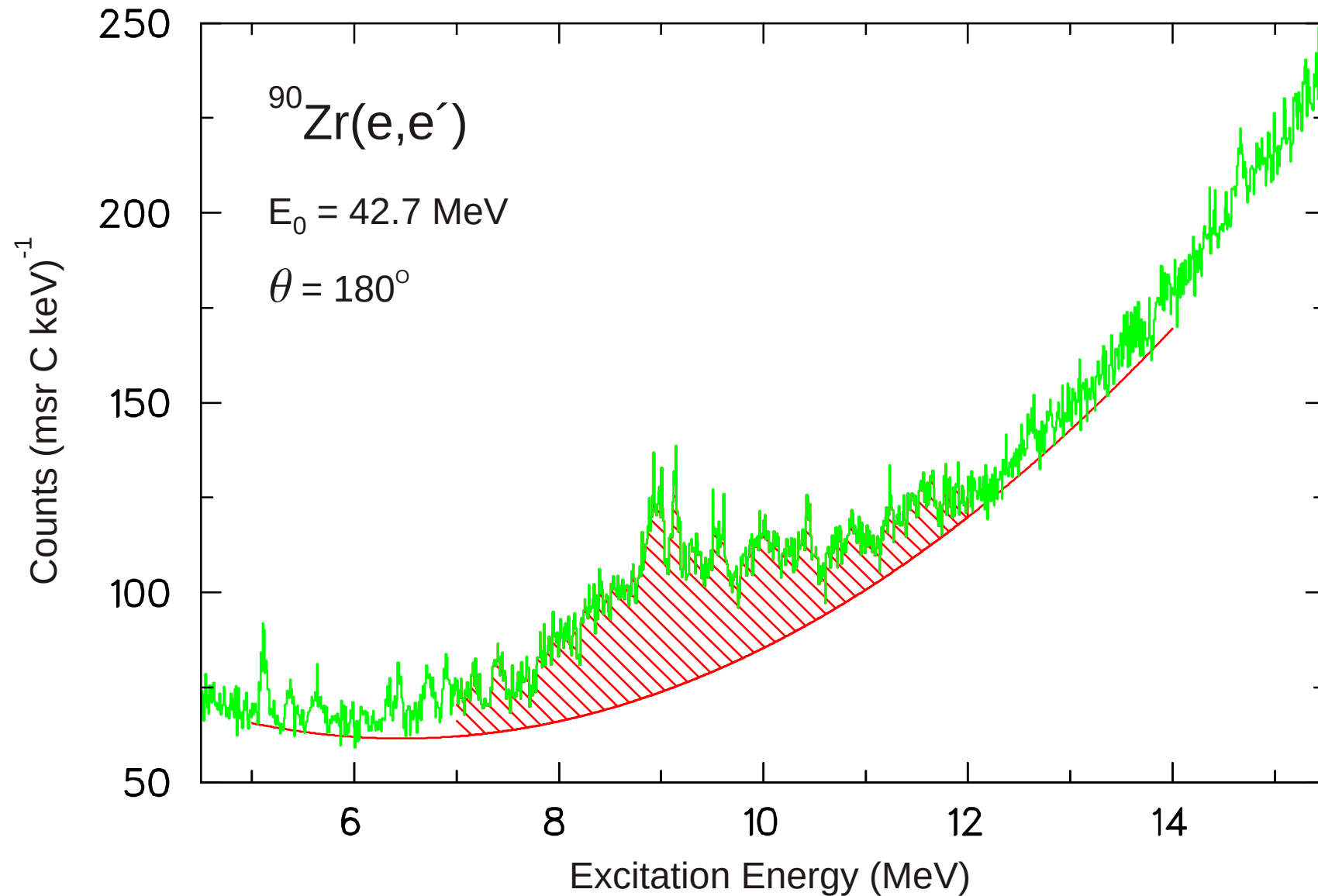




M2 and Spin Dipole Modes

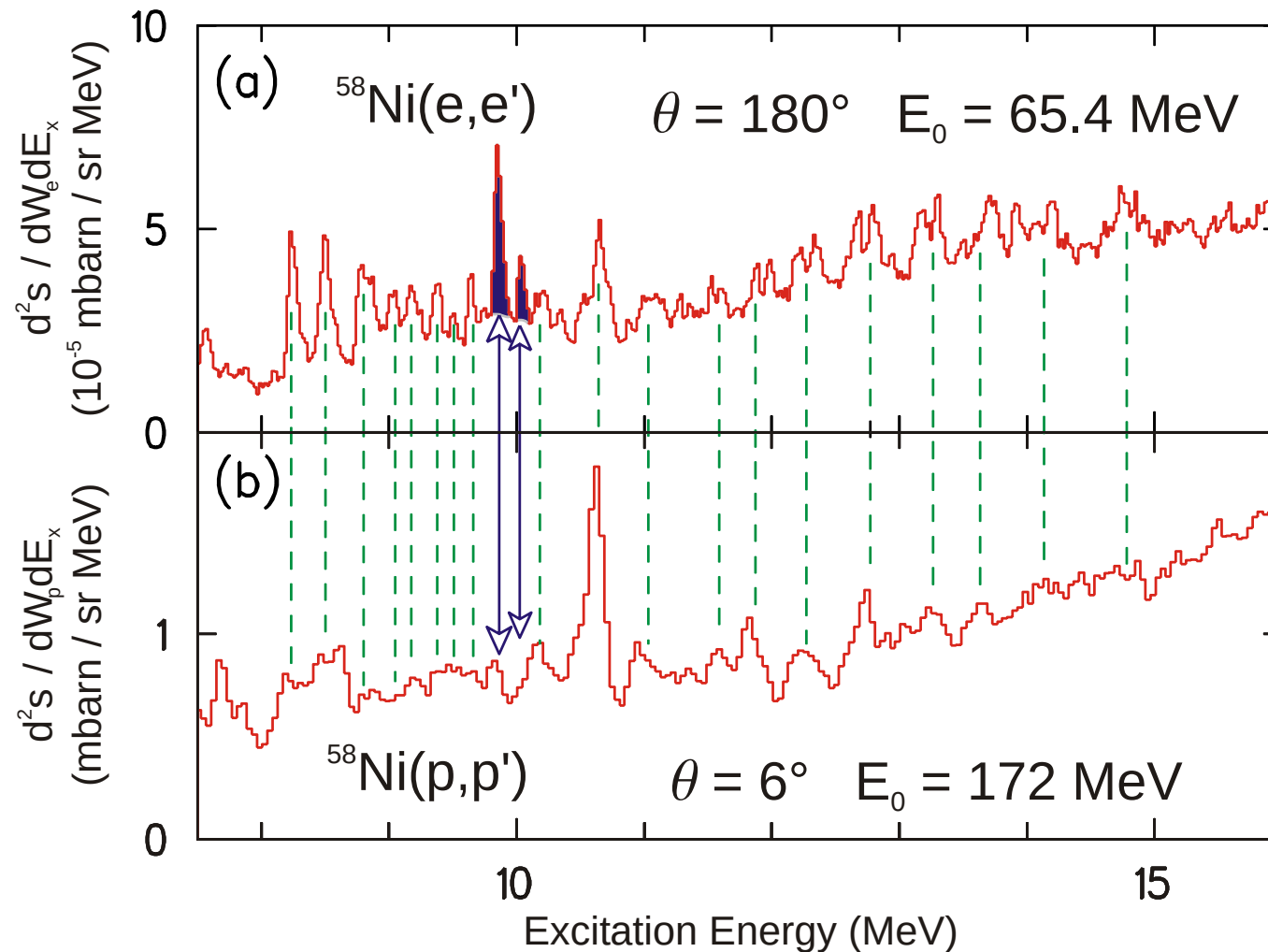


180° Electron Scattering: Selectivity





Direct Evidence for the Twist Mode

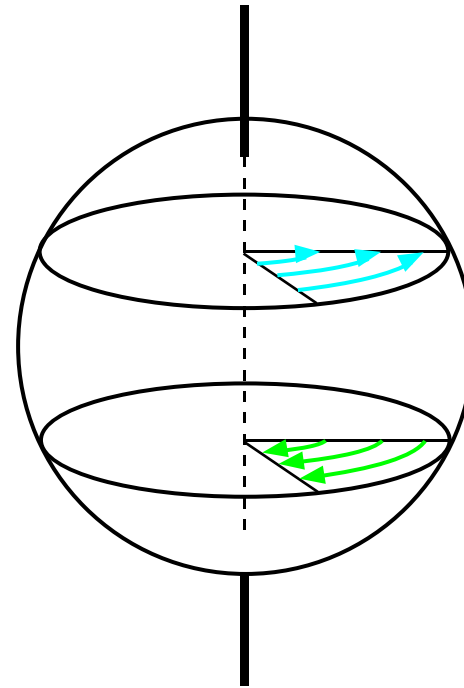
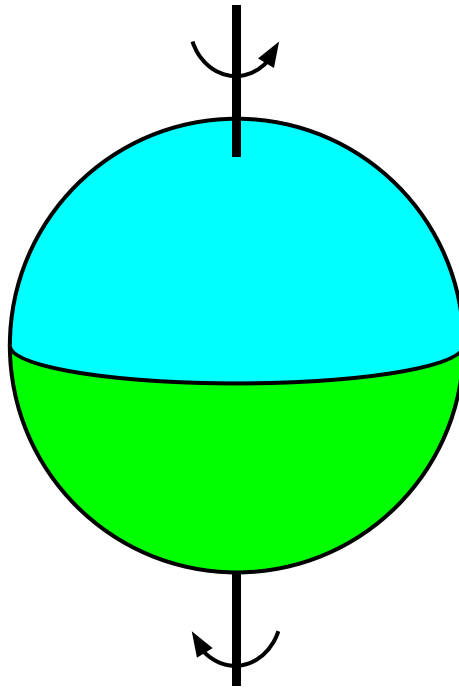


