

Collective Quadrupole Modes in Nuclei – New Insights into Old Problems*

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- Quadrupole phonons as building blocks of low-energy structure
- High-resolution electron and proton scattering
- The case of ^{94}Mo
 - symmetric and mixed-symmetric phonons
 - purity of two-phonon states



Identification of Mixed-Symmetry States: Interacting Boson Model

- Pairing of nucleons to s- / d-bosons

- F-Spin: π boson: $F_0 = 1/2$
 ν boson: $F_0 = -1/2$

$$\frac{|N_\pi - N_\nu|}{2} \leq F \leq F_{\max} = \frac{N_\pi + N_\nu}{2}$$

→ $F = F_{\max}$: symmetric states

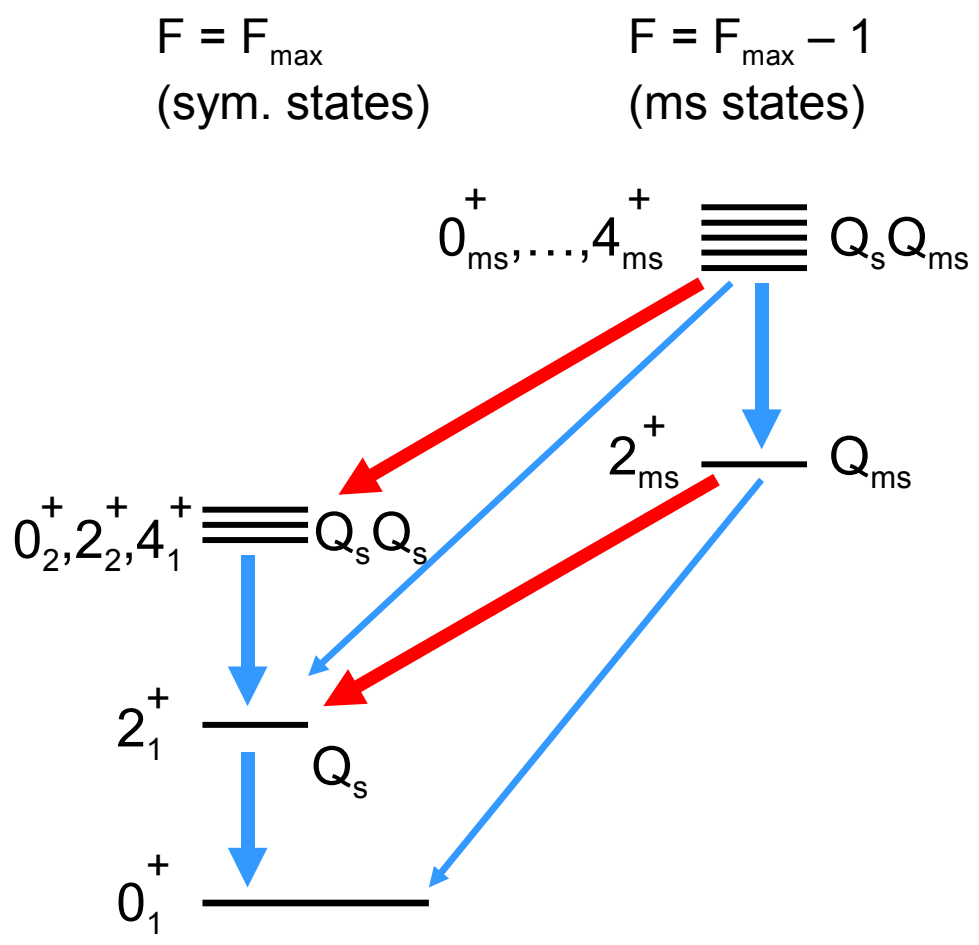
→ $F < F_{\max}$: mixed-symmetry states (ms)

- Q-phonon scheme:

$$Q_S = Q_\pi + Q_\nu \quad |2_1^+\rangle \propto Q_S |0_1^+\rangle$$

$$Q_{ms} = \frac{N}{2} \left(\frac{Q_p}{N_\pi} - \frac{Q_v}{N_\nu} \right) \quad |2_{ms}^+\rangle \propto Q_{ms} |0_1^+\rangle$$

Identification of Mixed-Symmetry States: Q-Phonon Scheme



- Strong **E2** transitions for decay of symmetric Q-phonon
- Weak **E2** transitions for decay of ms Q-phonon
- Strong **M1** transitions for decay of ms states to symmetric states

- The low-energy spectrum of ^{94}Mo is well studied and most one- and two-phonon states have been identified
N.Pietrella et al, Phys. Rev. Lett. 83 (1999) 1303
N.Pietrella et al, Phys. Rev. Lett. 84 (2000) 3775
C.Fransen et al, Phys. Lett. B 508 (2001) 219
C.Fransen et al, Phys. Rev. C 67 (2003) 024307
- Structure of basic phonons
- Purity of two-phonon states
- Study of 2^+ states with (e,e') and (p,p')
 - isoscalar / isovector decomposition
 - sensitive to one-phonon components of the wave function

- High resolution required to resolve all 2^+ states below 4 MeV
- Lateral dispersion matching techniques

- (e,e'):
S-DALINAC, TU Darmstadt

$$E_e = 70 \text{ MeV}$$

$$\Theta = 93^\circ - 165^\circ$$

$$\Delta E = 30 \text{ keV (FWHM)}$$

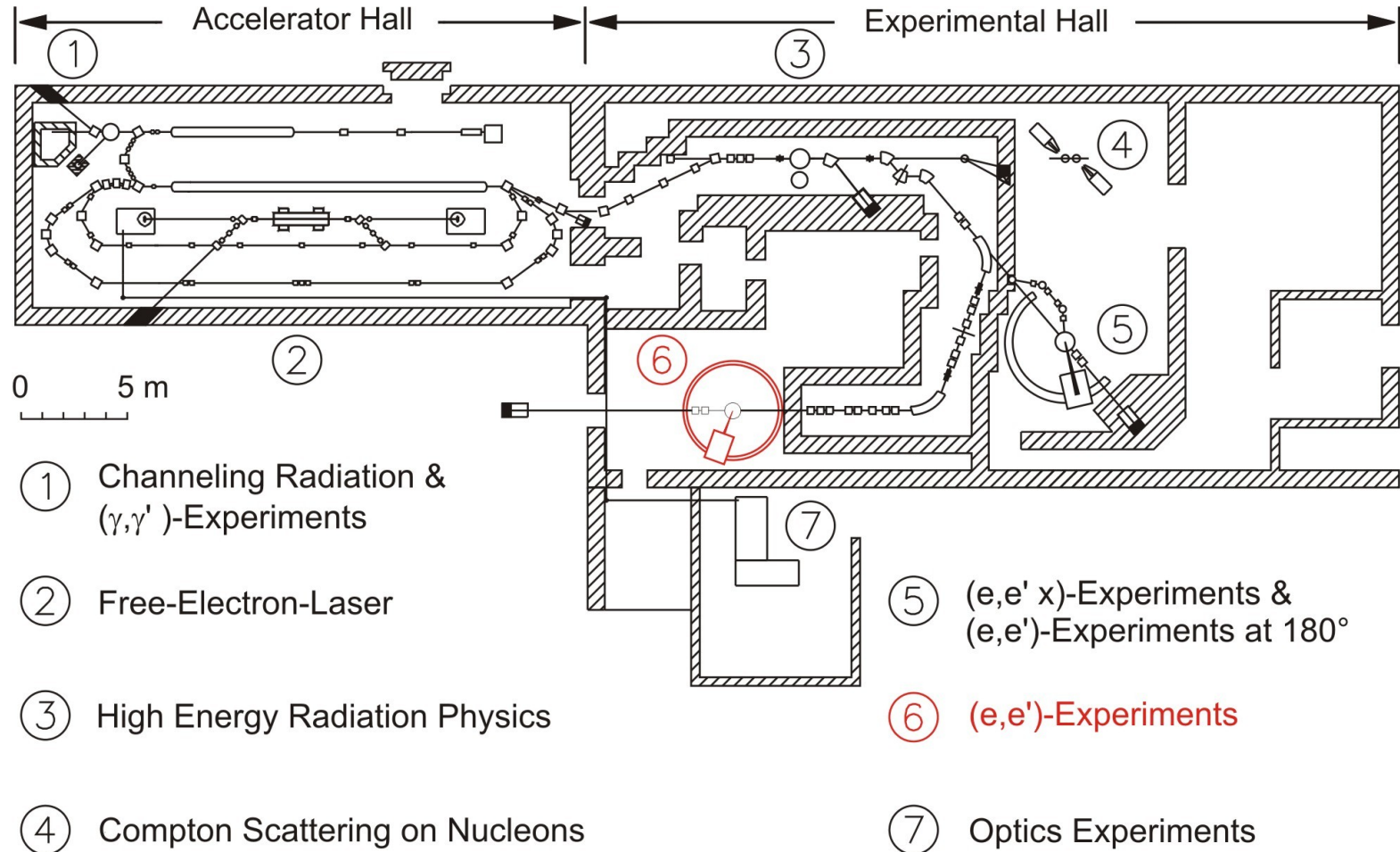
- (p,p'):
SSC, iThemba LABS

$$E_p = 200 \text{ MeV}$$

$$\Theta = 7^\circ - 26^\circ$$

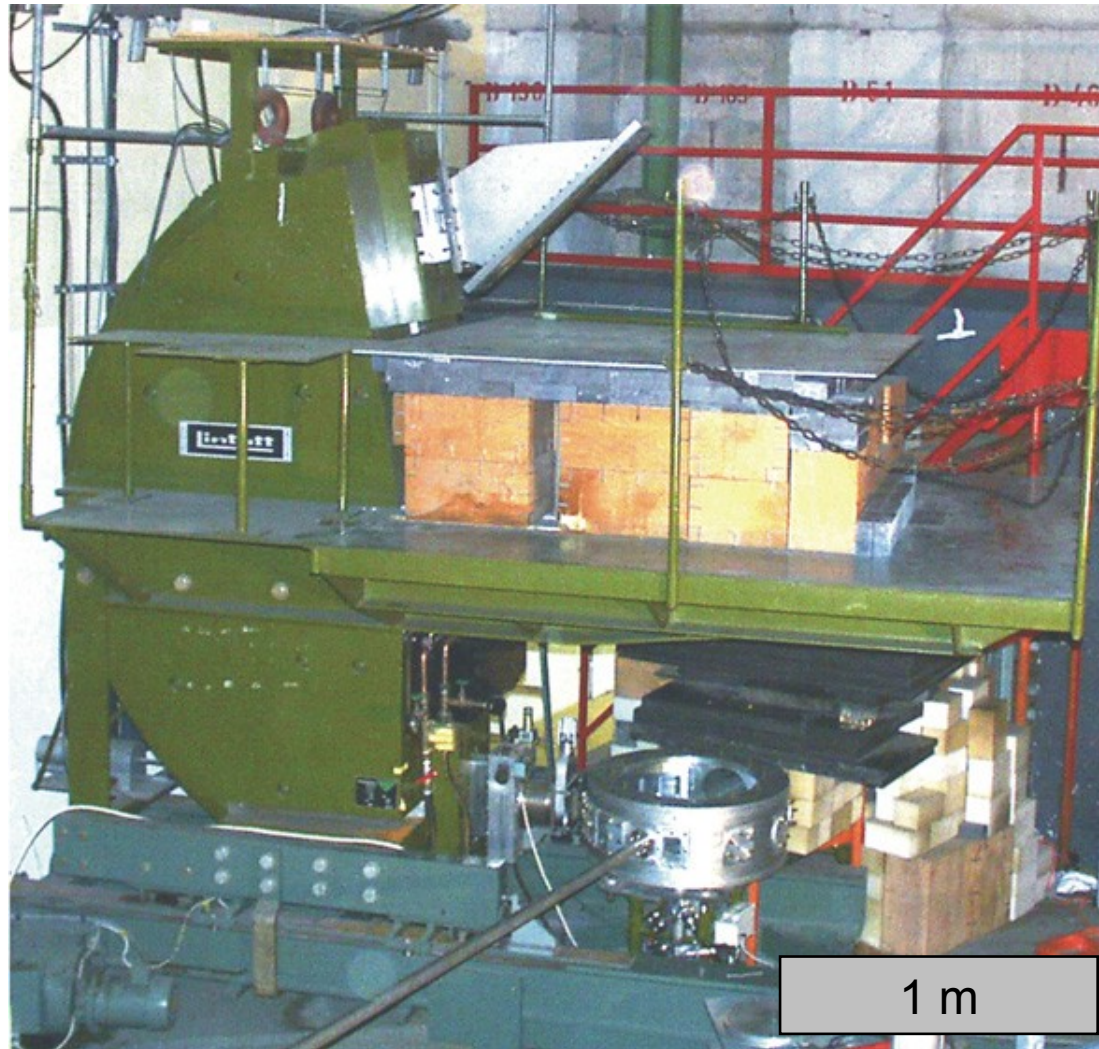
$$\Delta E = 35 \text{ keV (FWHM)}$$

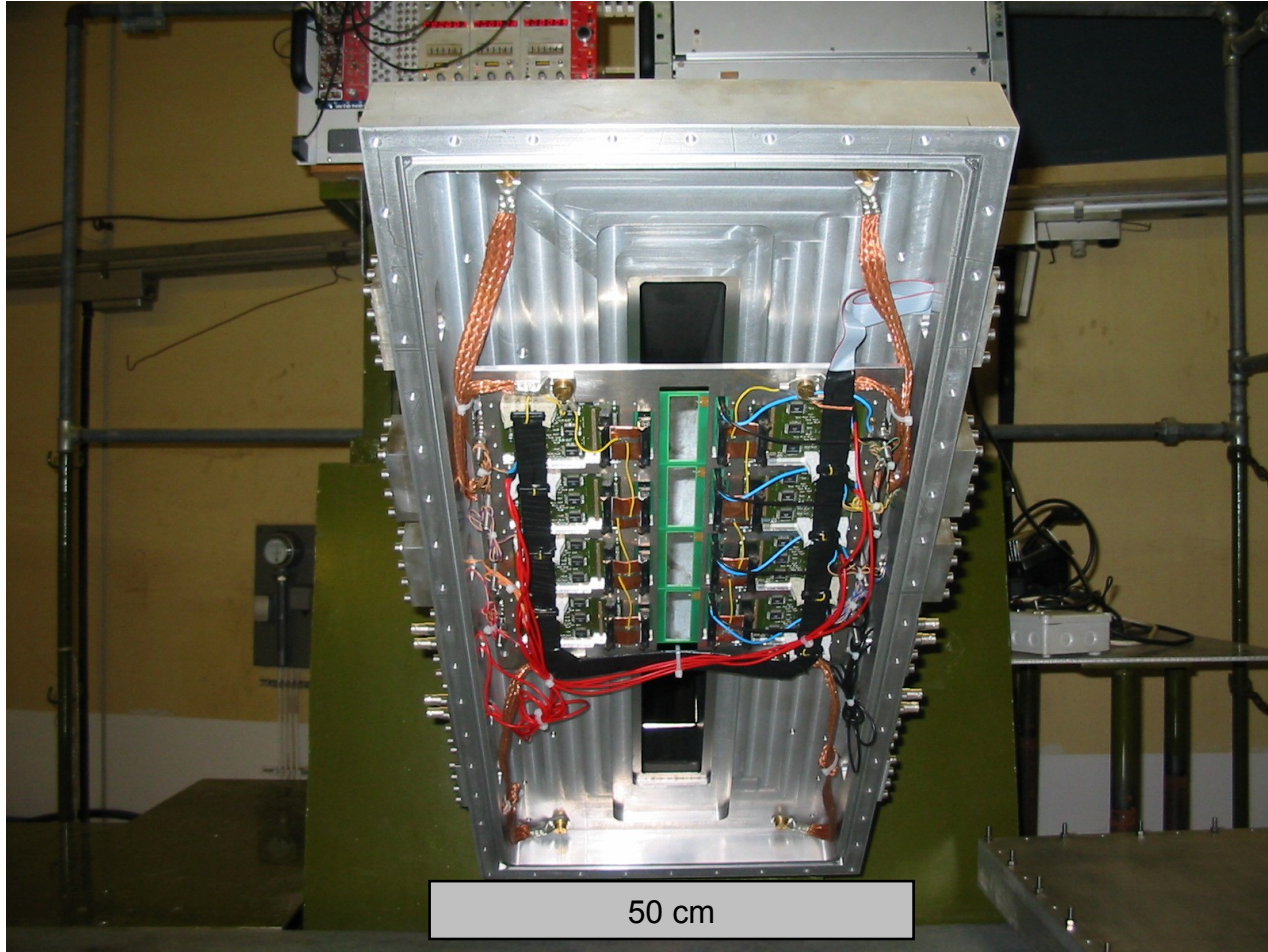
S-DALINAC and its Experimental Facilities