- B. Reitz et al., Phys. Lett. B 532, 179 (2002)



The $J^p = 2^-$ Twist Mode

G. Holzwarth, G. Eckart, Z. Phys A283 (1977) 219.

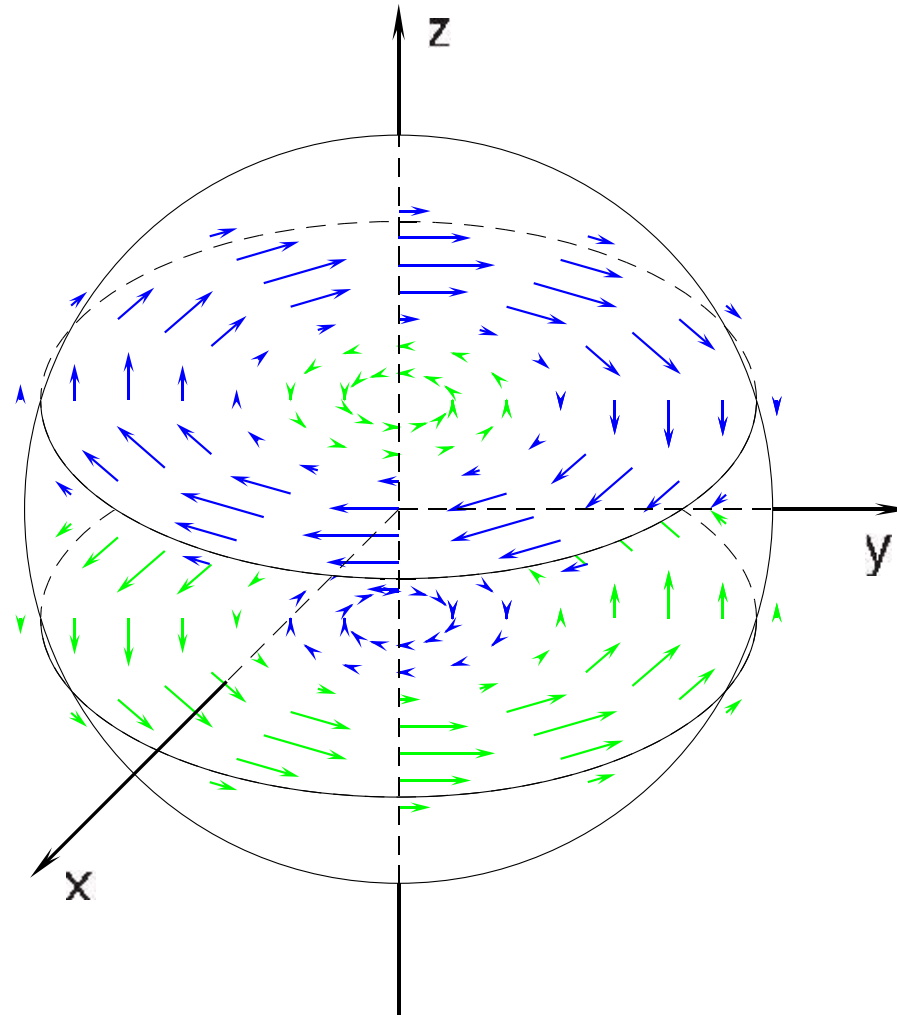


$$\text{shear module } \mu/\rho = \begin{cases} 15.3 \text{ MeV} & \text{nuclear matter} \\ 6.3 \text{ MeV} & {}^{48}\text{Ca} \\ 7.2 \text{ MeV} & {}^{90}\text{Zr} \end{cases}$$

- P. von Neumann-Cosel et al., Phys. Rev. Lett. 82, 1105 (1999)



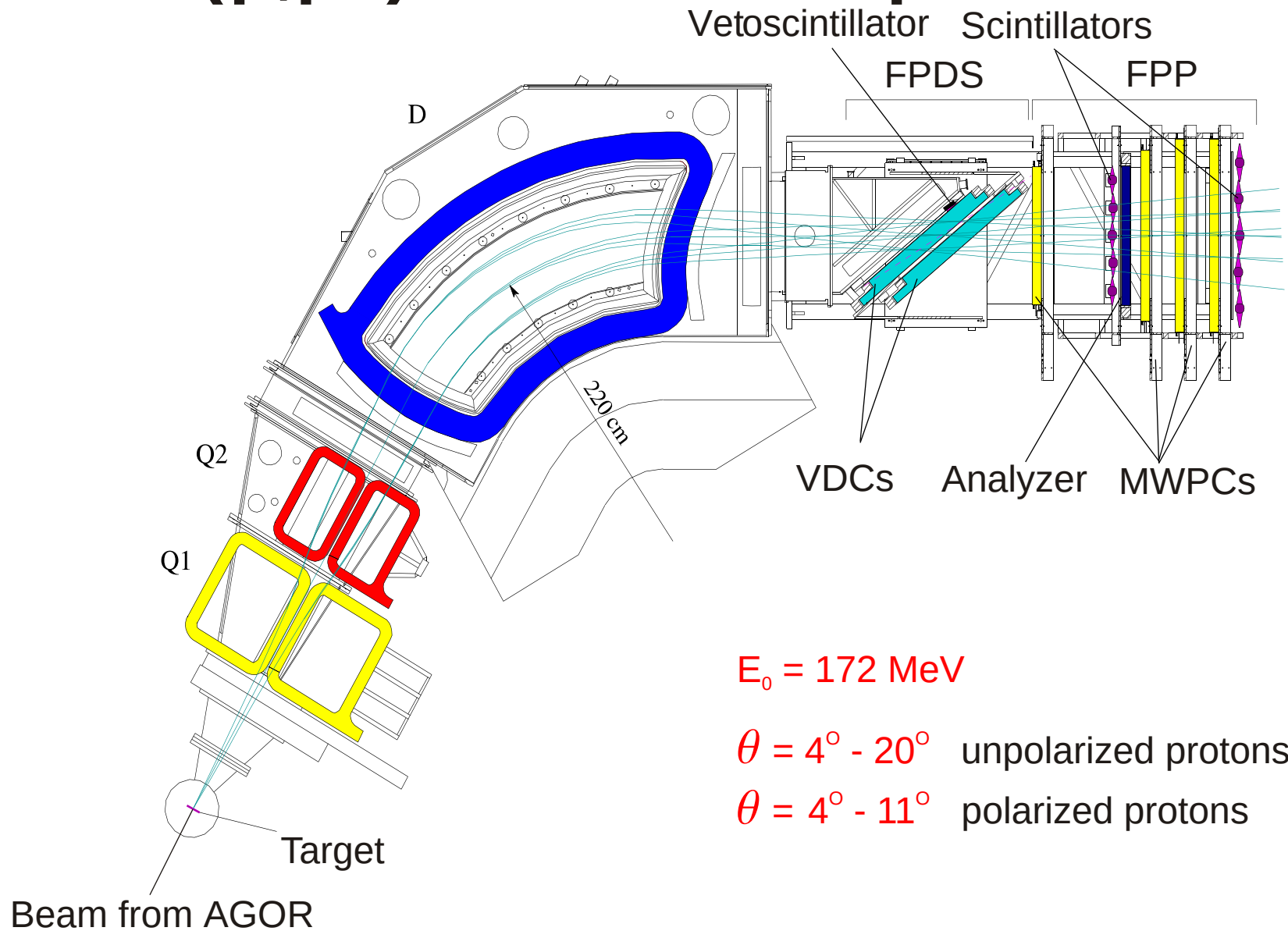
Orbital Transition Currents of the Twist Mode



- Shear module $m^*r \approx 6.5 \text{ MeV}$ (^{58}Ni)



$^{58}\text{Ni}(\vec{p}, \vec{p}')\text{ Reaction: Experimental Setup}$



$$E_0 = 172 \text{ MeV}$$

$$\theta = 4^\circ - 20^\circ \text{ unpolarized protons}$$

$$\theta = 4^\circ - 11^\circ \text{ polarized protons}$$



Effective NN Interaction

Model I: G-Matrix + Paris Potential $\Rightarrow$ von Geramb

Model II: G-Matrix + Bonn potential $\Rightarrow$ Karataglidis et al.

Model III: t-Matrix $\Rightarrow$ Love and Franey

Ground State and Excited States

2p2h Quasiparticle Phonon Model $\Rightarrow$ Ponomarev

E0 - E5, M0 - M6 transitions up to $E_x = 25$ MeV



Observations

- Quality of model description of experimental observables improves for

$$d^2s / dW dE_x \rightarrow S_{nn'} d^2s / dW dE_x \rightarrow S_{nn'}$$

- Possible reason: reaction part - in particular the non-spin part of the continuum is not correctly described
- Nuclear structure part seems to be correct

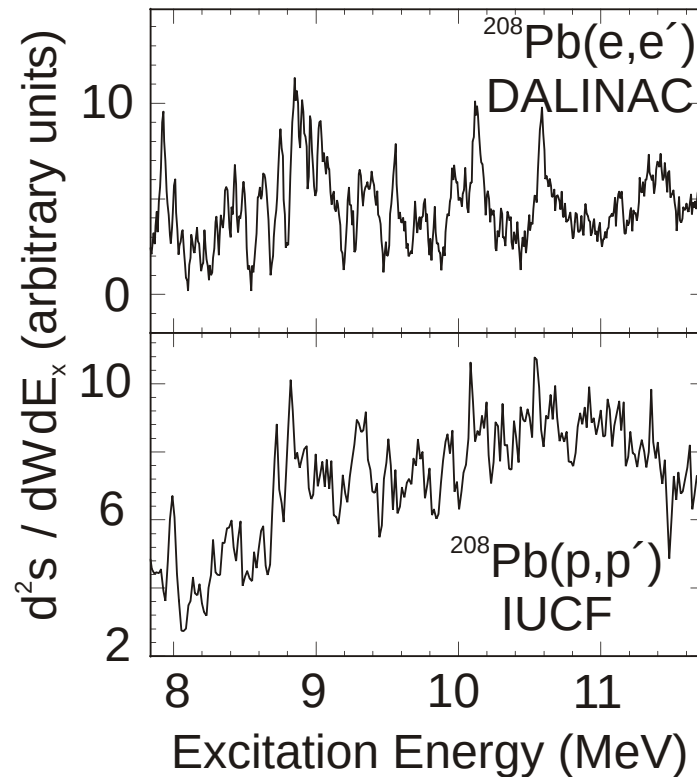


Fine Structure and Characteristic Scales

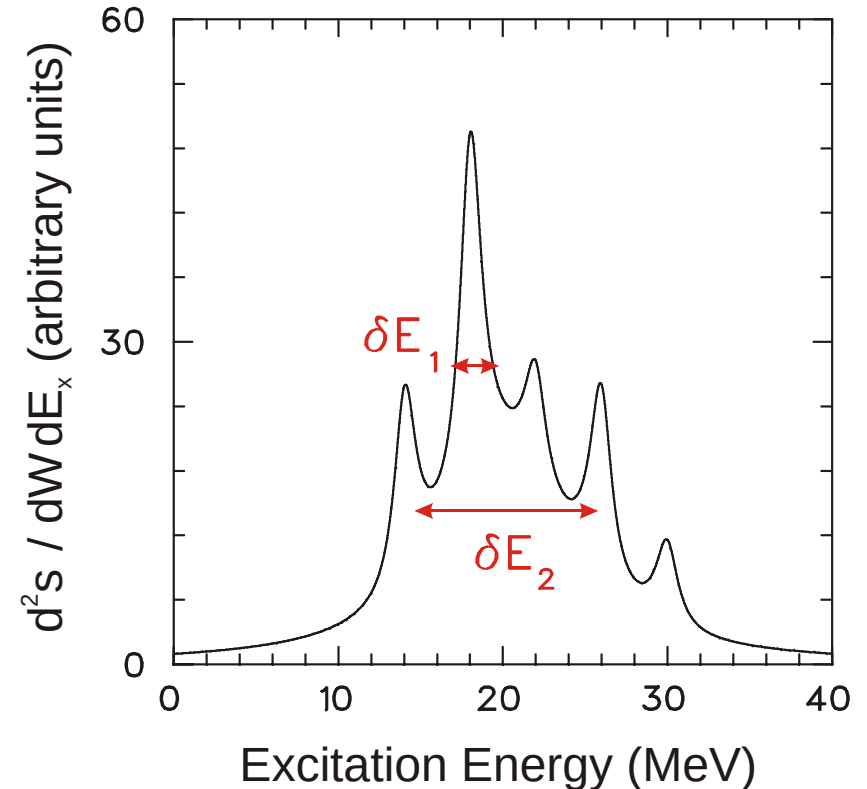


Fine Structure of Giant Resonances

Different Probes - Similar Structures



Multiple Scales of Fluctuations



Search for characteristic energy scales of fluctuations:

- Entropy Index Method
- Local Scaling Dimension: Aiba, Matsuo (1999)
- Wavelet Analysis



Entropy Index Method

D. Lacroix and P. Chomaz, Phys. Rev. C **60**, 064307 (1999)

- Spectrum DE divided into n bins with binwidth δE
 $(\Delta E = n \delta E) \Rightarrow \delta E$ sets the scales

- Define coefficient

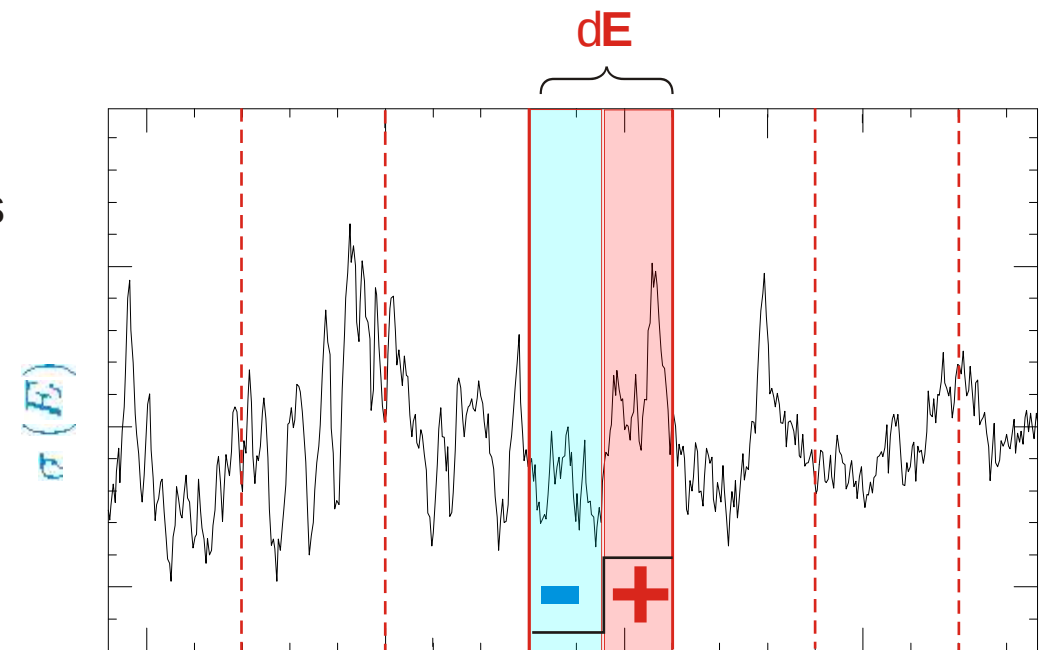
$$D_j(\delta E) = \int_{E_{j-1}}^{E_j} dE \sigma(E) \Omega_j(E)$$

with $\Omega_j(E) = \text{sign}(E - (j - 1/2)\delta E)$
 (Haar Wavelet)

- Define $W_j(\delta E) = |D_j| / \langle |D_j| \rangle$

- and entropy

$$K(\delta E) = -\frac{1}{n} \sum_{j=1}^n W_j(\delta E) \log W_j(\delta E)$$



Excitation Energy

$D_j(\delta E)$



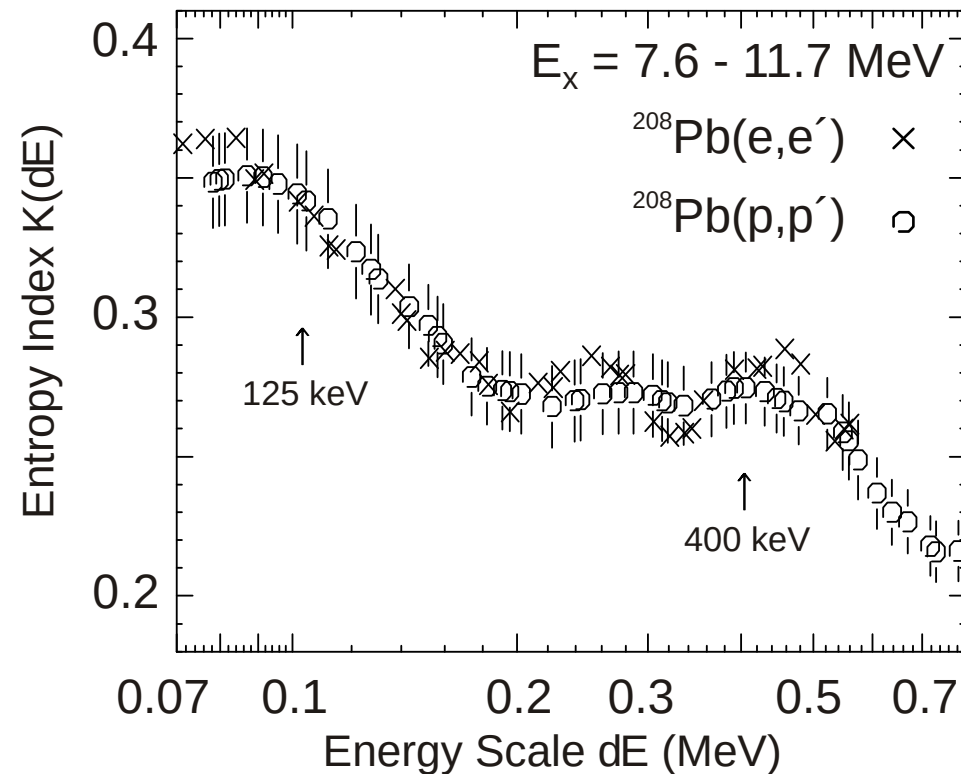
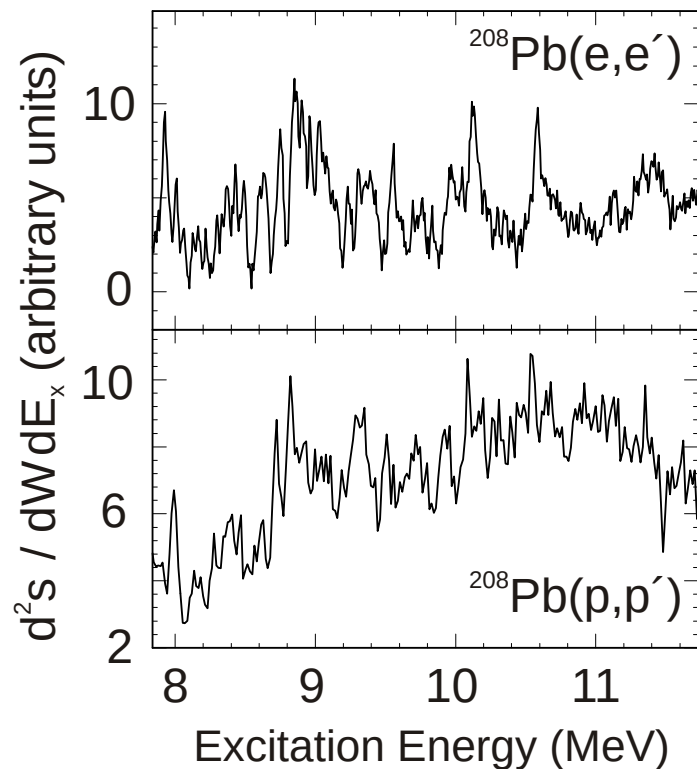
Entropy Index Properties