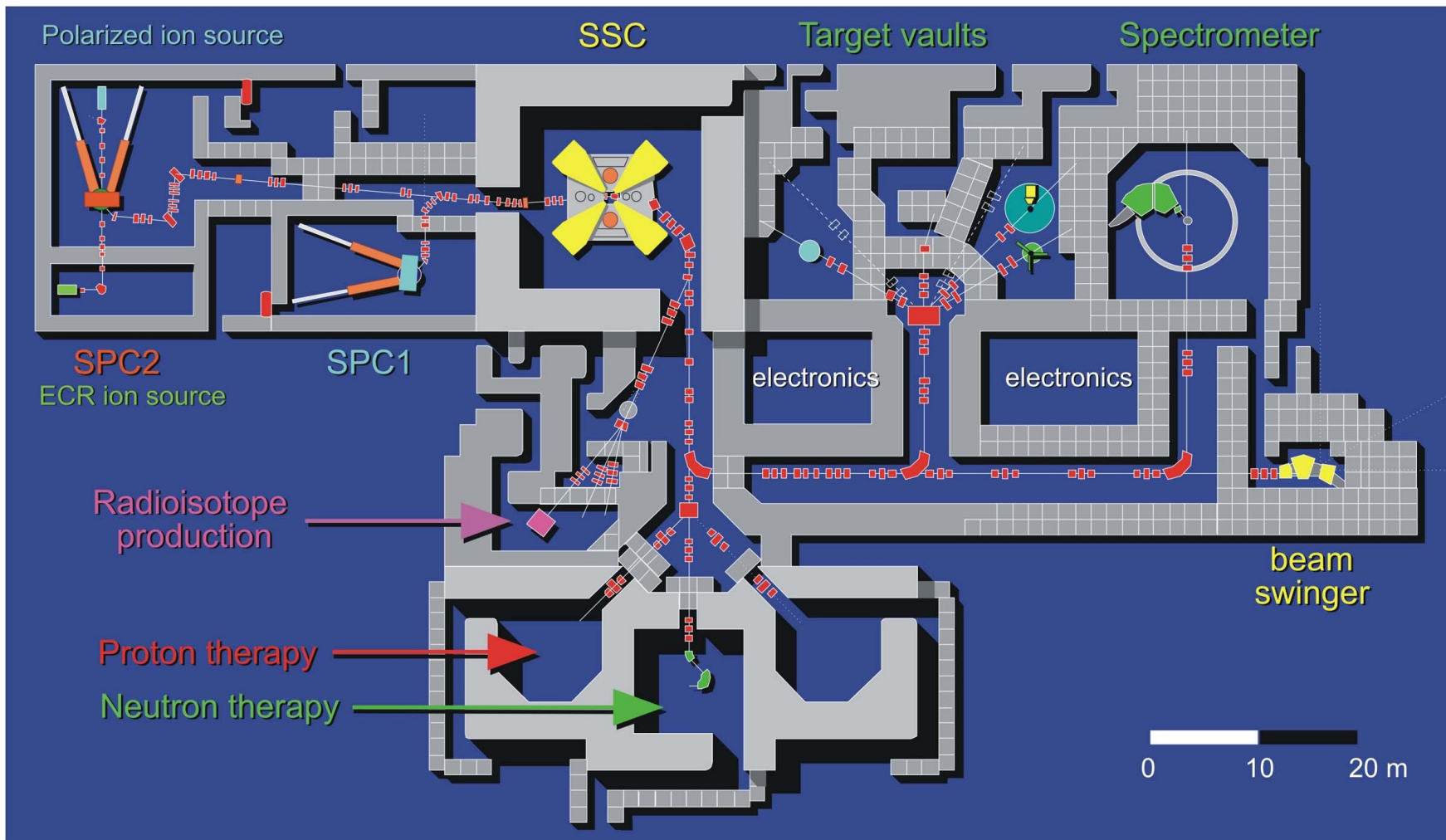
LINTOTT- Spectrometer



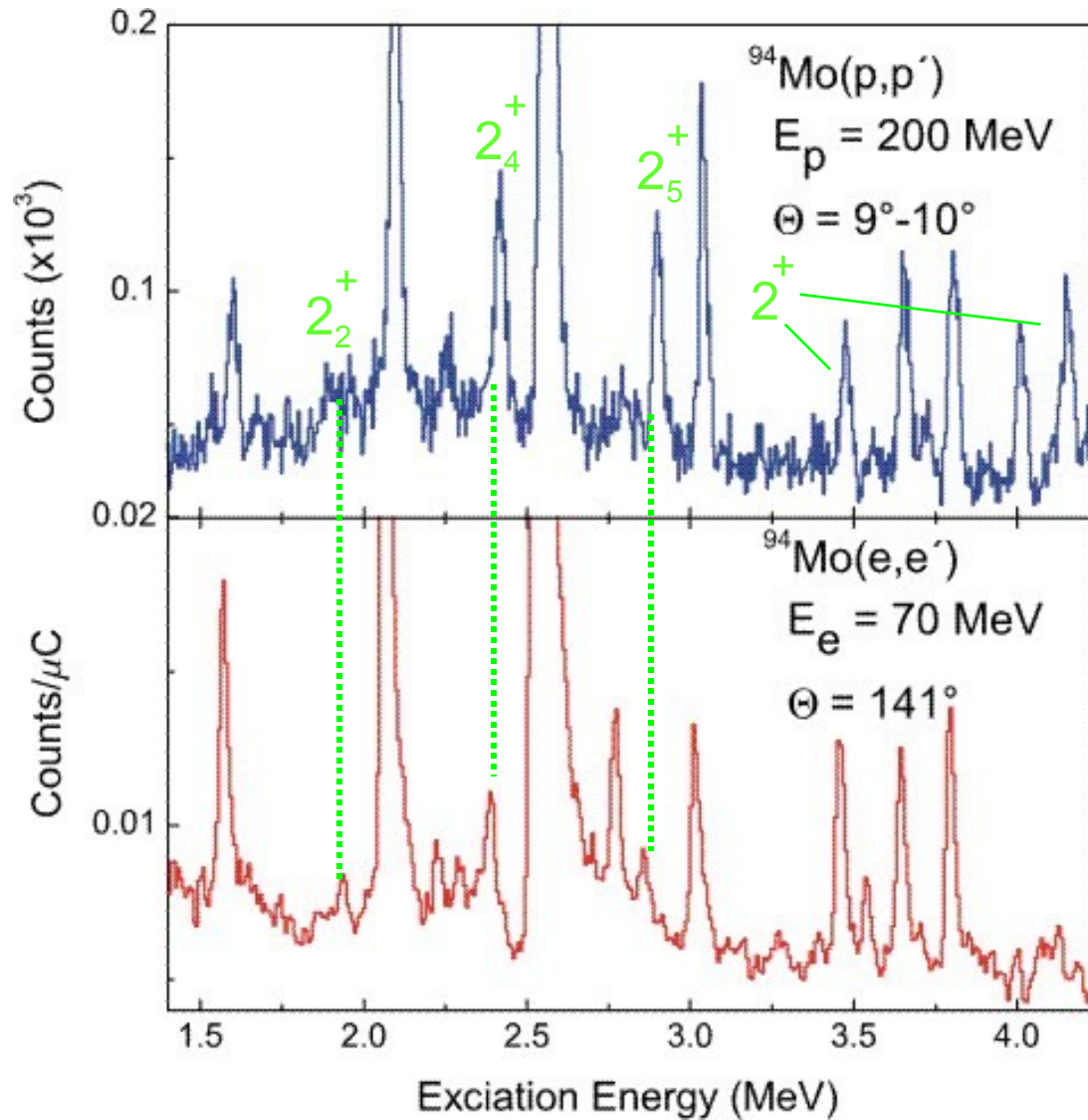




Separated-Sector Cyclotron Facility



Measured Spectra

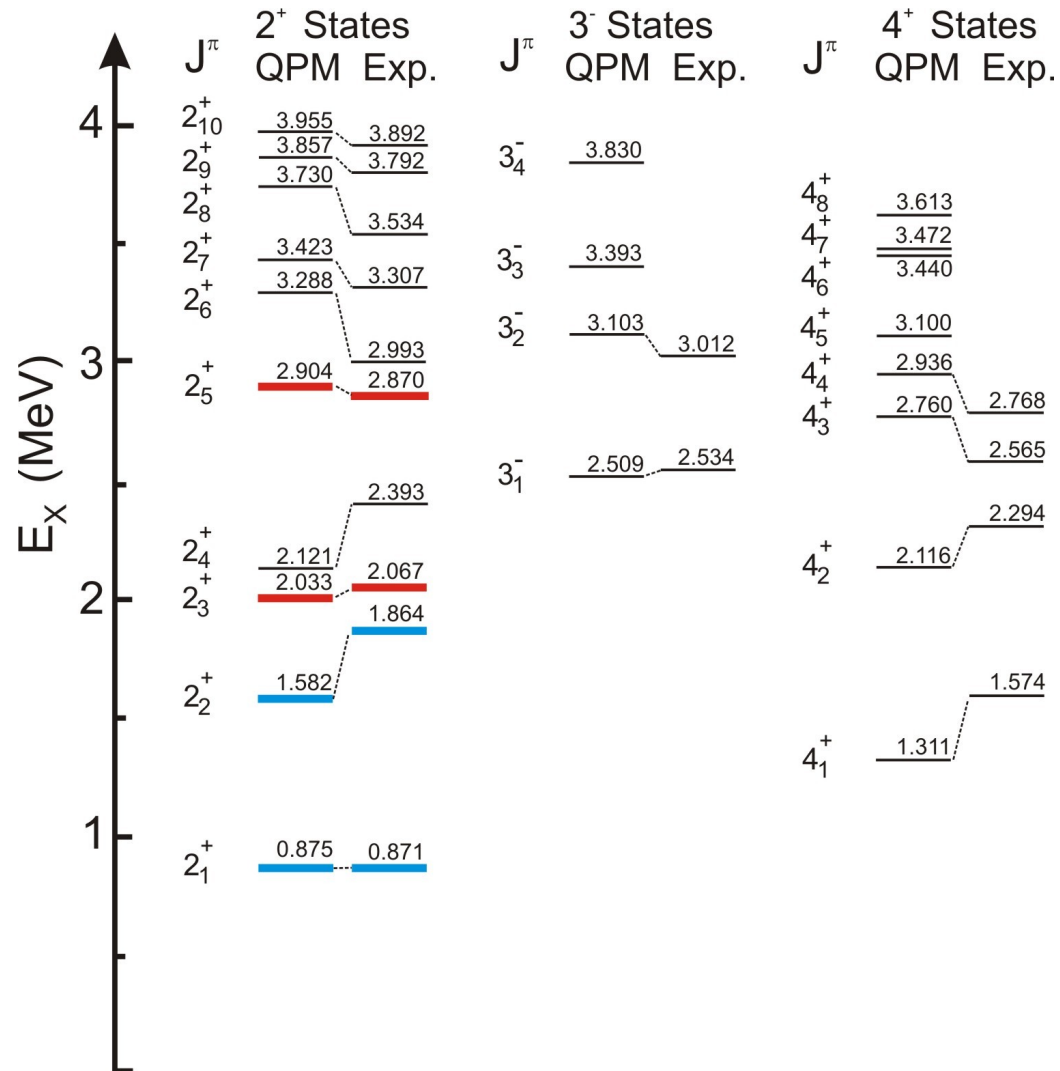


Wave functions:

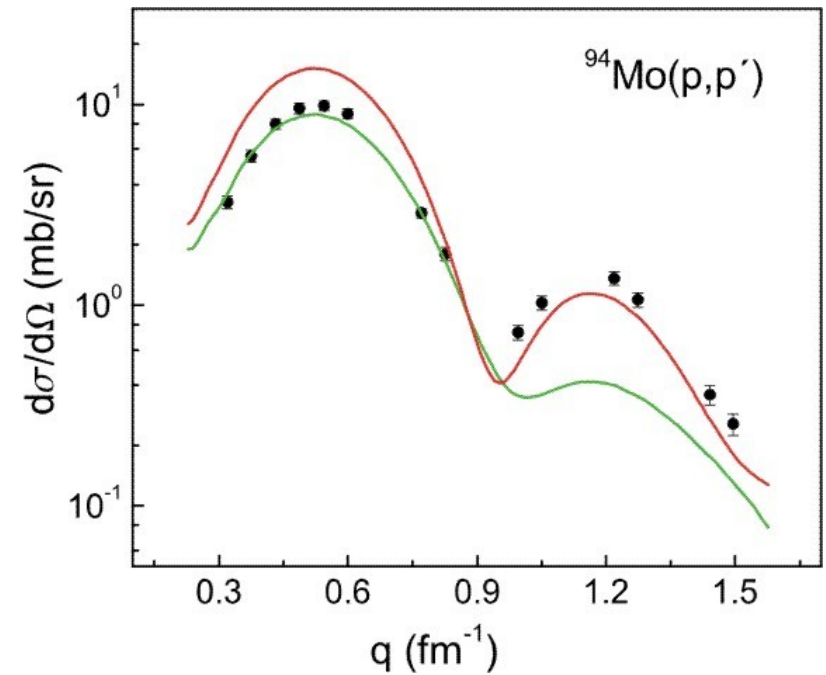
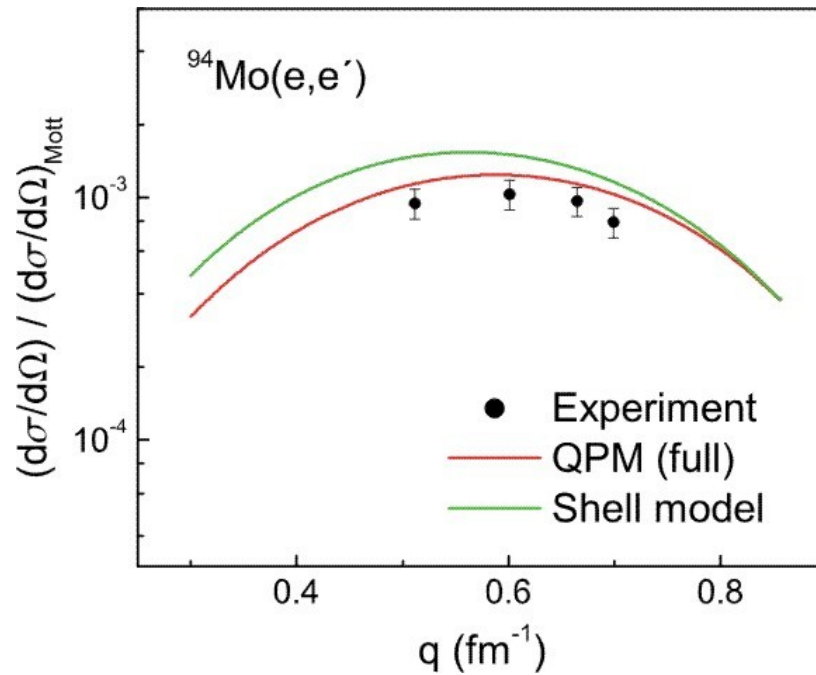
- Quasi-Particle Phonon Model (QPM)
 - pure one- and two-phonon states
 - full (up to 3 phonons)
- Shell Model
 - ^{88}Sr core
 - Surface Delta Interaction (SDI)
- Cross sections
 - DWBA treatment
 - Effective nucleon-target interaction (Paris, Love-Franey)

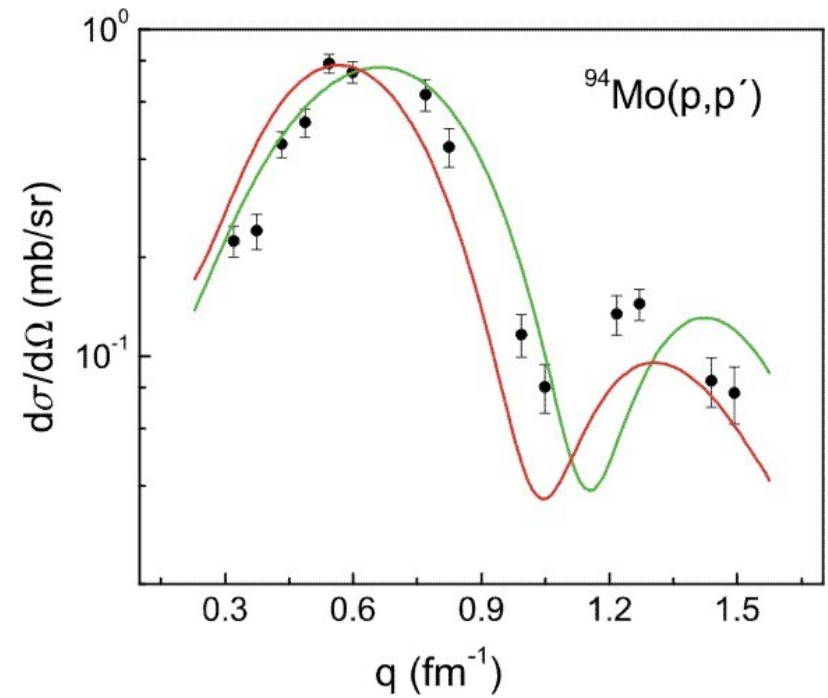
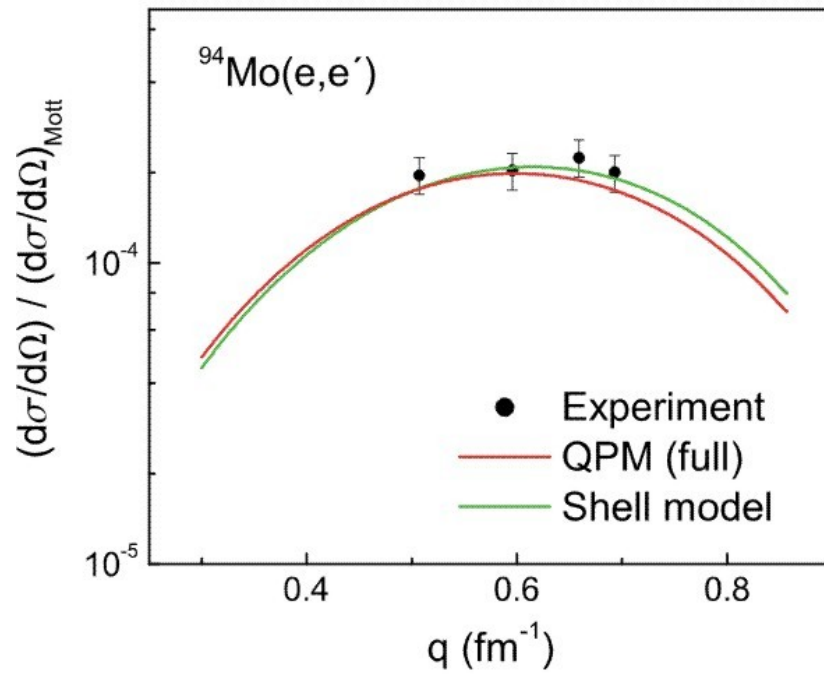