$$K(\delta E) = -\frac{1}{n} \sum_{j=1}^n W_j(\delta E) \log W_j(\delta E)$$

- for statistical fluctuations of D_j around the mean value
→ $K(\delta E) = \text{const}$
- for the appearance of characteristic scales
→ $K(\delta E)$ varies
- for scales with the most complex configuration
→ $K(\delta E)$ is maximal
- $K(\delta E)_{np-nh} > K(\delta E)_{mp-mh} > \dots > K(\delta E)_{1p-1h}$ where $n > m$
→ change of $K(\delta E) \iff$ onset of a new scale



Scales in (e,e') and (p,p'): The Example ^{208}Pb



- Experimental evidence for scales at 1.1 MeV, 400 keV, 125 keV
- Scales are independent of the probes
- Similar scales are found in SRPA: D. Lacroix et al., Phys. Lett. B479 (2000) 15



Scales in the Fine Structure of Giant Resonances

- Global phenomenon?
 - Other nuclei
 - Other resonances
- Is the wavelet analysis unique?
- Final goal: physics of the scales → $G^\uparrow$, $G^\downarrow$, CRPA, ...
- Posters by Kalmykov et al.,
Shevchenko et al.

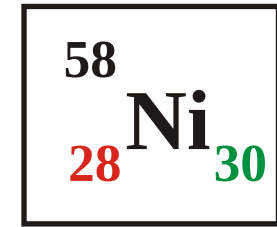
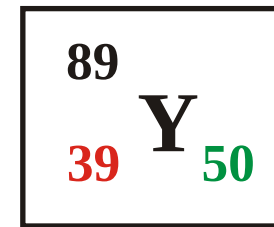
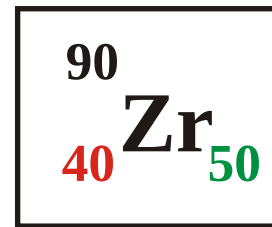
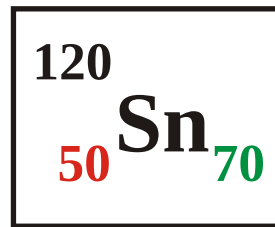
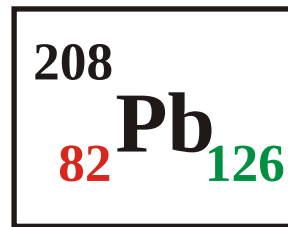


Recent Experiments

Place: iThemba LABS in South Africa

Reaction: (p, p')

Targets:



Beam Energy: $E_0 = 200 \text{ MeV}$

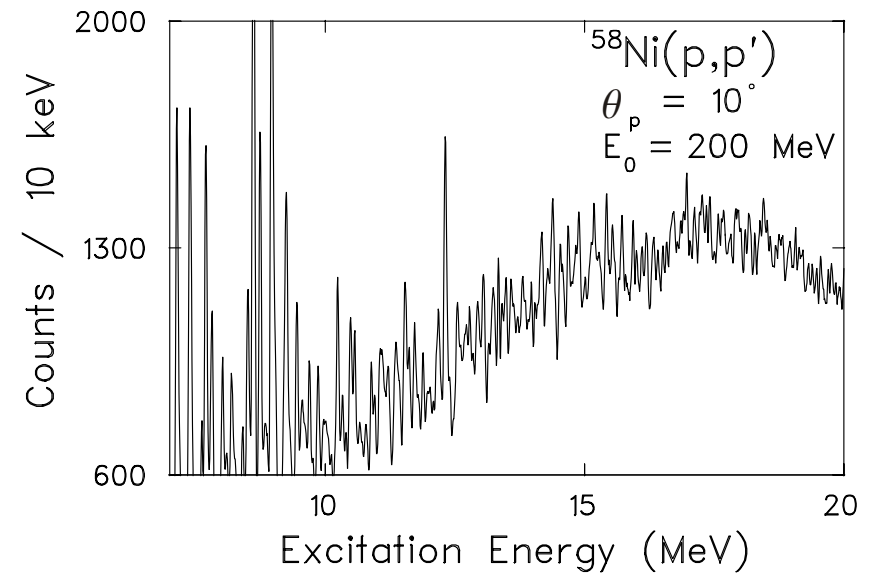
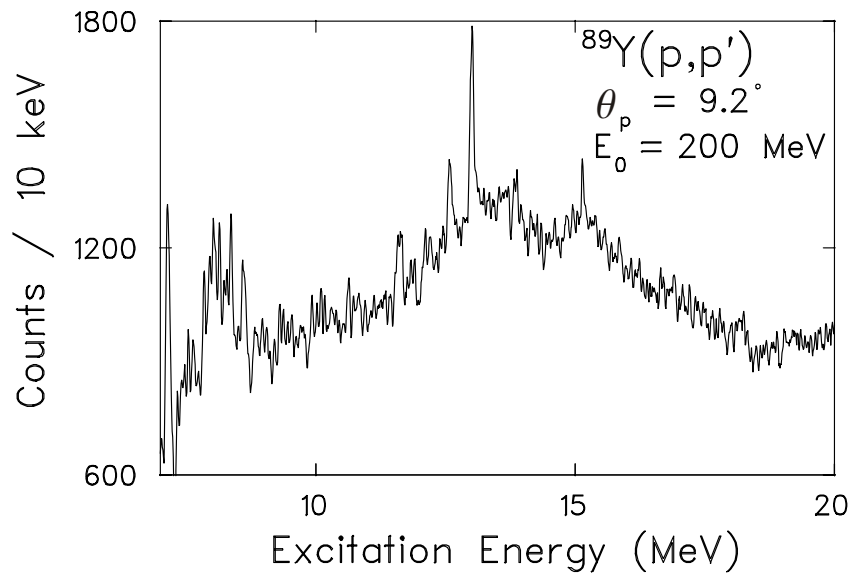
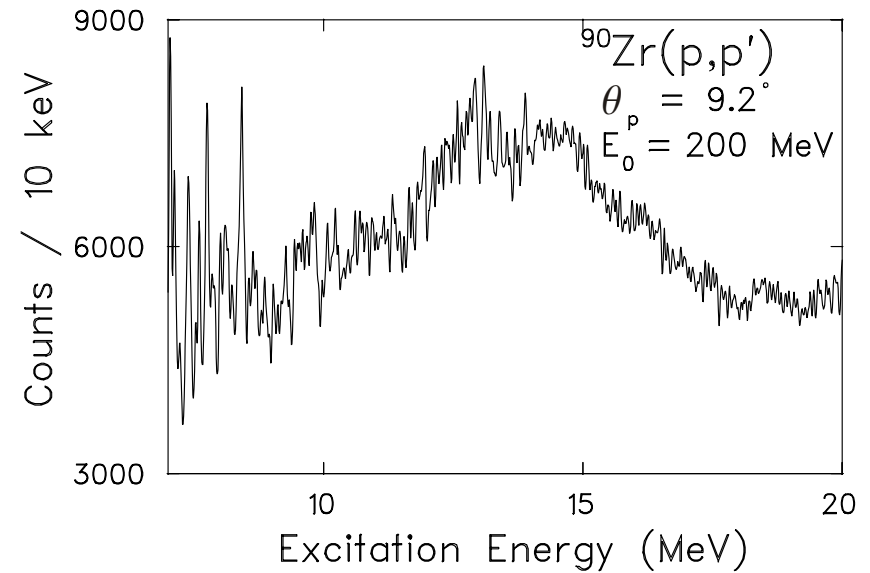
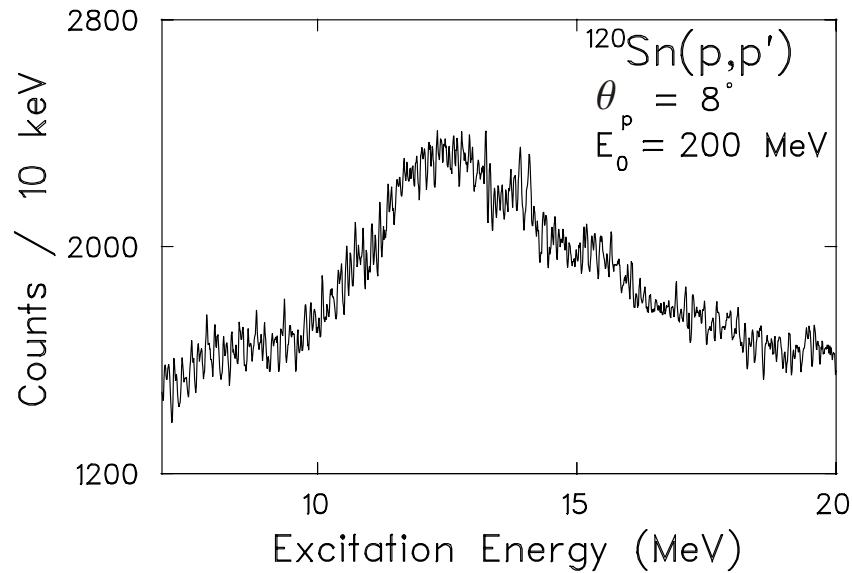
Excitation Energy Range: $E_x = 0 - 23 \text{ MeV}$

Energy Resolution (FWHM): $DE = 35 - 50 \text{ keV}$

Scattering Angles: $8^\circ - 10^\circ$
(close to maximum of $DL=2$ transitions)
 $6^\circ - 14^\circ$
(check contributions of different multipoles)

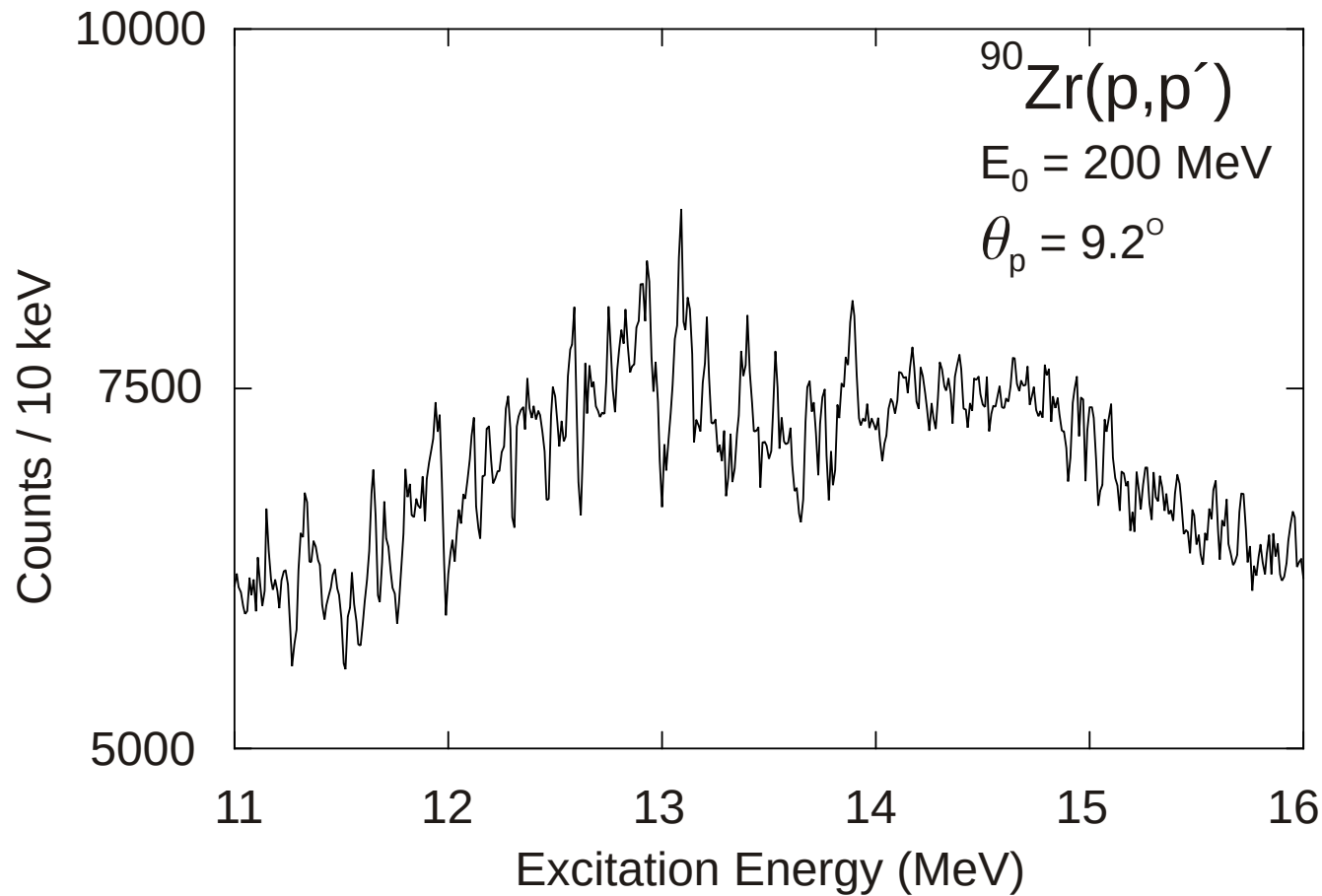


Fine Structure of the ISGQR: A Global Phenomenon?