QPM Predictions

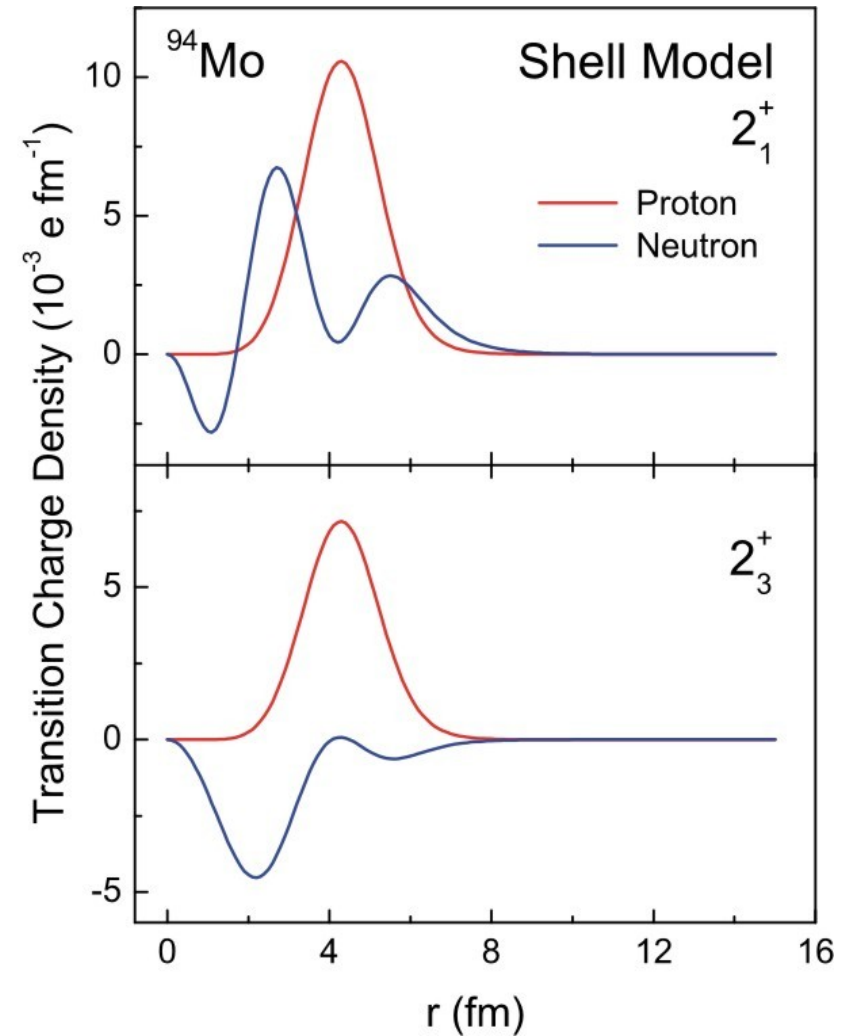
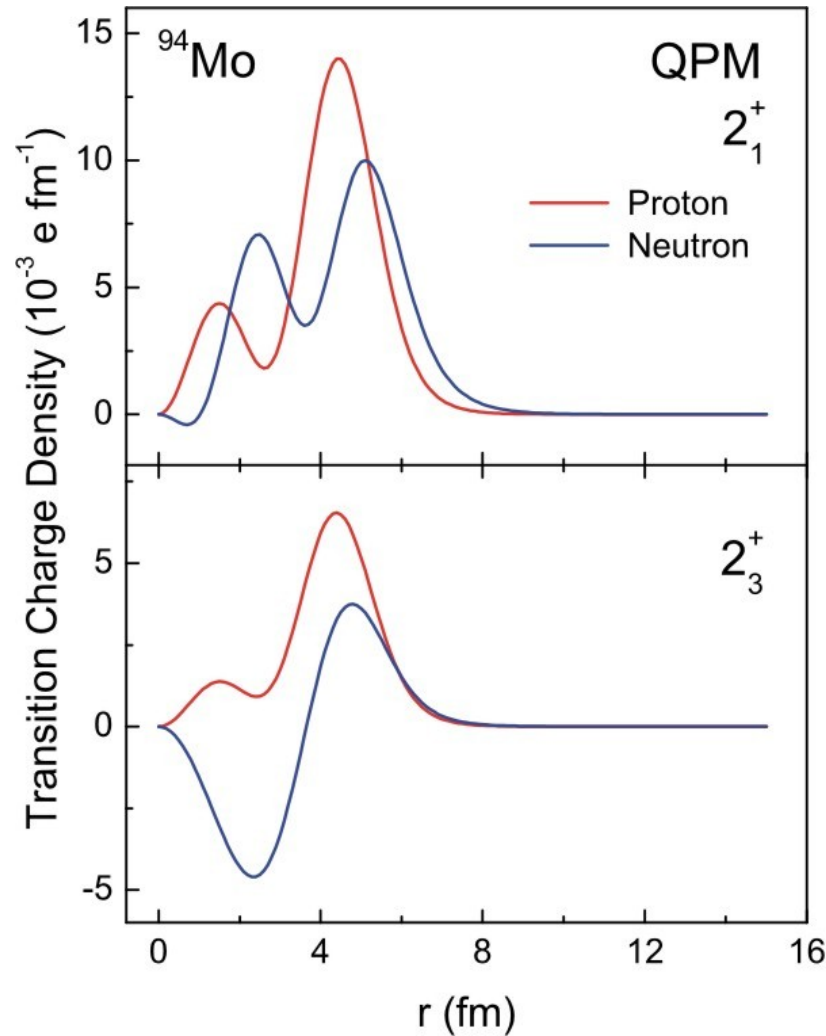


One-Phonon Symmetric State: $E_x = 0.871$ MeV

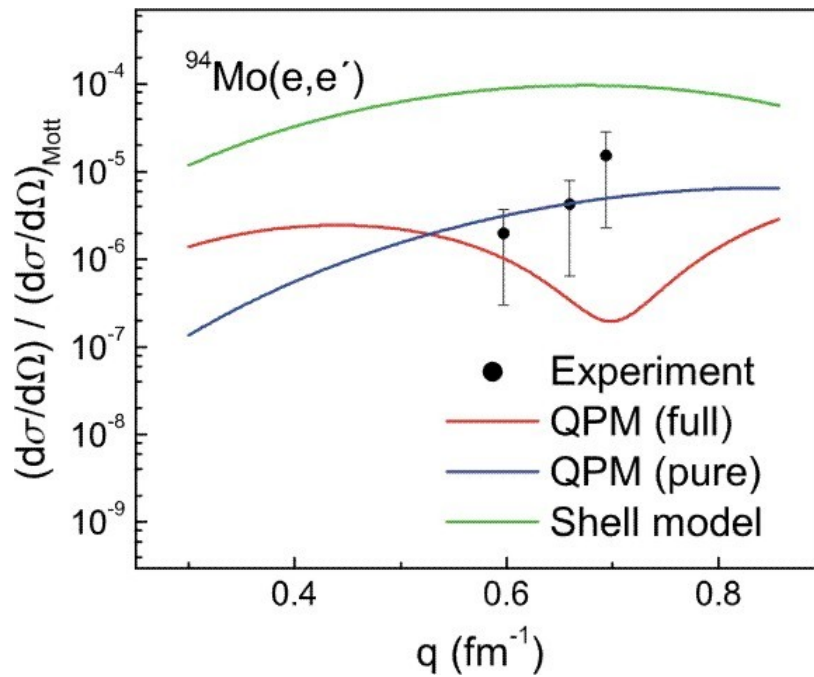




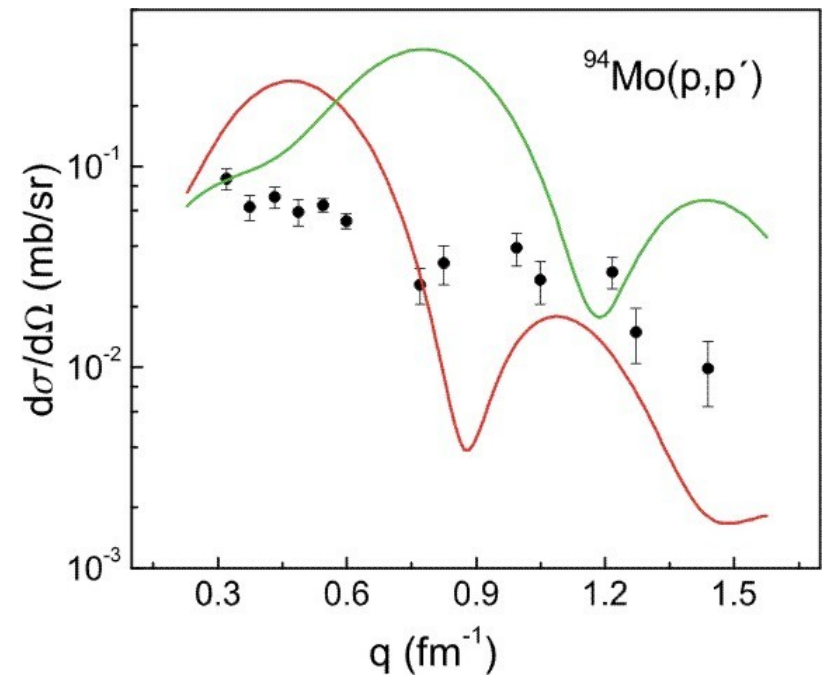
Radial Transition Charge Densities



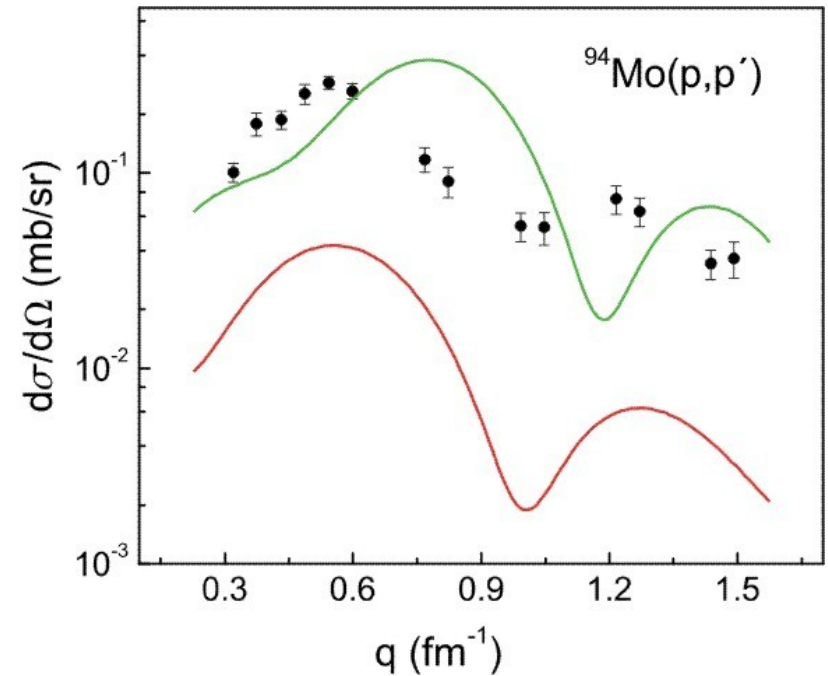
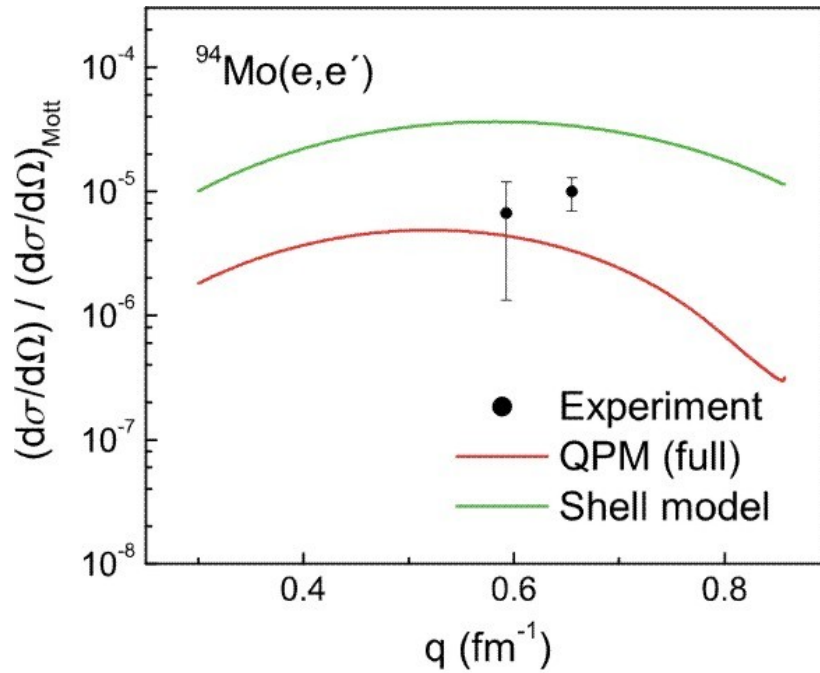
Two-Phonon Symmetric State: $E_x = 1.864$ MeV



- pure two-phonon state



- two-step contributions?

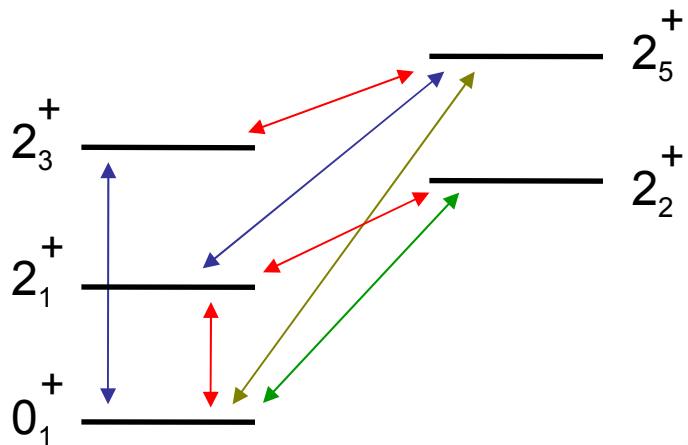


- 5 – 10 % one-phonon admixture

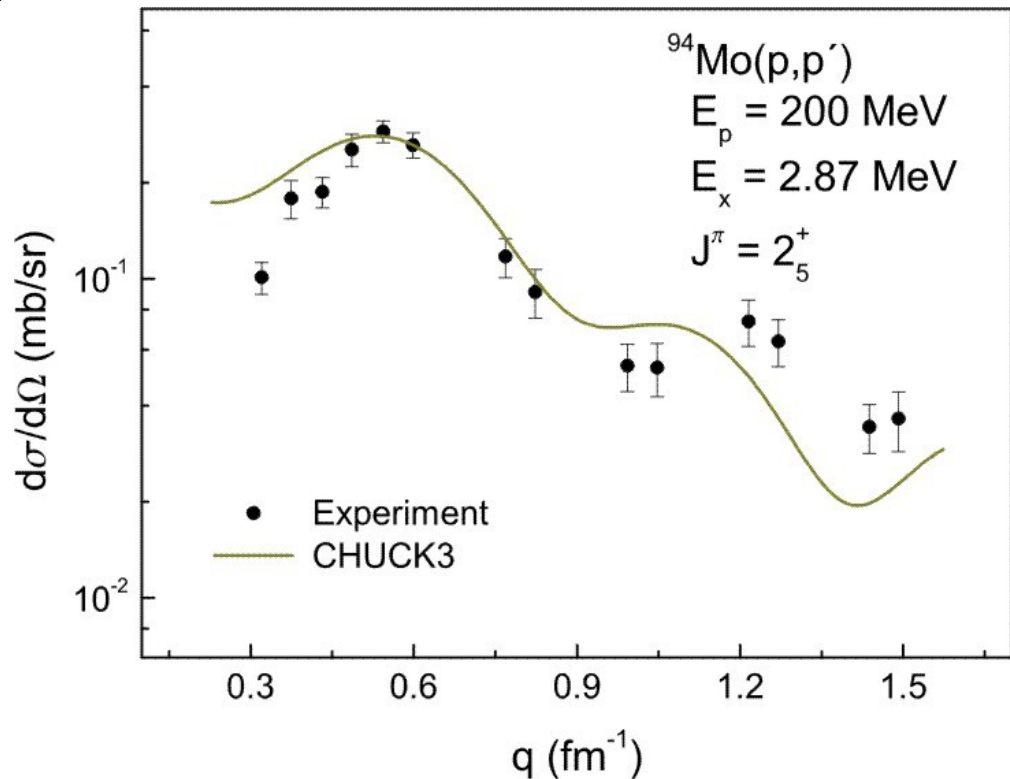
- two-step contributions?