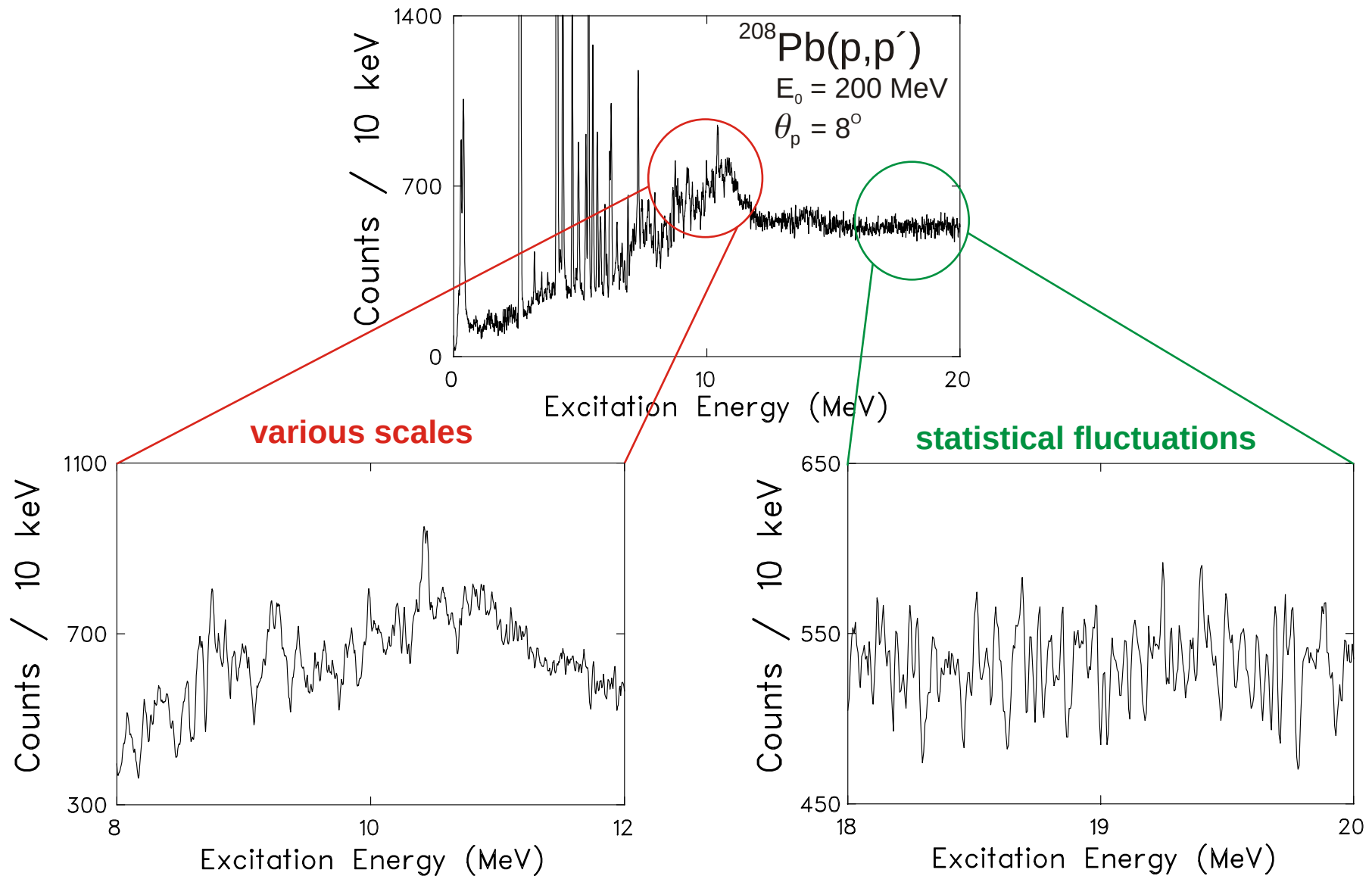
Details of the Fine Structure



- Not a Lorentzian
- Fluctuations of different strength and scales



Scales and Fluctuations





Wavelet Analysis

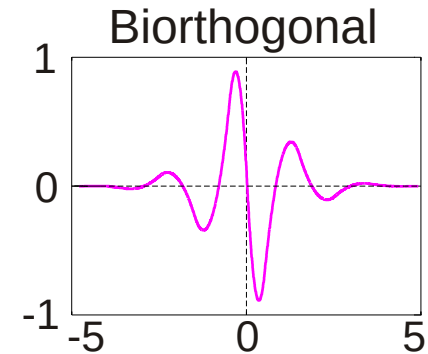
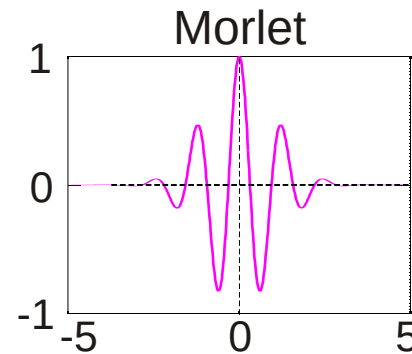
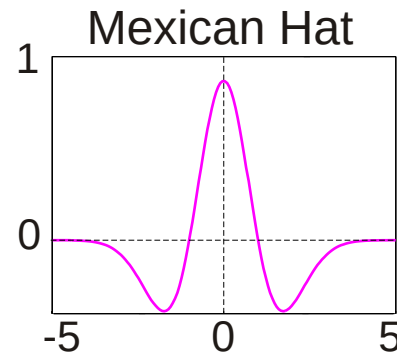
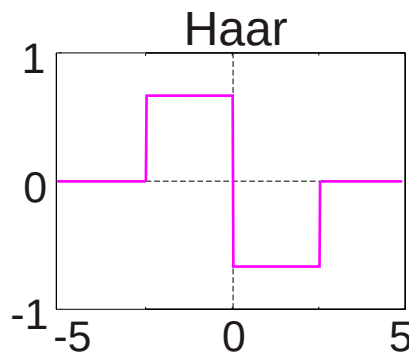
- Entropy Index Method is limited
 - ⇒ no information on localization of scales
 - ⇒ no reconstruction of original spectrum possible
- Another possibility: **Discrete Wavelet Transform**
from signal processing



Discrete Wavelet Analysis

Wavelets:

$$\int_{-\infty}^{\infty} \Psi^* (x) dx = 0$$



Wavelet
Coefficients:

$$C(\delta E, E_x) = \frac{1}{\sqrt{\delta E}} \int s(E) \Psi^* \left(\frac{E_x - E}{\delta E} \right) dE$$

↑
scale

↑
position

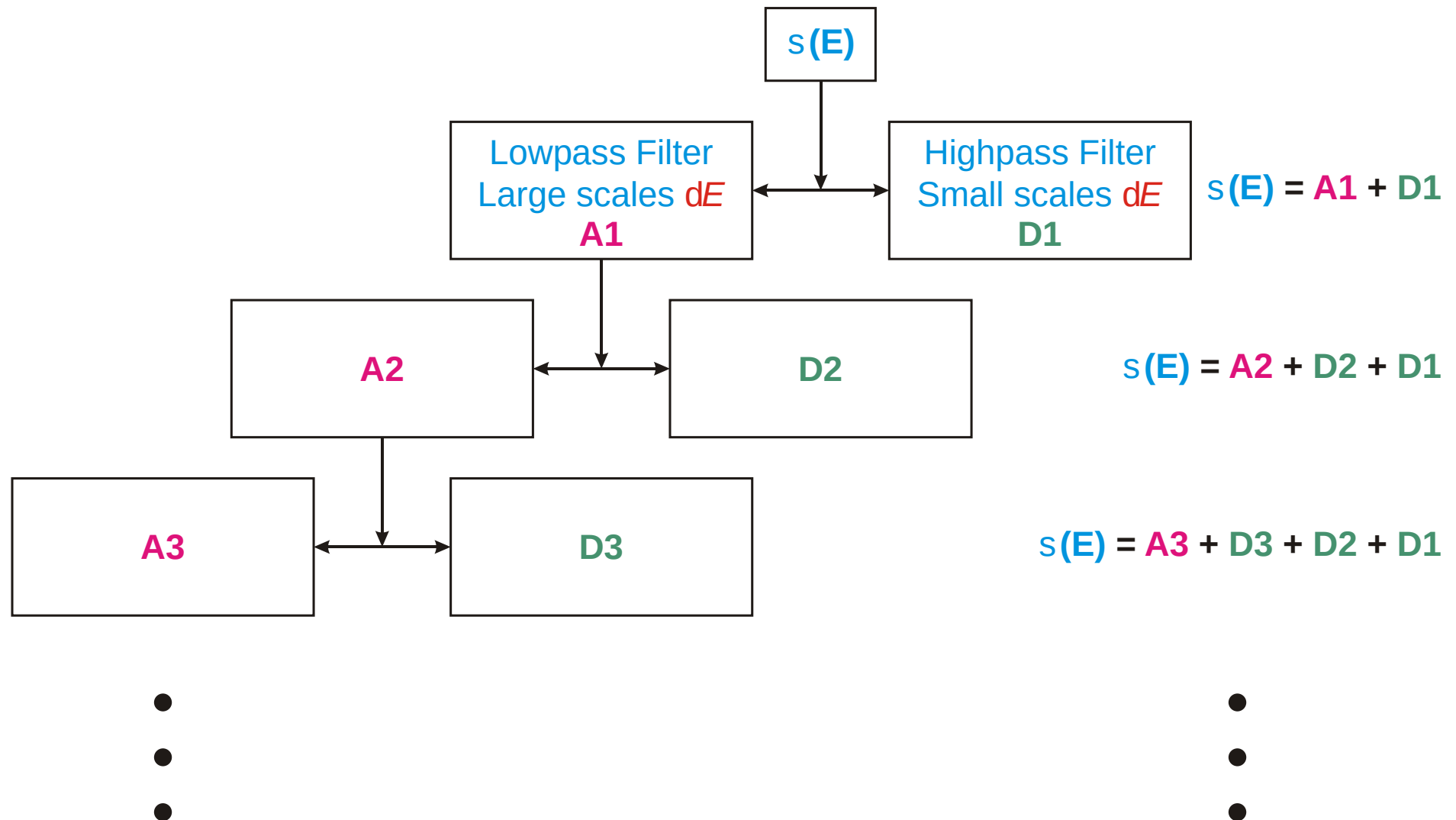
↑
spectrum

↑
wavelet

Steps: $\delta E = 2^j$ with $j = 1, 2, 3, \dots$ and $E_x = \delta E$

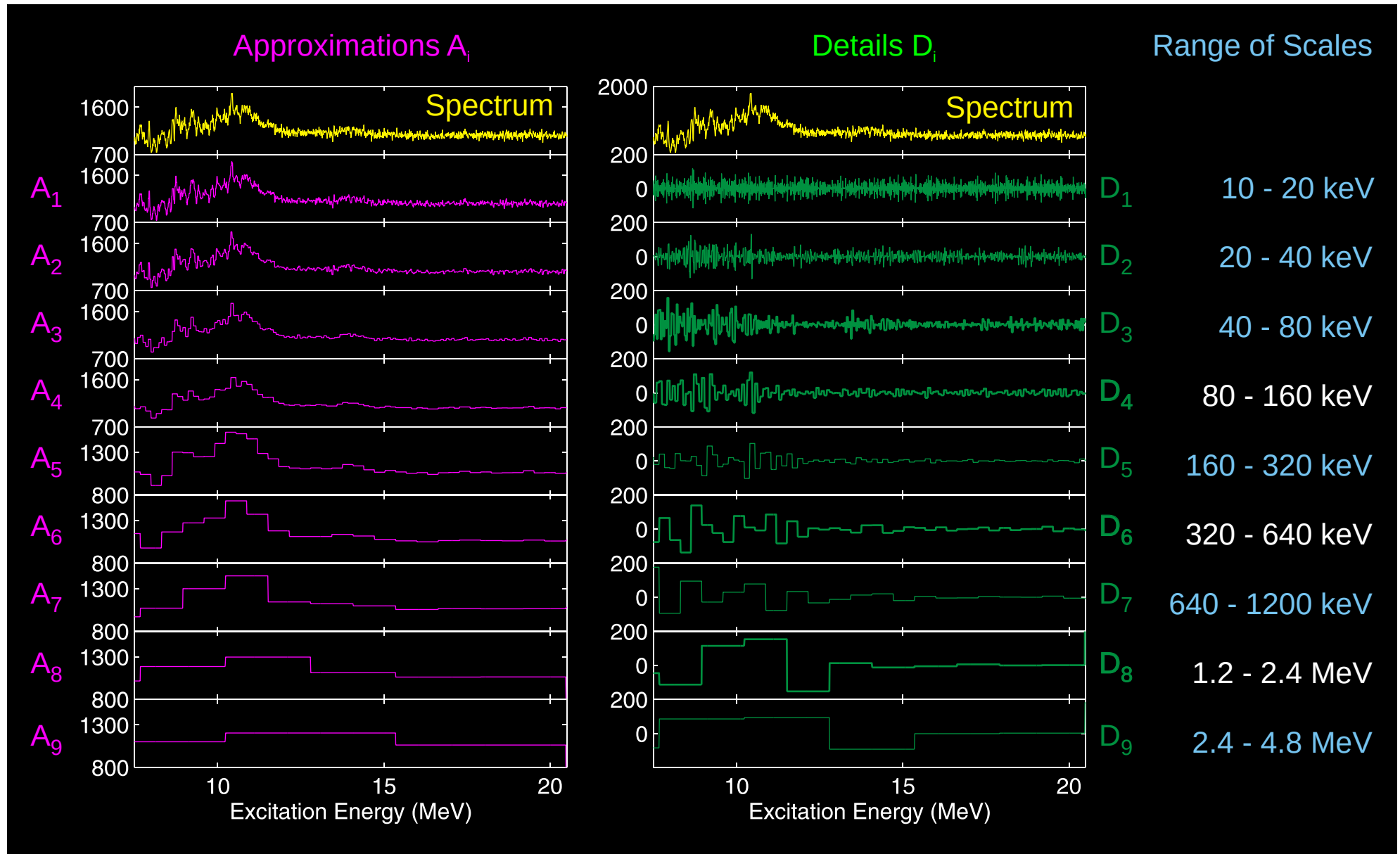


Decomposition



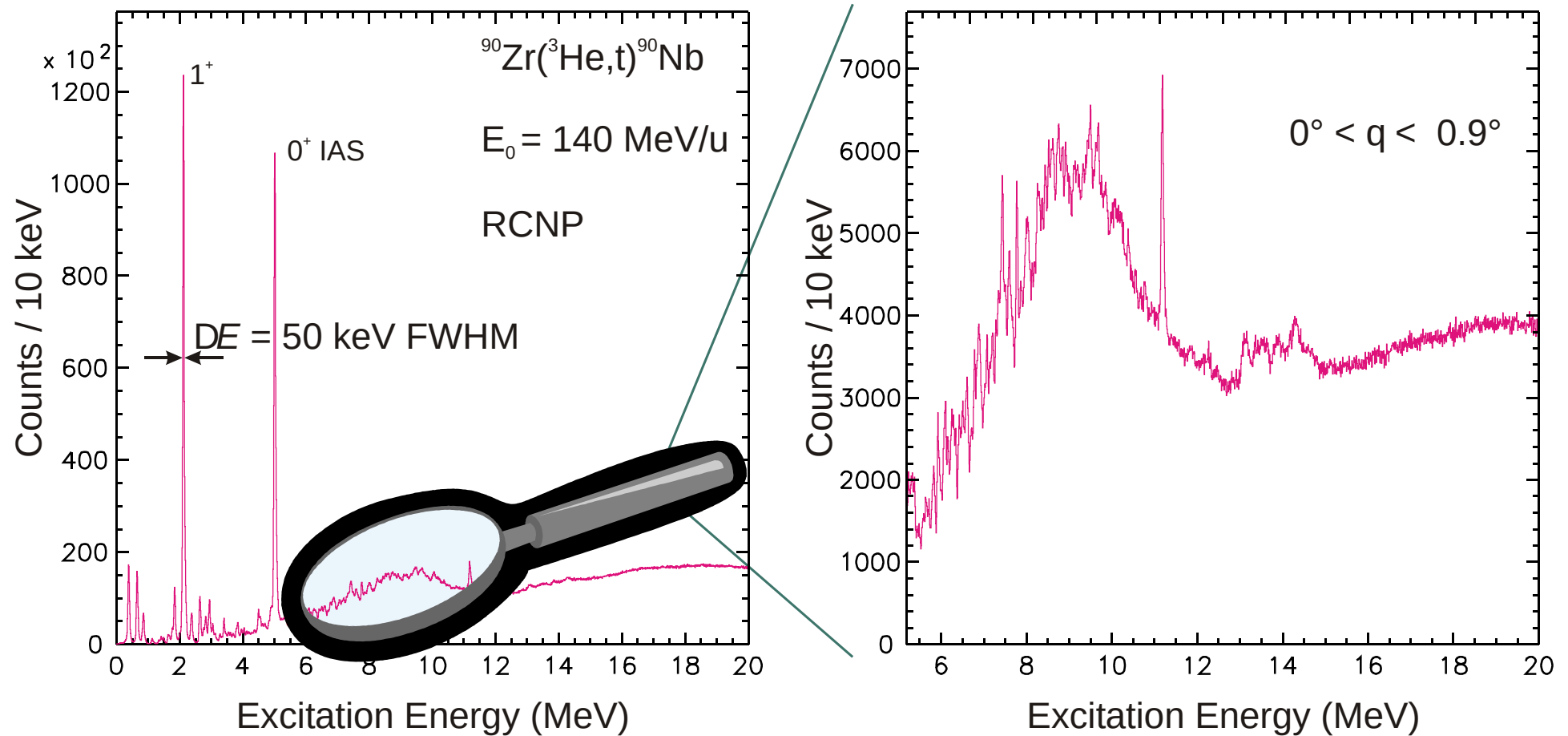


Decomposition of $^{208}\text{Pb}(p,p')$ Spectrum





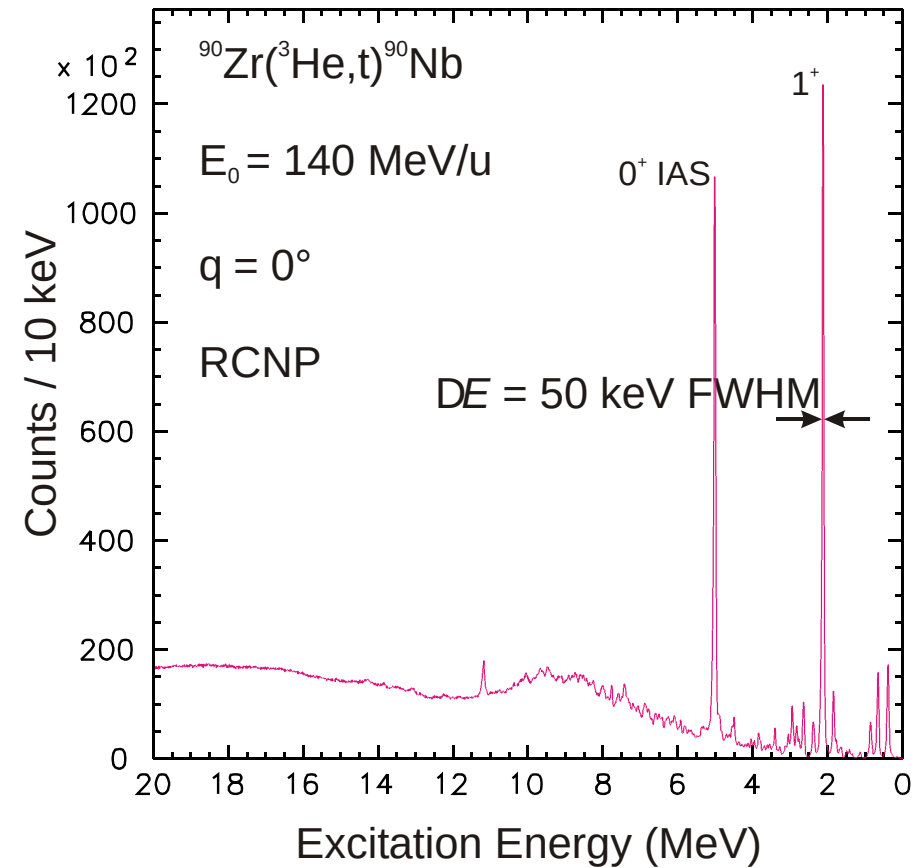
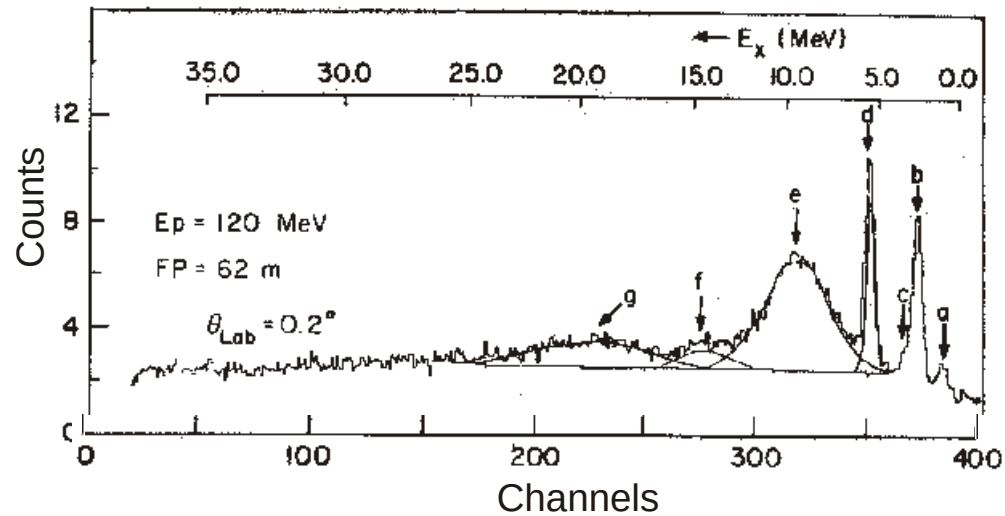
Fine Structure of the Spin-Flip GTR