Coupled-Channel Analysis



- $\beta = 1.23$
- $\beta = 0.35$
- $\beta = 0.0$
- $\beta = 0.2$



- Admixed proton-symmetric state confirmed

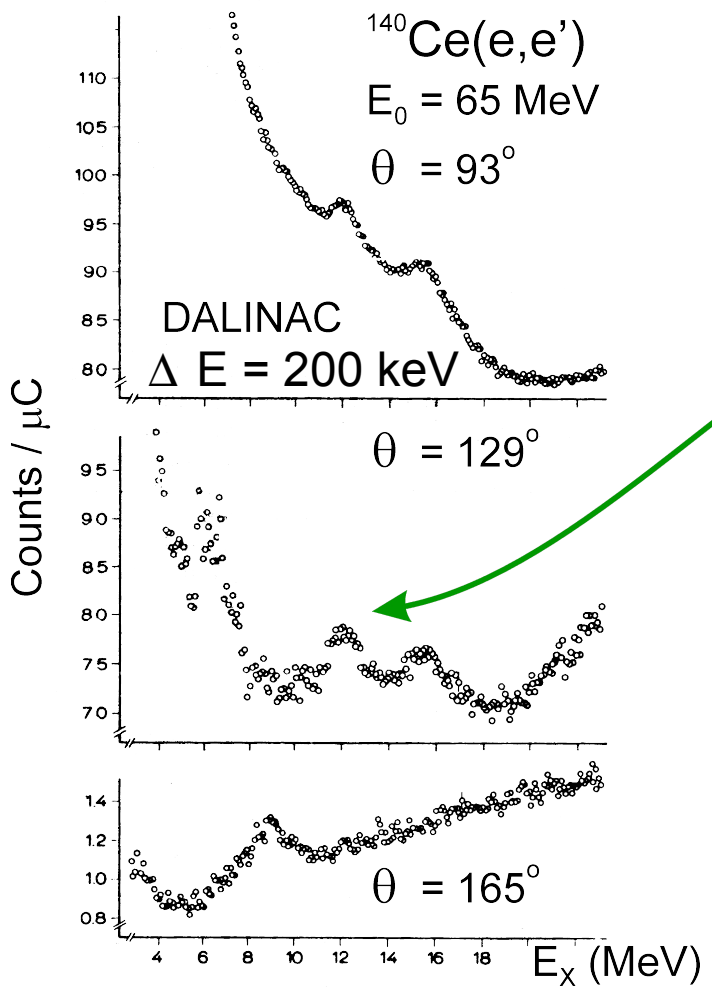
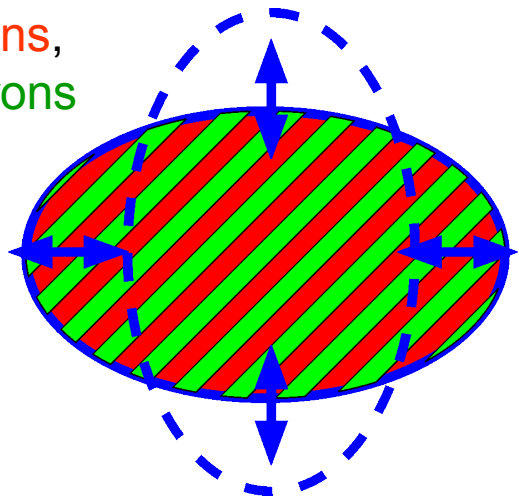
- Study of one- and two-phonon 2^+ states in ^{94}Mo with high-resolution (e,e') and (p,p') experiments
- Combined analysis with QPM reveals
 - symmetric and mixed-symmetric character of one-phonon states
 - two-phonon symmetric state extremely pure
 - about 25% admixtures in the two-phonon mixed-symmetric wave function (mostly 3-phonon)
 - quantitatively consistent results after inclusion of two-step processes in (p,p')
- Shell model description moderate to poor
 - limited model space

- Introduction: Damping of giant resonances
- Evidence for fine structure of giant resonances
- Wavelet analysis and characteristic scales
- Dominant damping mechanisms
- Summary and outlook

Damping of GR: Isoscalar Quadrupole Mode

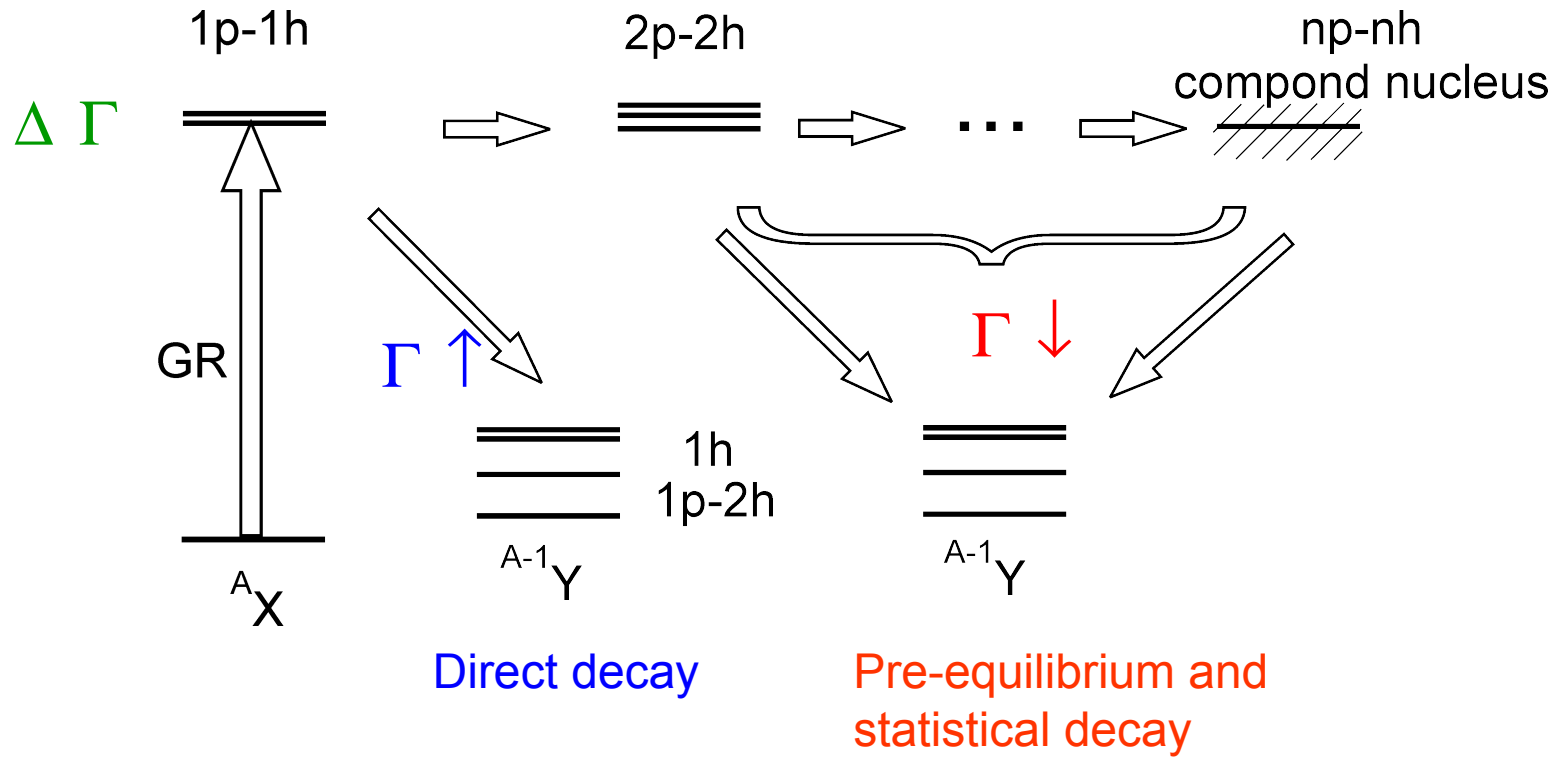
$$\Delta L = 2 \quad \Delta T = 0 \quad \Delta S = 0$$

protons,
neutrons



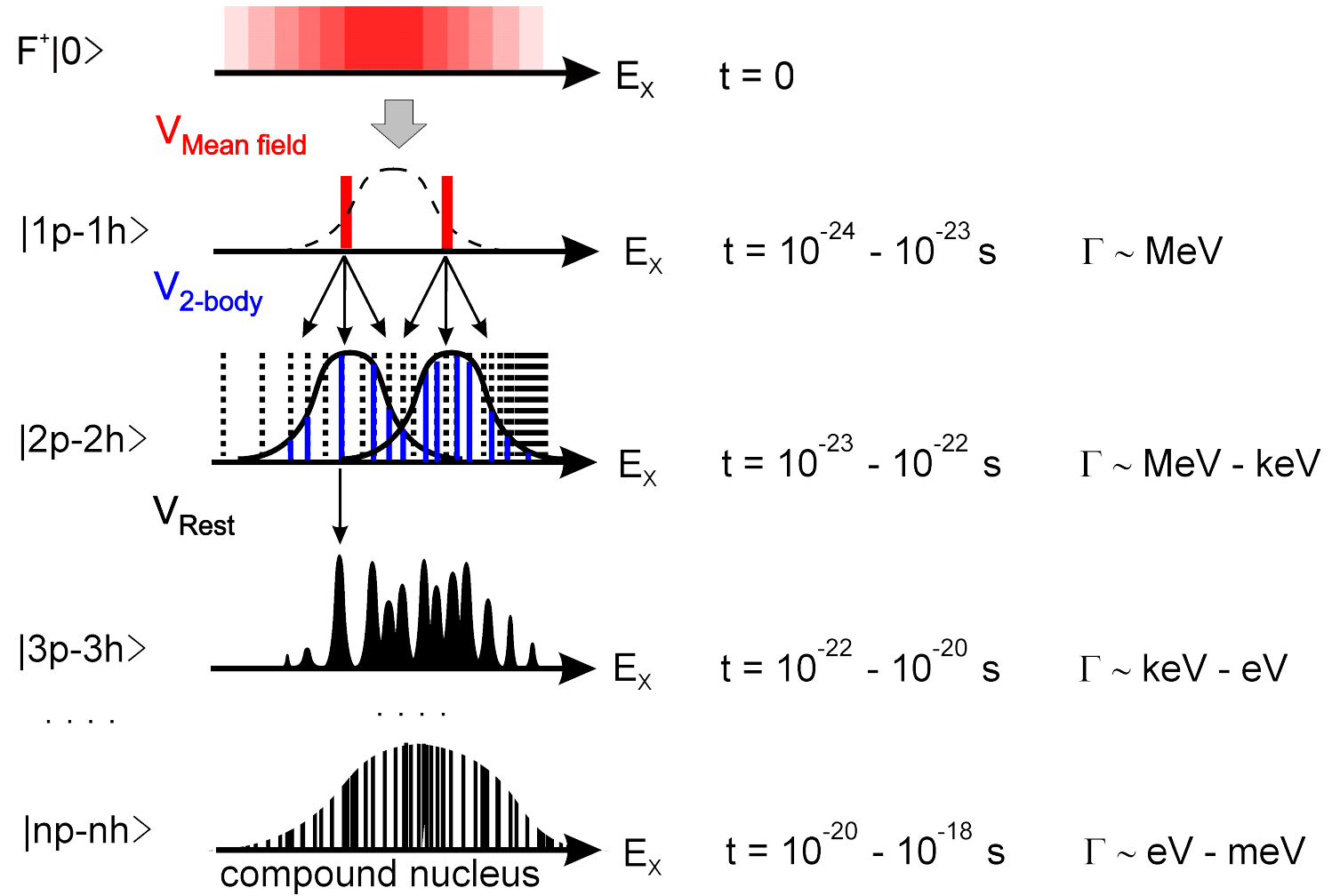
- Pitthan and Walcher (Darmstadt, 1972)
- Centroid energy: $E_c \sim 63 A^{-1/3}$ MeV
- Width
- Damping mechanisms?

Excitation and Decay of Giant Resonances

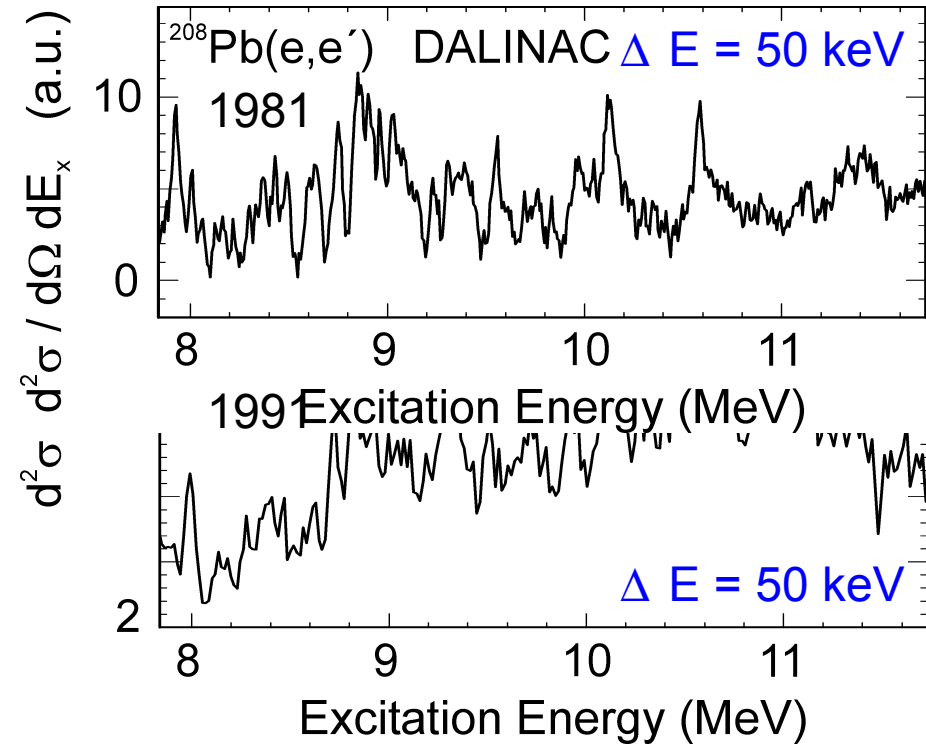
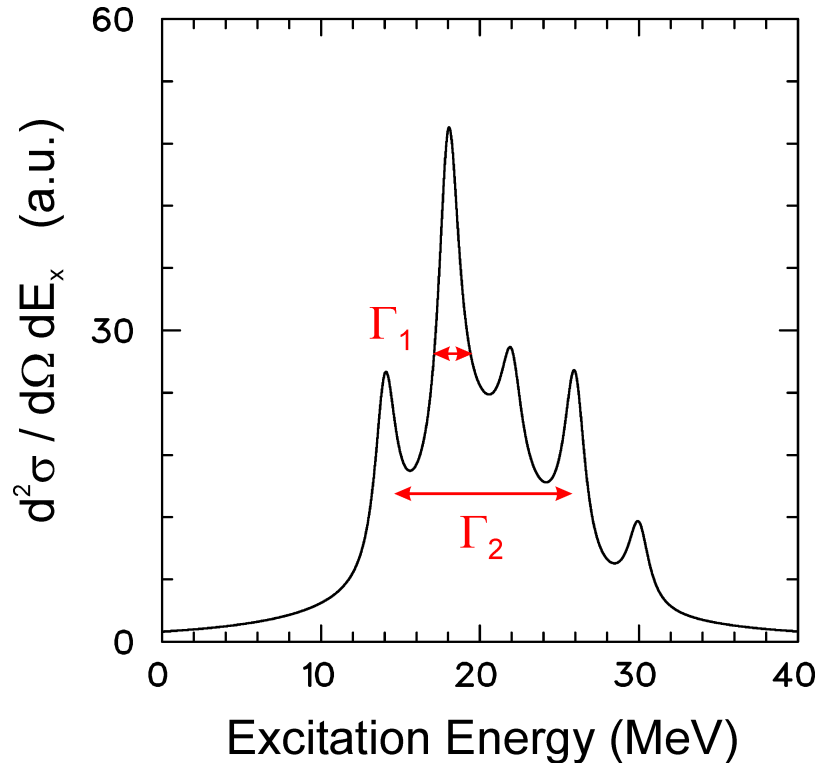


Resonance decay width: $\Gamma = \Delta \Gamma + \Gamma \uparrow + \Gamma \downarrow$

Doorway-State Model



ISGQR in ^{208}Pb



- High resolution is crucial
- Different probes but similar structures

- Global phenomenon?
 - Other nuclei
 - Other resonances
- Methods for characterization of fine structure?
- Goal: Dominant damping mechanisms

Place:

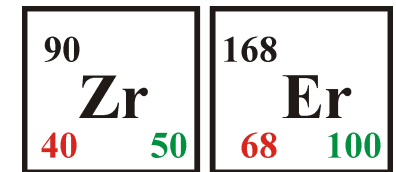
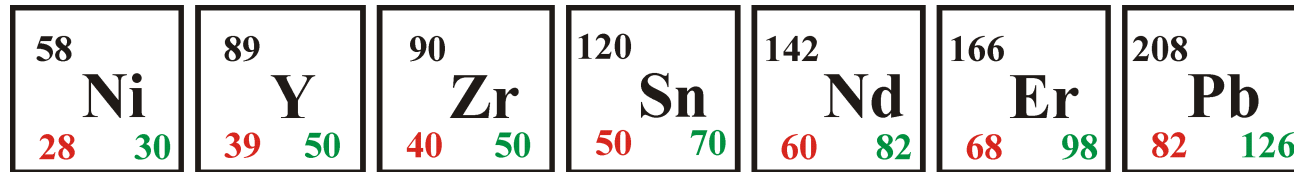
iThemba LABS,
South Africa

RCNP, Osaka

Reaction:

ISGQR from (p,p')

GT from ($^3\text{He},t$)



Beam energy:

200 MeV

140 MeV/u

Scattering angles:

$8^\circ - 10^\circ$
($\Delta L = 2$)

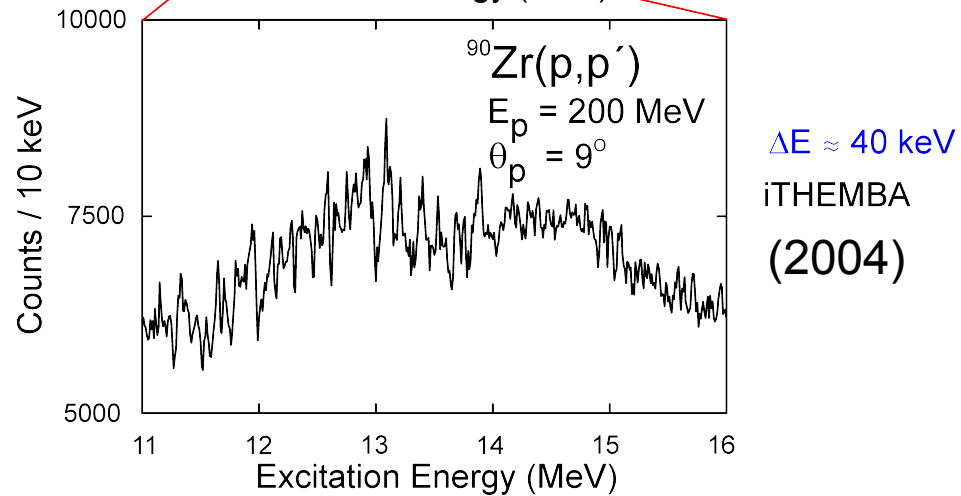
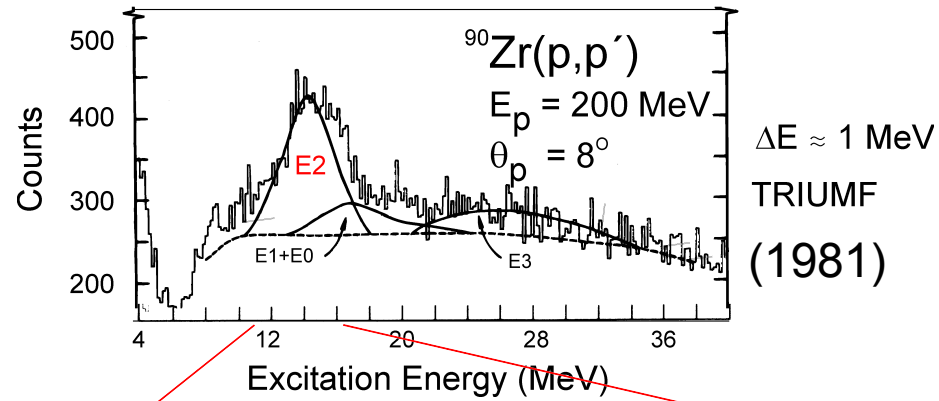
0°
($\Delta L = 0$)

Energy resolution:
(FWHM)

$\Delta E = 35 - 50 \text{ keV}$

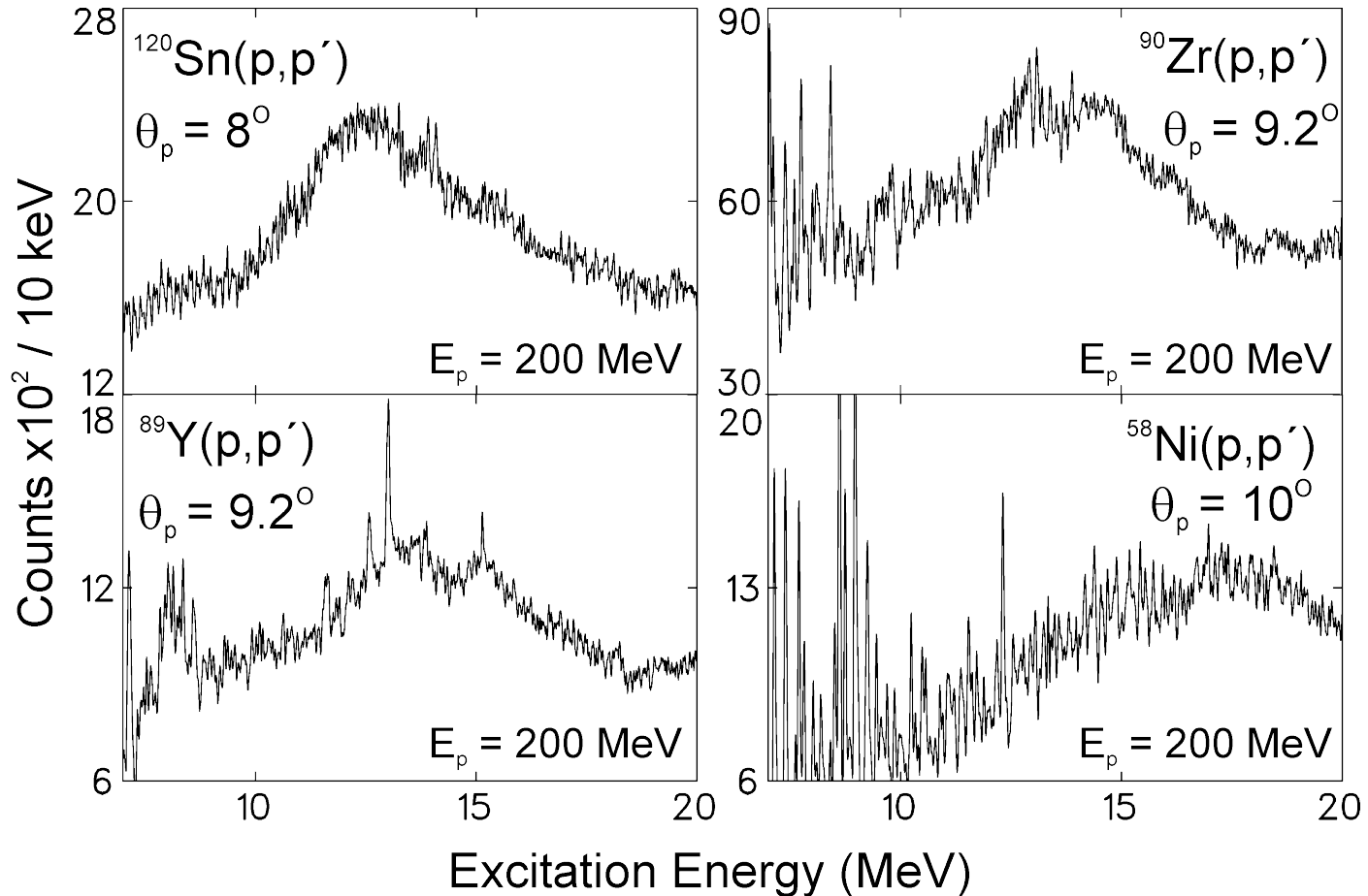
$\Delta E = 50 \text{ keV}$

Fine Structure of the ISGQR



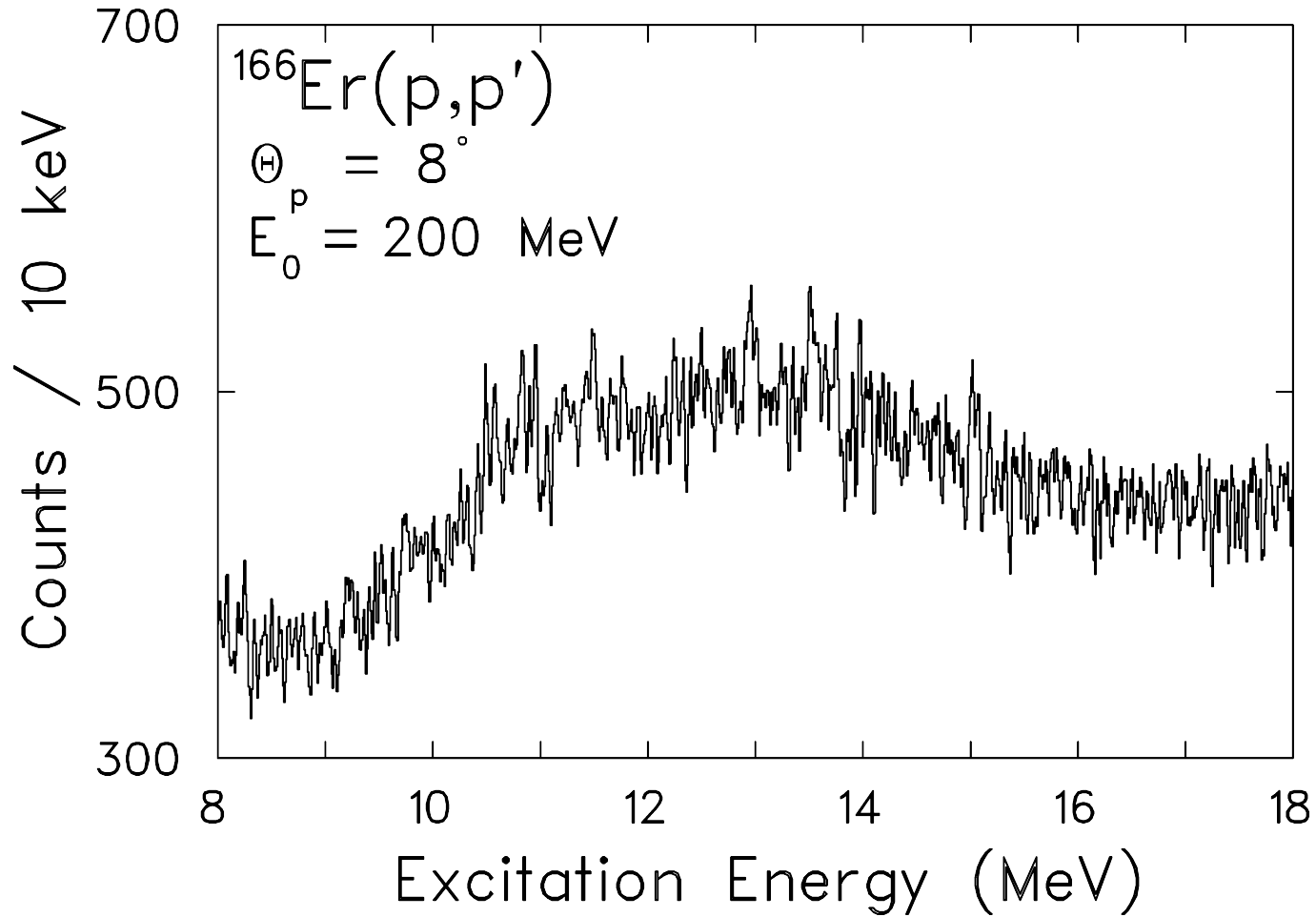
- Not a Lorentzian

Fine Structure of the ISGQR in Other Nuclei



- Fine structure of the ISGQR is global

Fine Structure in Deformed Nuclei?



- Fluctuation analysis using autocorrelation function
- Doorway-state analysis
- Fourier analysis
- Entropy index method
- Local scaling dimension

 **Wavelet transform from signal processing**

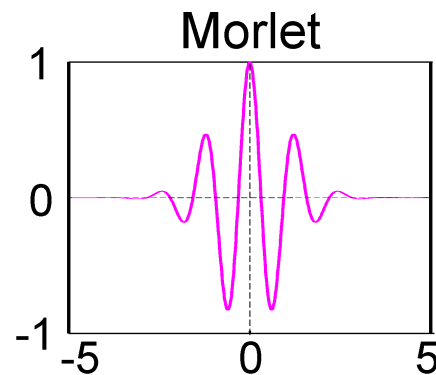
Wavelet coefficients:

$$C(\delta E, E_x) = \frac{1}{\sqrt{\delta E}} \int \sigma(E) \Psi^*\left(\frac{E_x - E}{\delta E}\right) dE$$

↑ ↑ ↑ ↑
 scale position spectrum wavelet

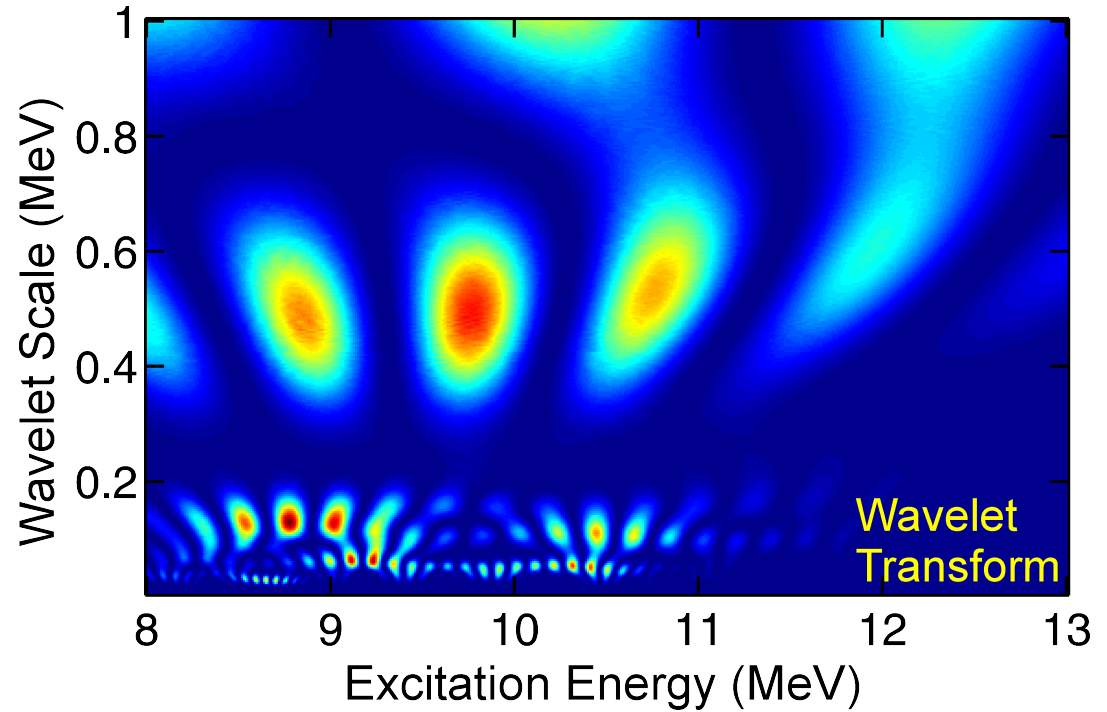
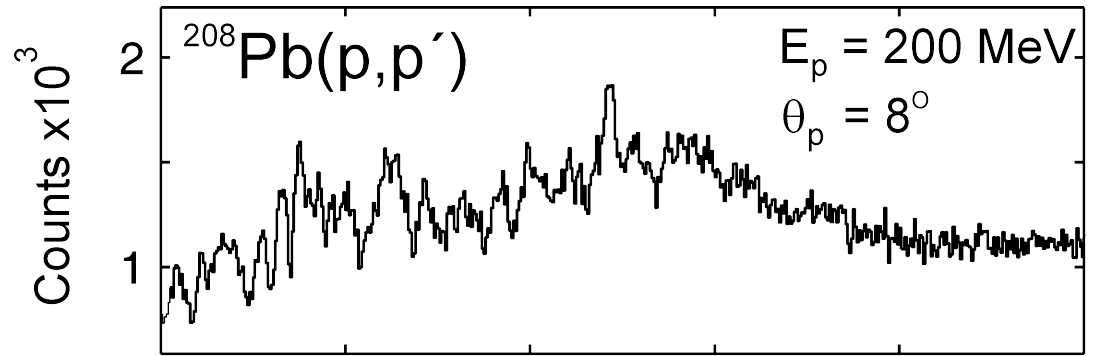
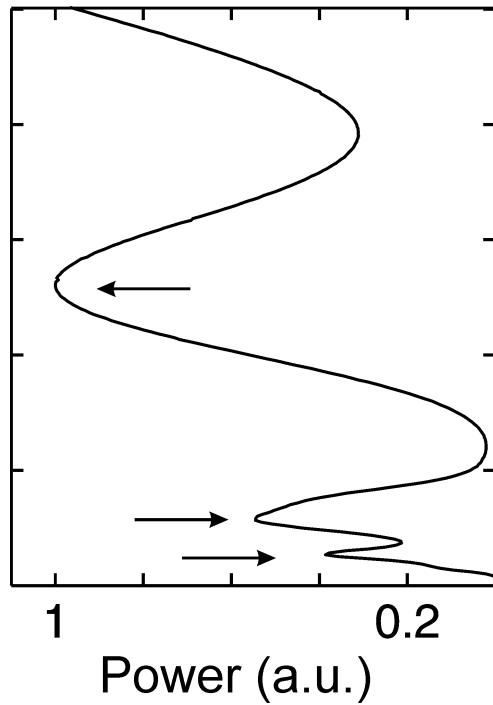
Continuous: $\delta E, E_x$ are varied continuously

$$\int_{-\infty}^{\infty} \Psi^*(x) dx = 0 \quad \text{and} \quad \int_{-\infty}^{\infty} |\Psi^*(x)|^2 dx < \infty$$