Fine Structure of the Spin-Flip GTR

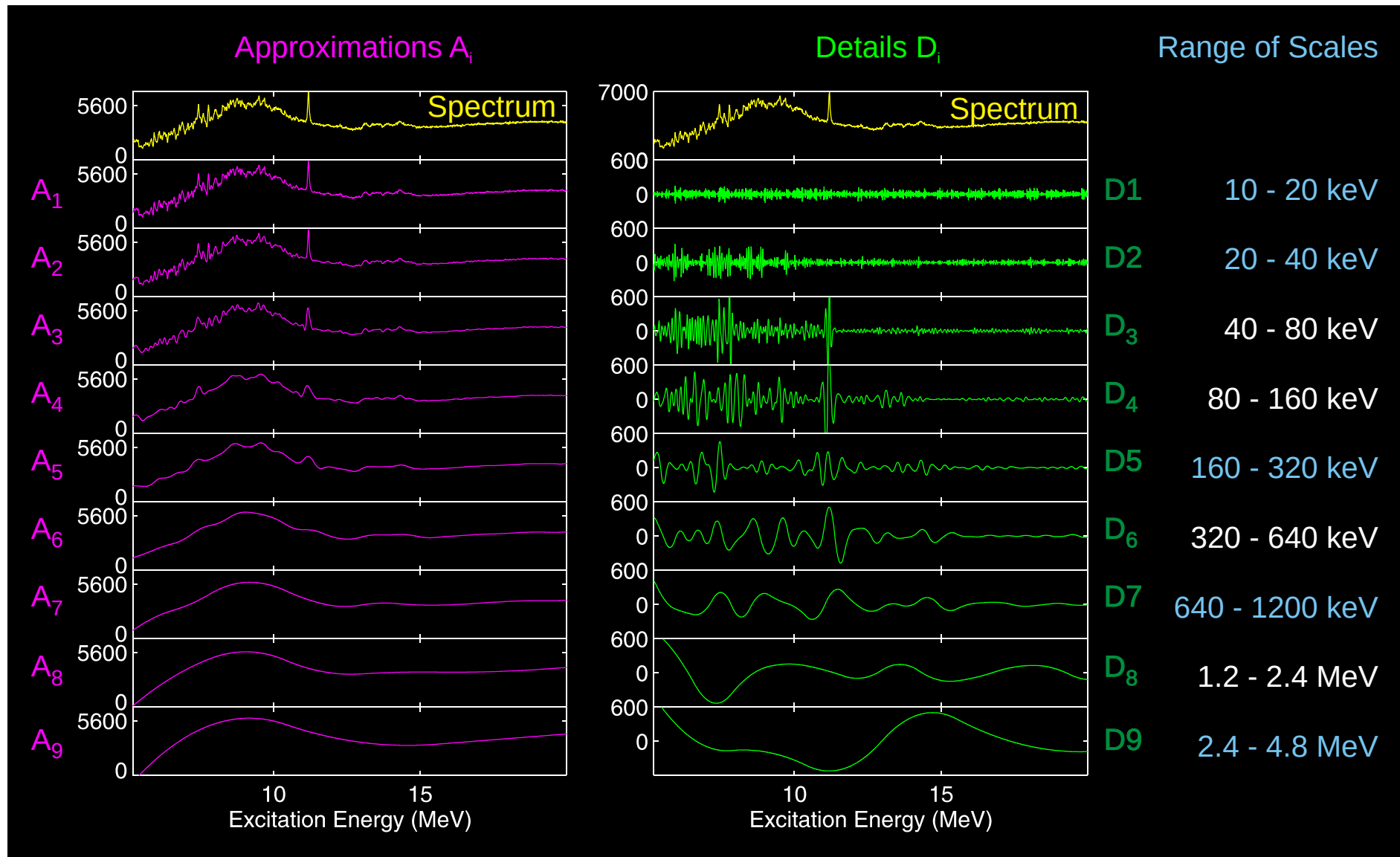
$^{90}\text{Zr}(p,n)^{90}\text{Nb}$ D. Bainum et al., Phys. Rev. Lett., **44** (1980) 1751



- observed for the first time
- scales $\rightarrow G\downarrow$ vs. $G\uparrow$ and comparison with electric GR's
- selectivity: $J^p = 1^+ \rightarrow$ level density

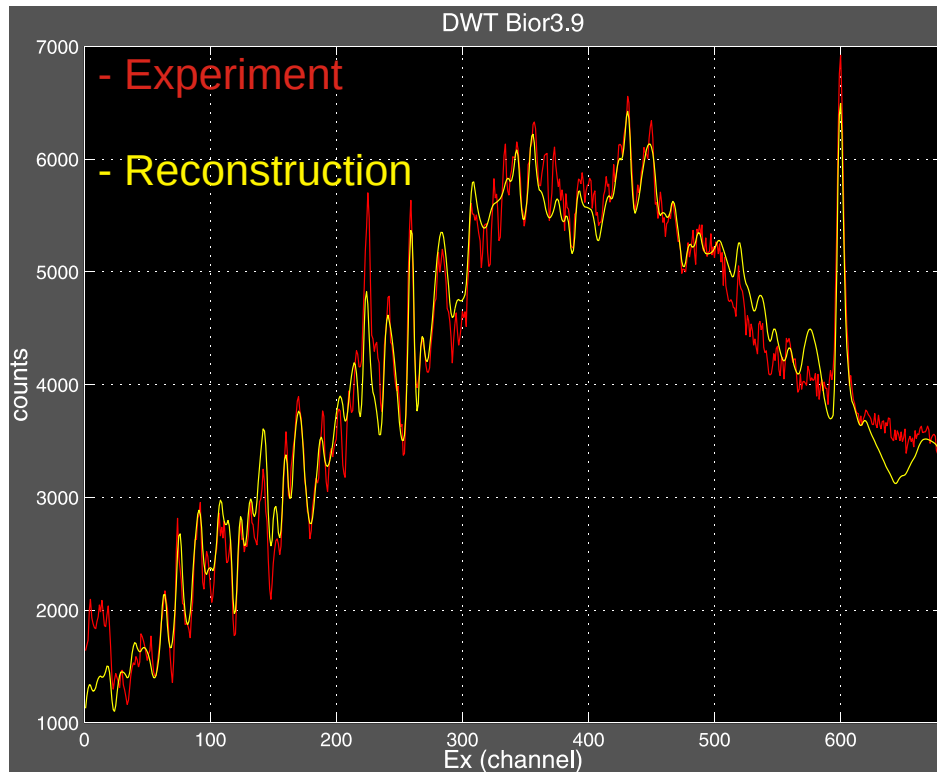


Decomposition of $^{90}\text{Zr}(^3\text{He},t)^{90}\text{Nb}$ Spectrum

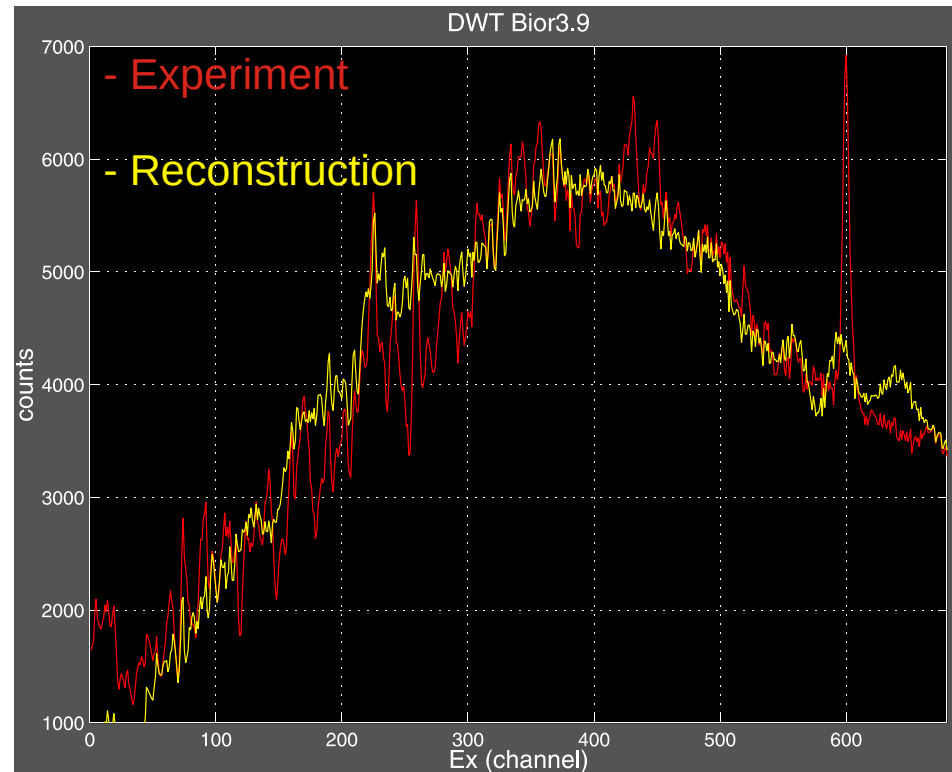




Discrete Wavelet Transform: Reconstructed Spectra



$$s_r(E) = A8 + D8 + D6 + D4 + D3$$



$$s_r(E) = A8 + D7 + D5 + D2 + D1$$



Conclusion

- PDR:
 - ➡ neutron surface density oscillations
 - ➡ toroidal (current) mode might be present
- M2 and Spin Dipole Modes:
 - ➡ direct evidence for twist mode
 - ➡ extraction of spin dipole strength from proton scattering
 - ➡ comparison with model predictions
- Fine structure of GR's and characteristic scales:
 - ➡ fine structure is a global phenomenon
 - ➡ preliminary results of fast wavelet analysis are encouraging



Photon Scattering (Nuclear Resonance Fluorescence)