$$\Psi(x) = \cos(2\pi\omega x) e^{-x^2/2}$$

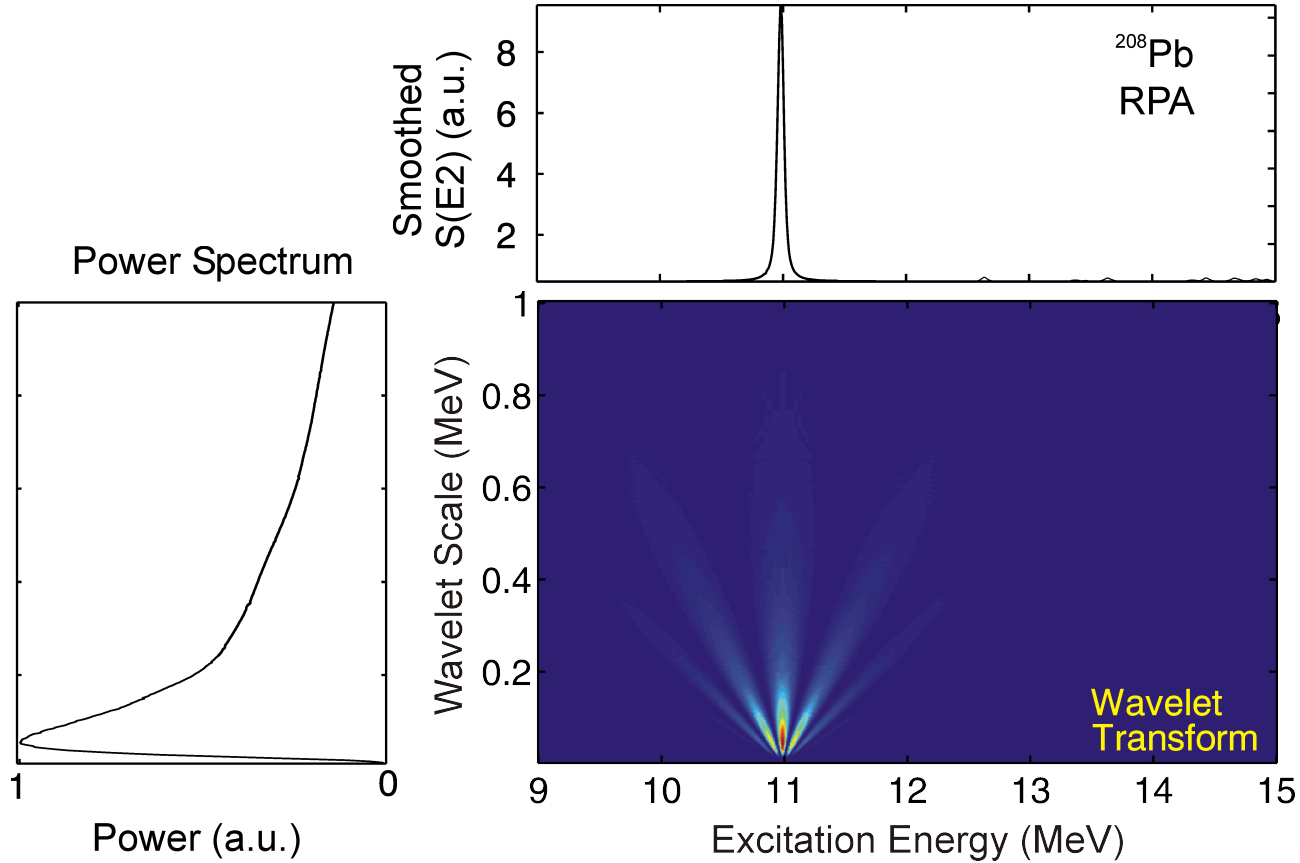
Application: ISGQR in $^{208}\text{Pb}(p,p')$



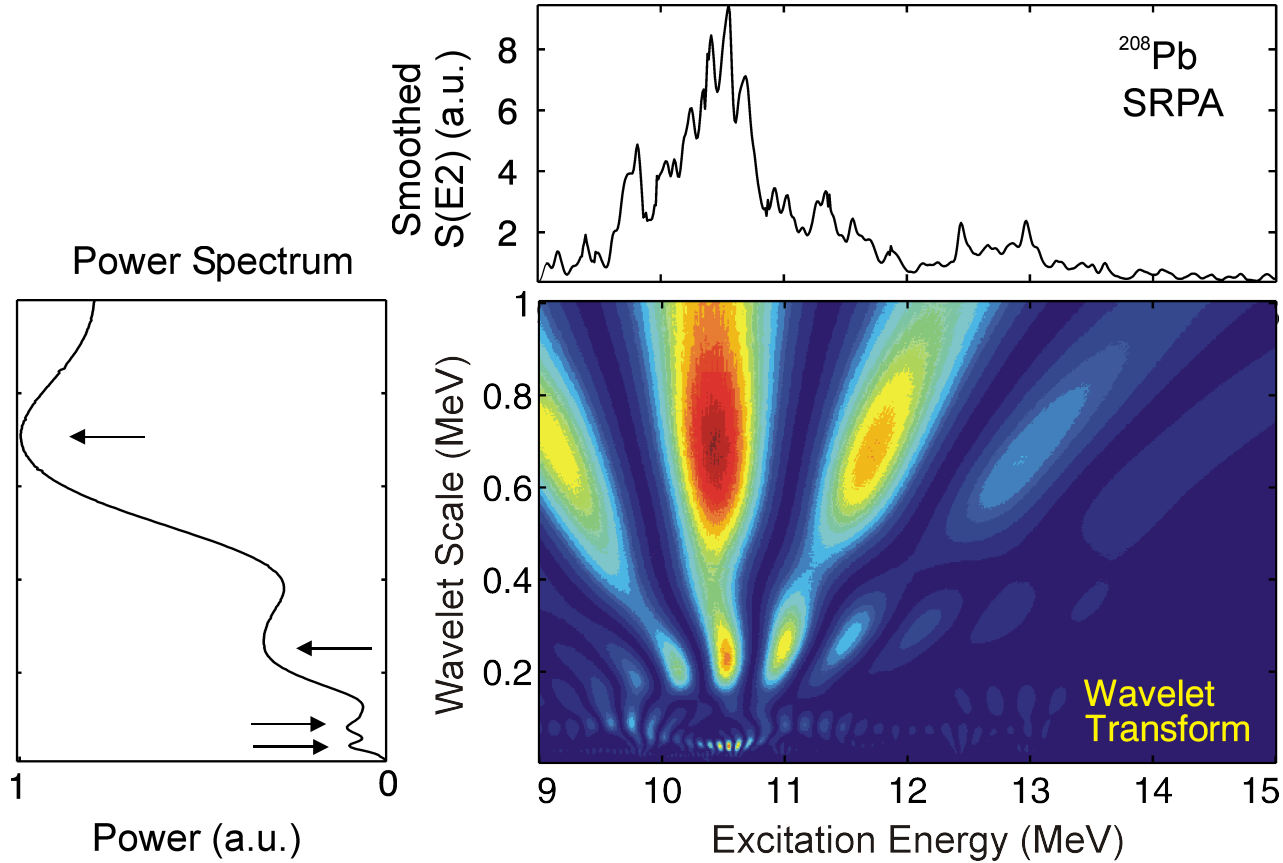
Summary of Scales

		Scales (keV)					
		I	II			III	
ISGQR	^{58}Ni	130	360	580	850	2800	4700
	^{89}Y	120	540	830		3100	
	^{90}Zr	70	540			3100	
	^{120}Sn	80	220	330	470	3200	
	^{142}Nd	130	420			1200	3200
	^{208}Pb	110	500			1500	2600
	^{166}Er	150	250	880		2260	3260
GTR	^{90}Nb	80	300	950		2500	

- Three classes of scales
- **Class I** scales appear in all nuclei
- **Class II** scales change with mass number
- **Class III** scales gross structure (e.g. width)

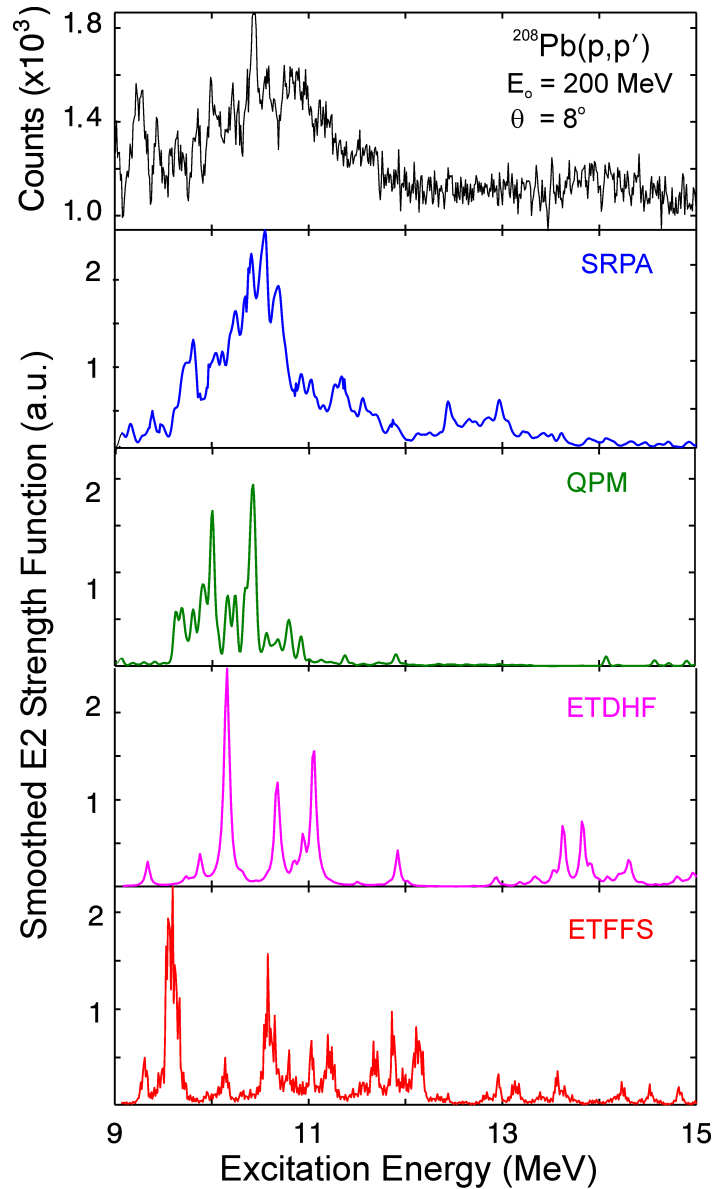


- No scales from 1p-1h states



- Coupling to 2p-2h generates fine structure and scales

Microscopic Models: Case of ^{208}Pb



Wambach et al. (2000)

Ponomarev (2003)

Lacroix et al. (2001)

Kamerdziev et al. (1997)

Experiment vs. Model Predictions

	I	II	III
Exp / keV	110	550	1500 2600
Models / keV			
SRPA	80	250 800	2100
QPM	110	770	1400
ETDHF	120	230	1000
ETFFS	130	310 570	2500

- Three classes of scales as in experiment
- Strong variations of **class II** and **class III** scales

Two types of dissipation mechanisms:

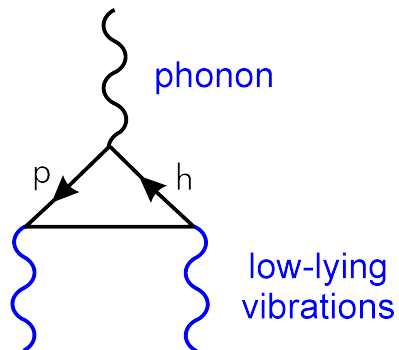
collective damping



low-lying surface vibrations



$1p-1h \otimes \text{phonon}$



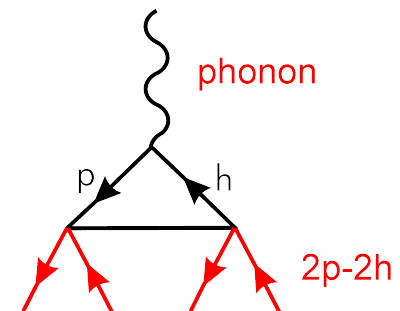
non-collective damping

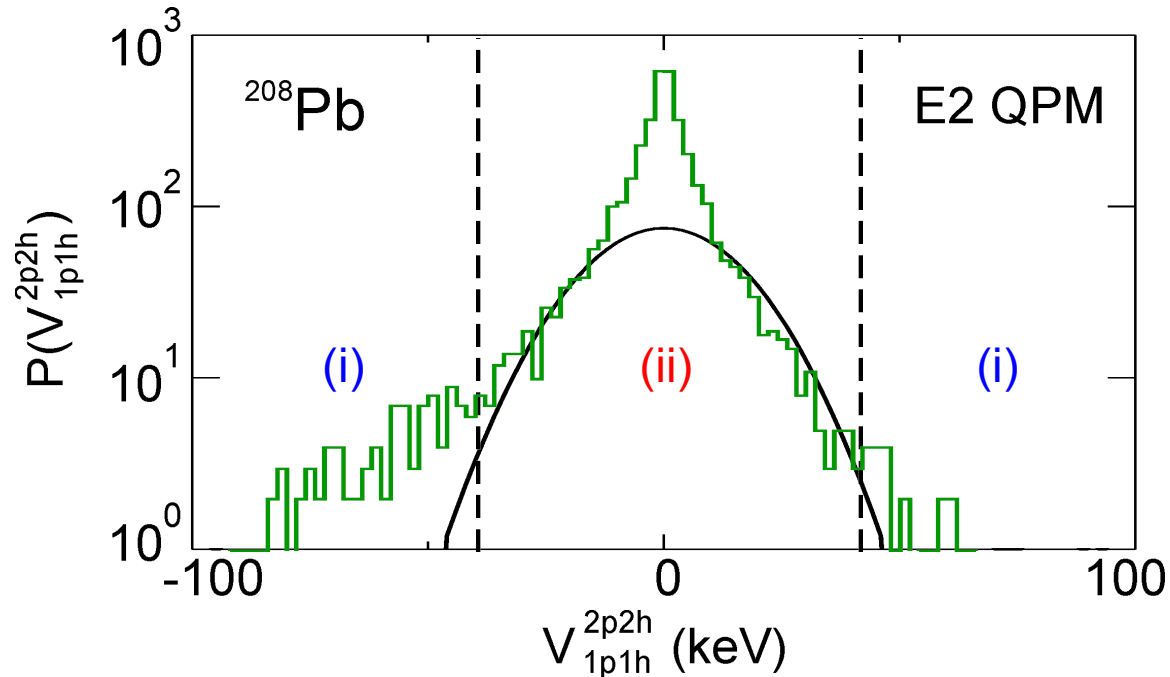


background states



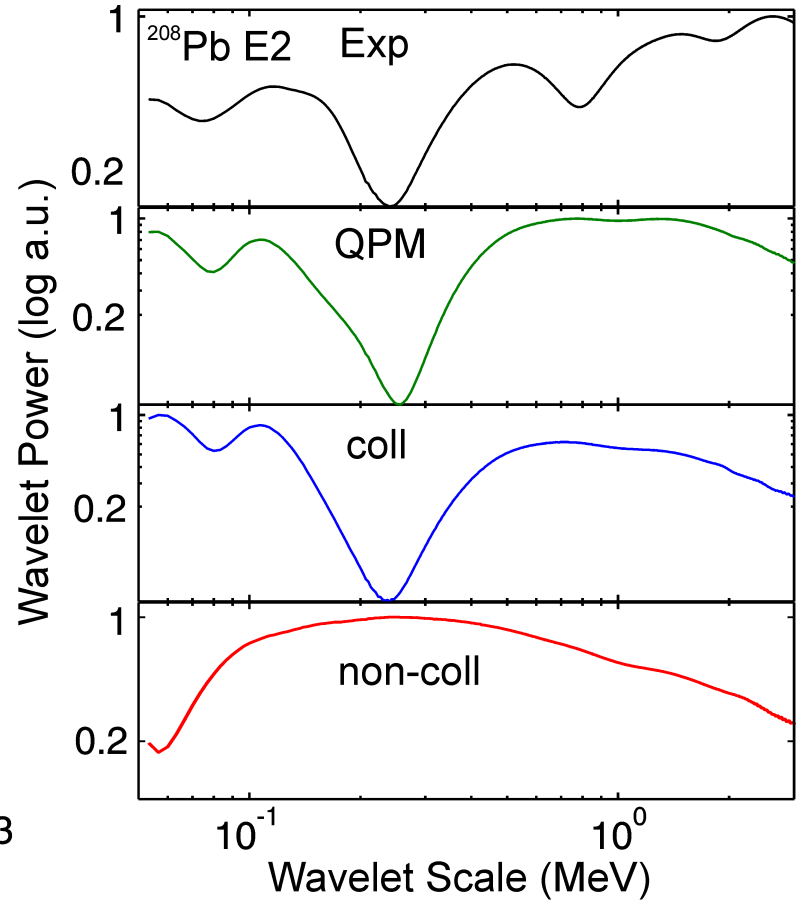
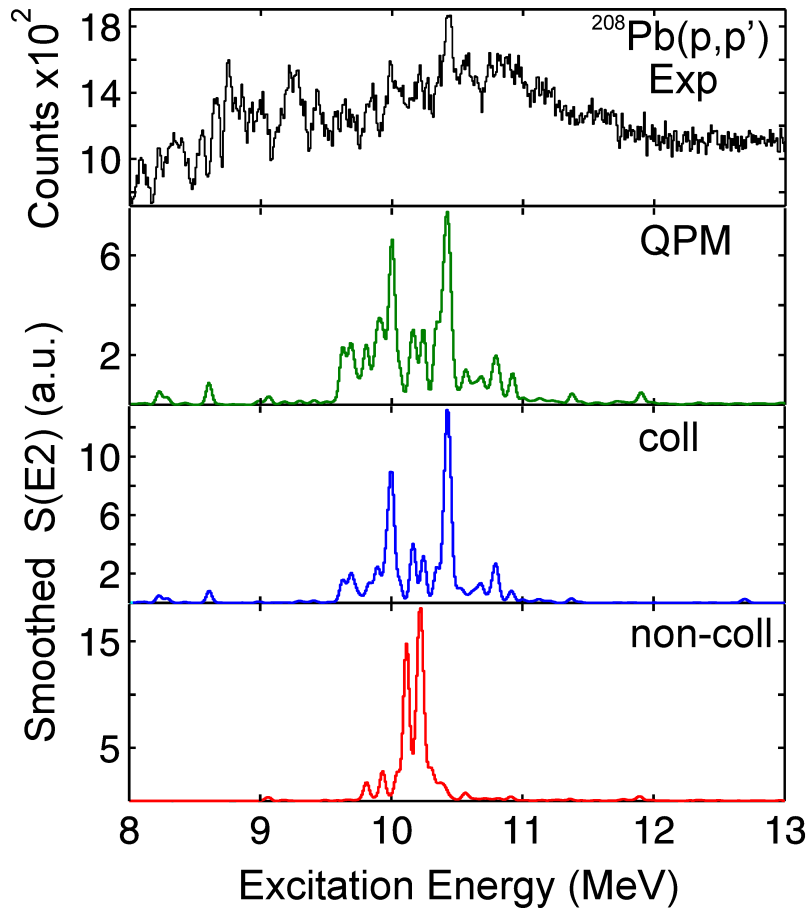
coupling to $2p-2h$ states





- RMT: Gaussian distribution for $\langle 1p1h | V_{1p1h}^{2p2h} | 2p2h \rangle$
- QPM: deviations at large and at small m.e.
- Large m.e. define the **collective damping** mechanism
- Small m.e. are responsible for the **non-collective** damping

Collective vs. Non-collective Damping in ^{208}Pb

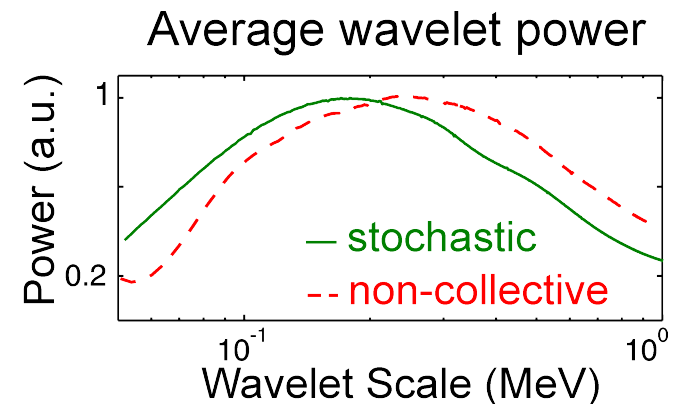
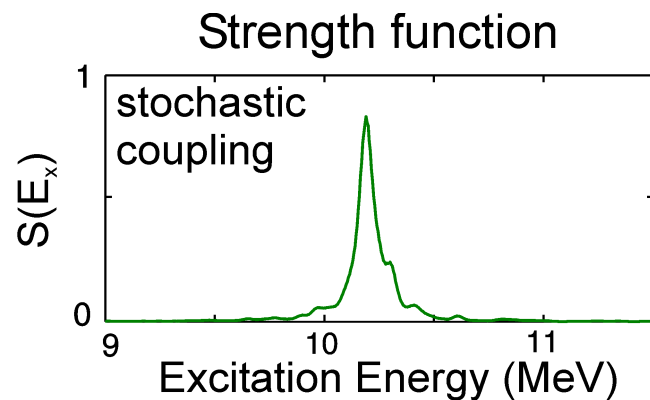


- **Collective part:**
- **Non-collective part:**

all scales

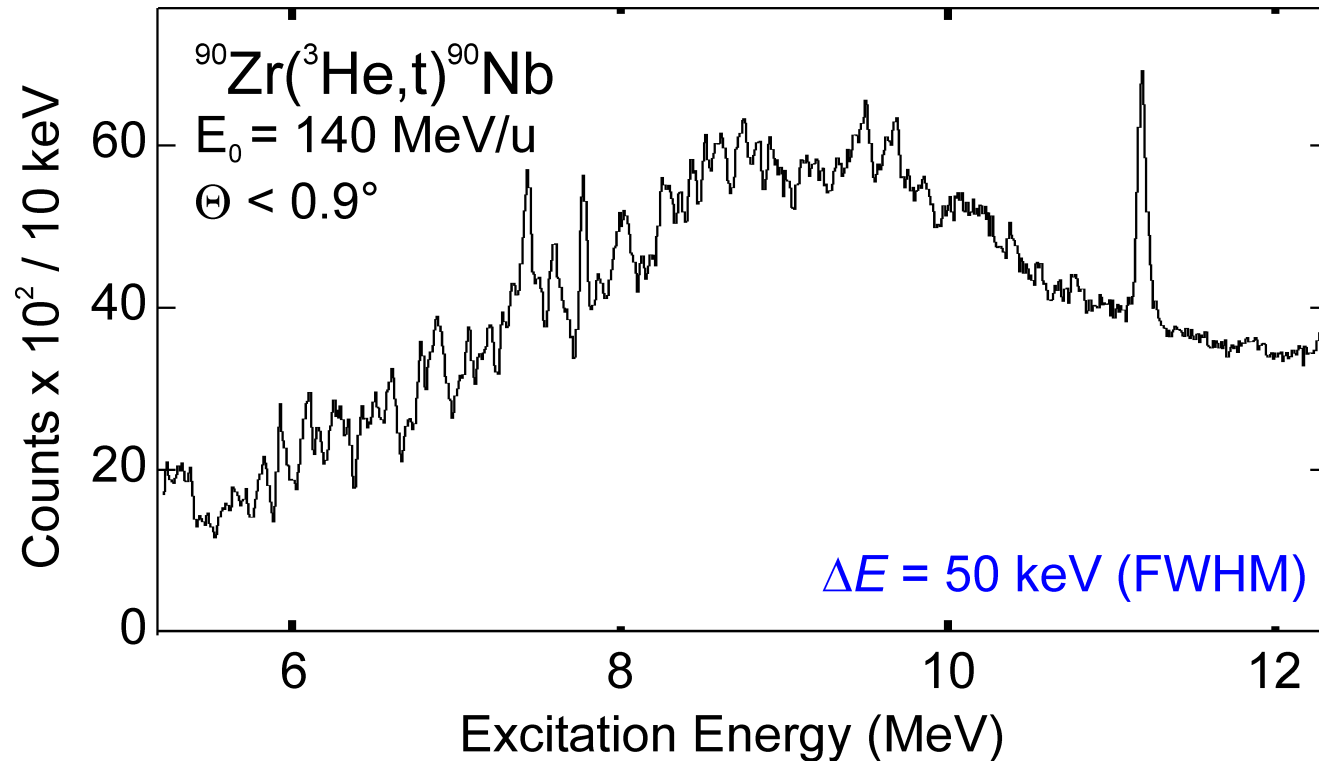
no prominent scales

- Gaussian distribution for coupling matrix elements (RMT)
- Level spacing distribution according to GOE
- Average over statistical ensemble



- Similar results as for the non-collective damping mechanism
- Generic behavior of the non-collective damping?

Fine Structure of the Spin-Flip GTR



- Observed for the first time in a heavy nucleus
- Asymmetric fluctuations
- Selectivity: $J^\pi = 1^+ \rightarrow$ level density

Wavelet coefficients:
$$C(\delta E, E_x) = \frac{1}{\sqrt{\delta E}} \int \sigma(E) \Psi^*\left(\frac{E_x - E}{\delta E}\right) dE$$

↑ ↑ ↑ ↑
scale position spectrum wavelet

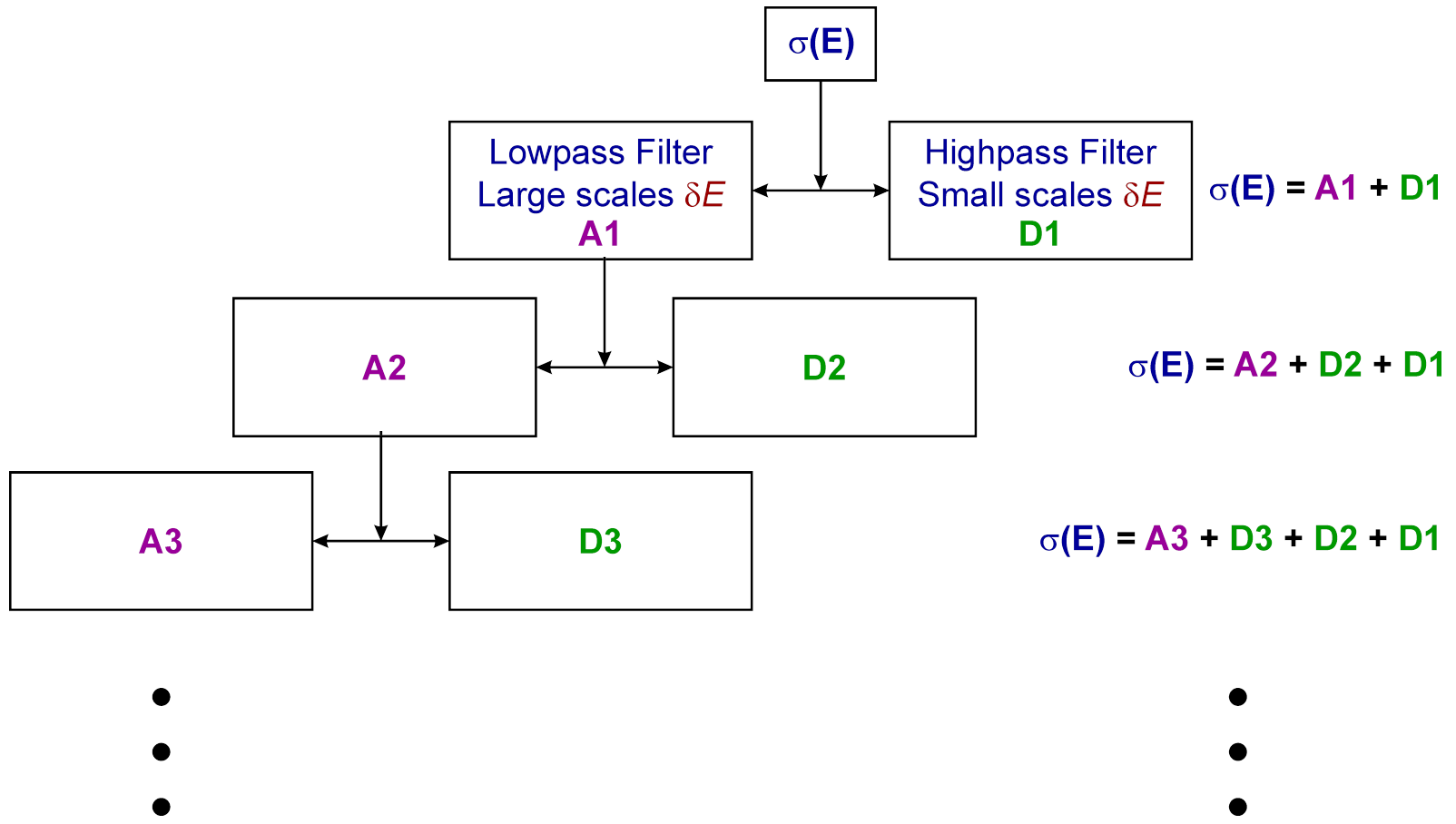
Discrete: $\delta E = 2^j$ and $E_x = k \delta E$ with $j, k = 1, 2, 3,$

...

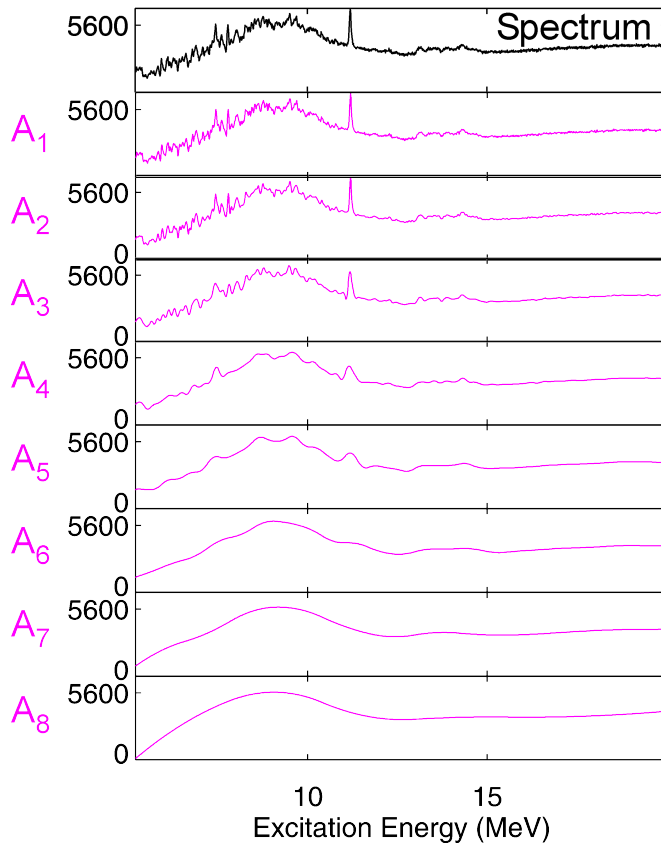
- Orthogonal basis of wavelet functions
- Exact reconstruction of the spectrum is possible
- Relevance of scales

Resolution is limited to ranges of scales

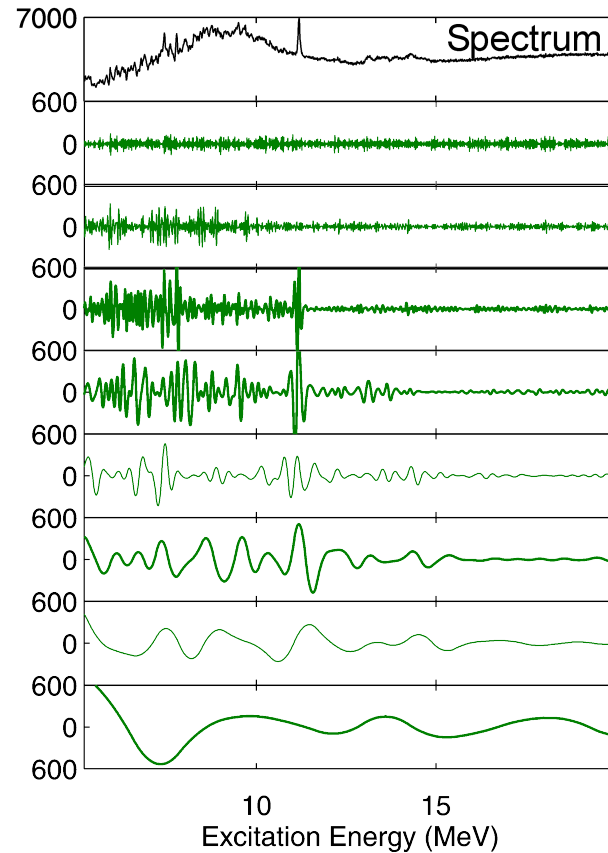
Decomposition



Approximations A_i



Details D_i

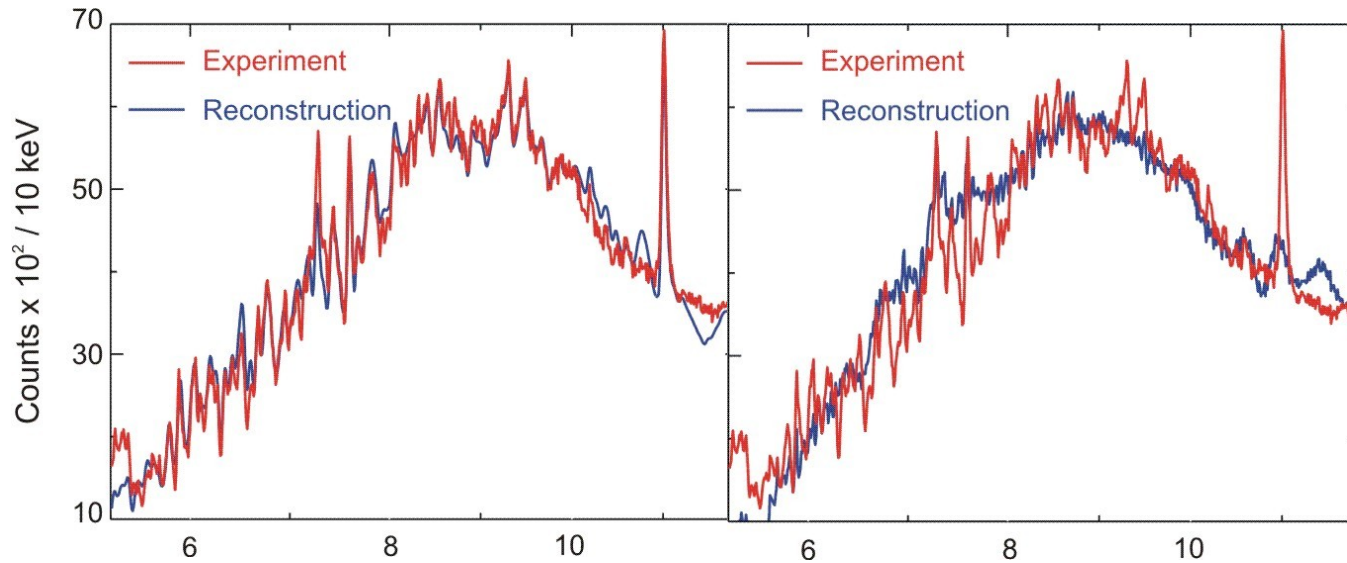


Range of Scales

D_1	20 - 40 keV	
D_2	40 - 80 keV	
D_3	80 - 160 keV	←
D_4	160 - 320 keV	←
D_5	320 - 640 keV	
D_6	640 - 1200 keV	←
D_7	1.2 - 2.4 MeV	
D_8	2.4 - 4.8 MeV	←

- Reconstruct the spectrum using important scales

$$\sigma_r(E) = A8 + D8 + D6 + D4 + D3 \quad \sigma_r(E) = A8 + D7 + D5 + D2 + D1$$

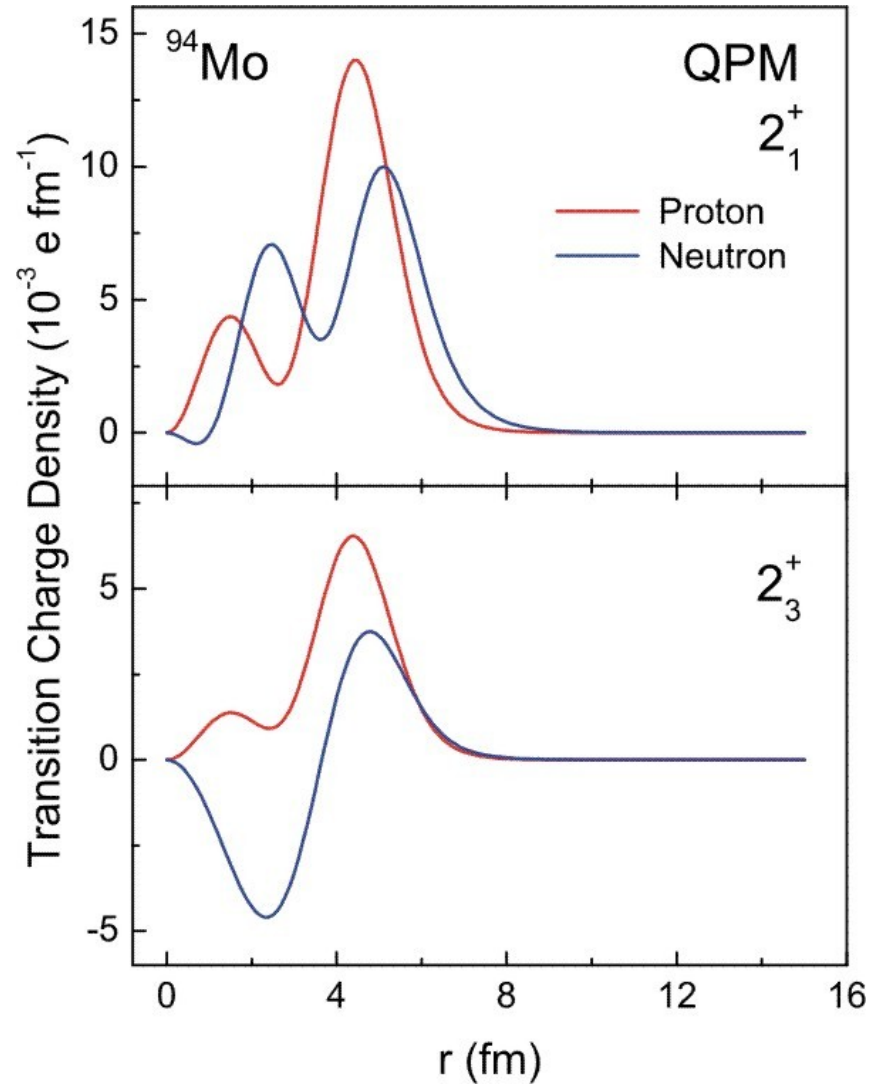


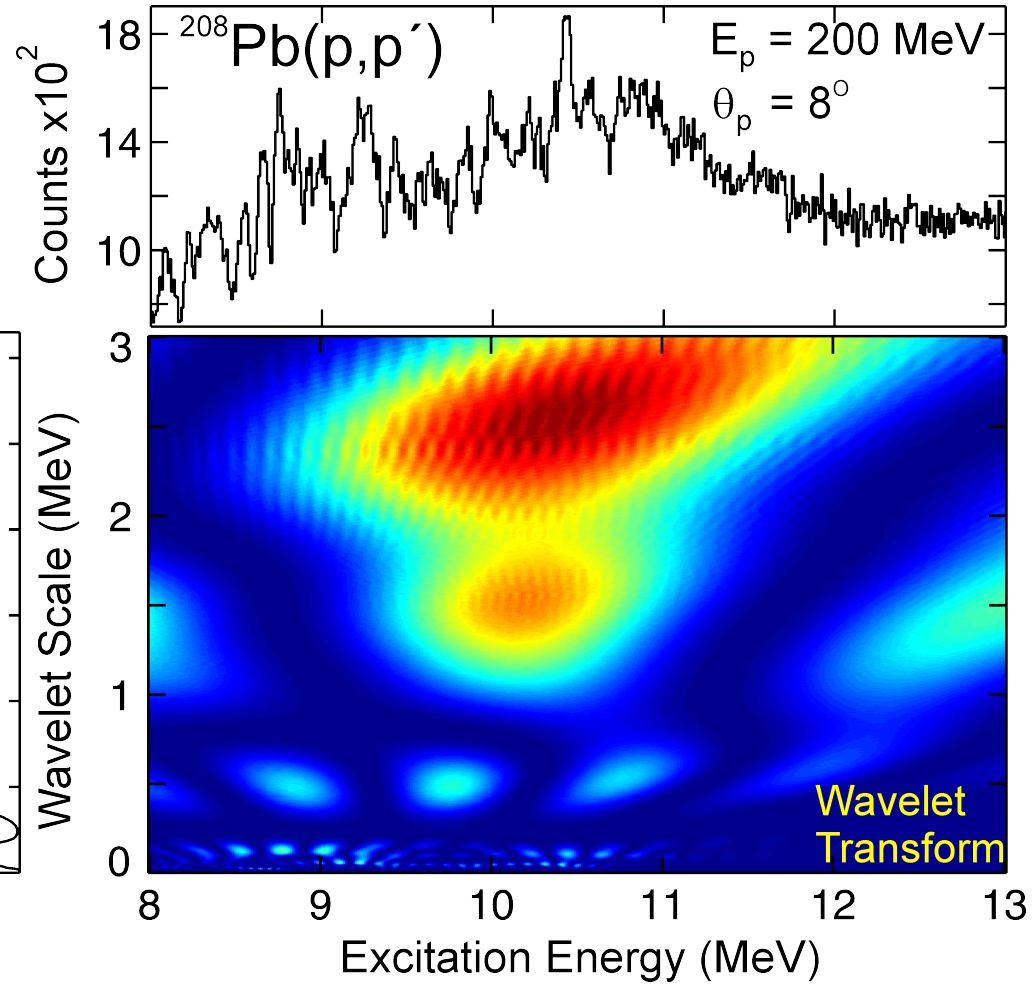
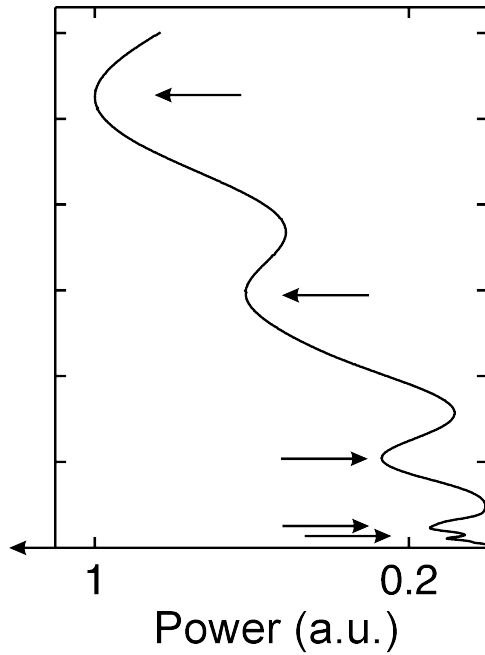
- Relevance of scale regions can be tested
- DWT and CWT results are consistent

- Fine structure is a general phenomenon of giant resonances
 - over a whole mass range
 - in different types of resonances
- Quantitative analysis with wavelets
- Origin of scales:
 - collective damping: low-lying surface vibrations
 - non-collective damping: stochastic coupling
- Relevance of scales for discrete wave transform
- Model-independent level densities

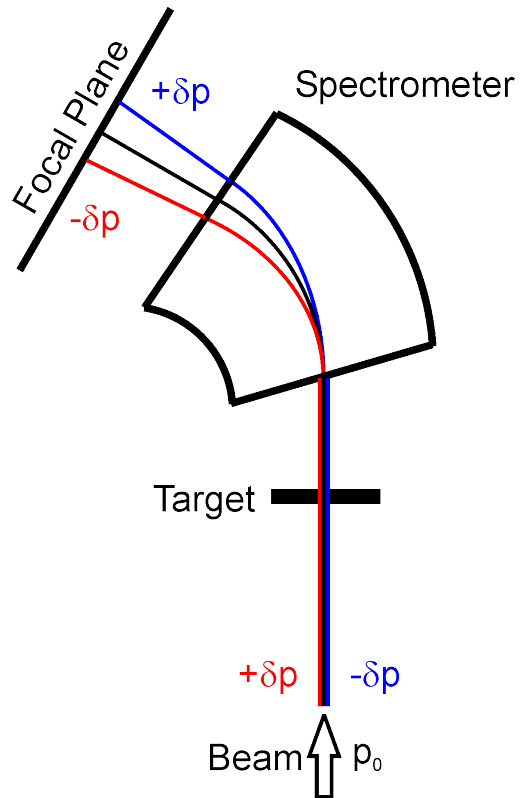
- Goal: next step in the hierarchy: 3p-3h
→ improvement of experimental resolution
- Contribution of other damping mechanisms
→ escape width
→ Landau damping
- Quantitative analysis of scales:
→ experiment and models

Radial Transition Charge Densities



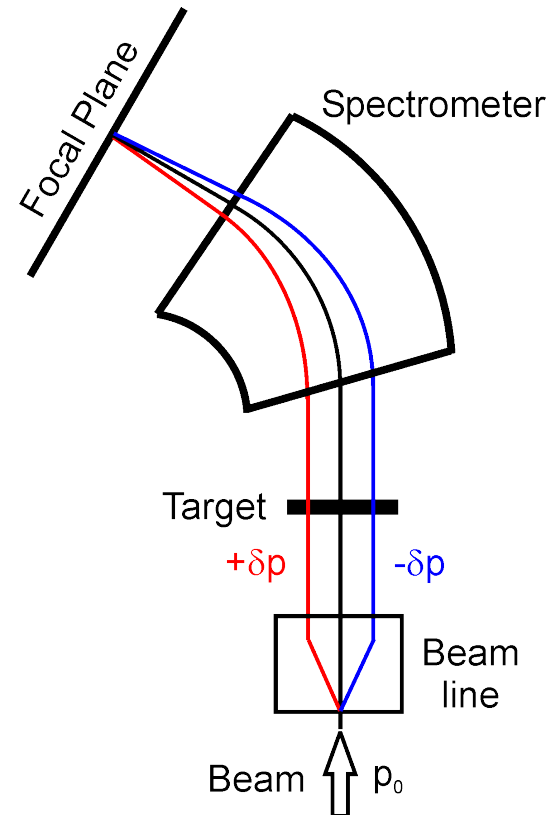


Achromatic mode



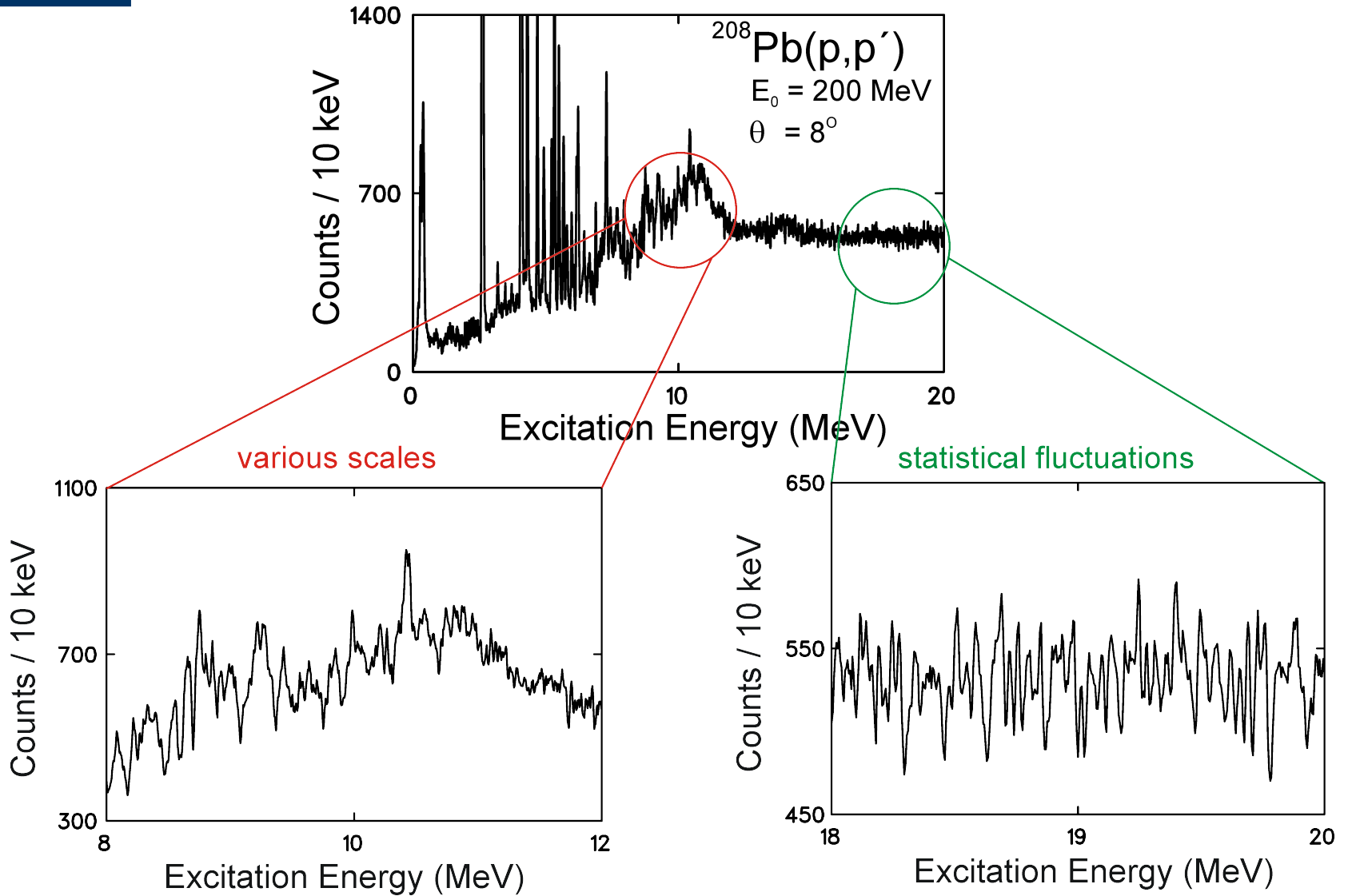
$\Delta E \sim 100 \text{ keV}$

Lateral dispersion matching

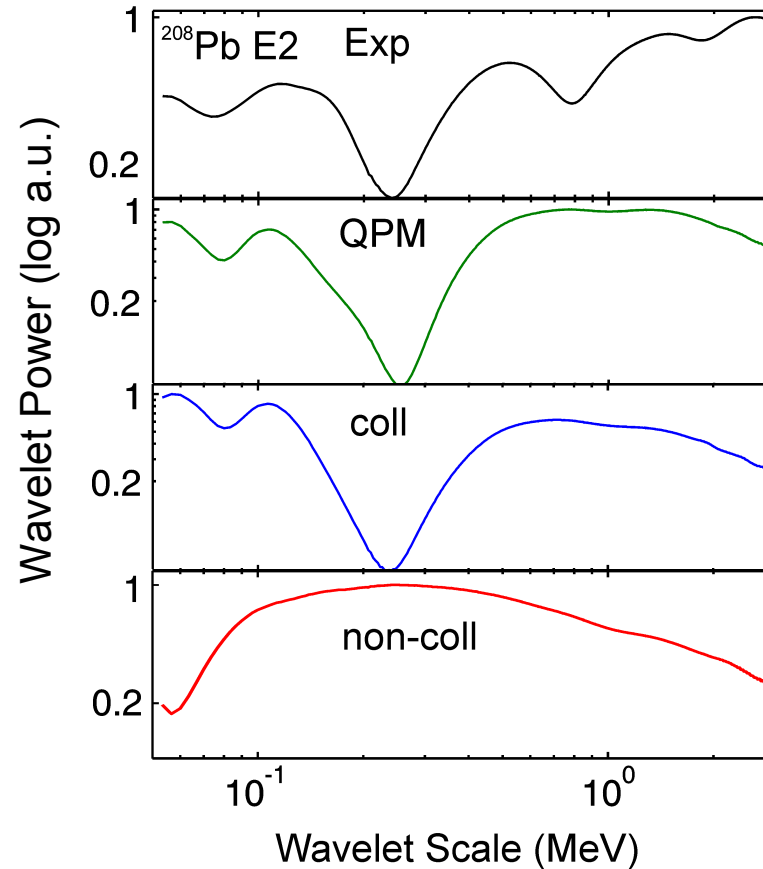


$\Delta E \sim 30 \text{ keV}$

Scales and Fluctuations



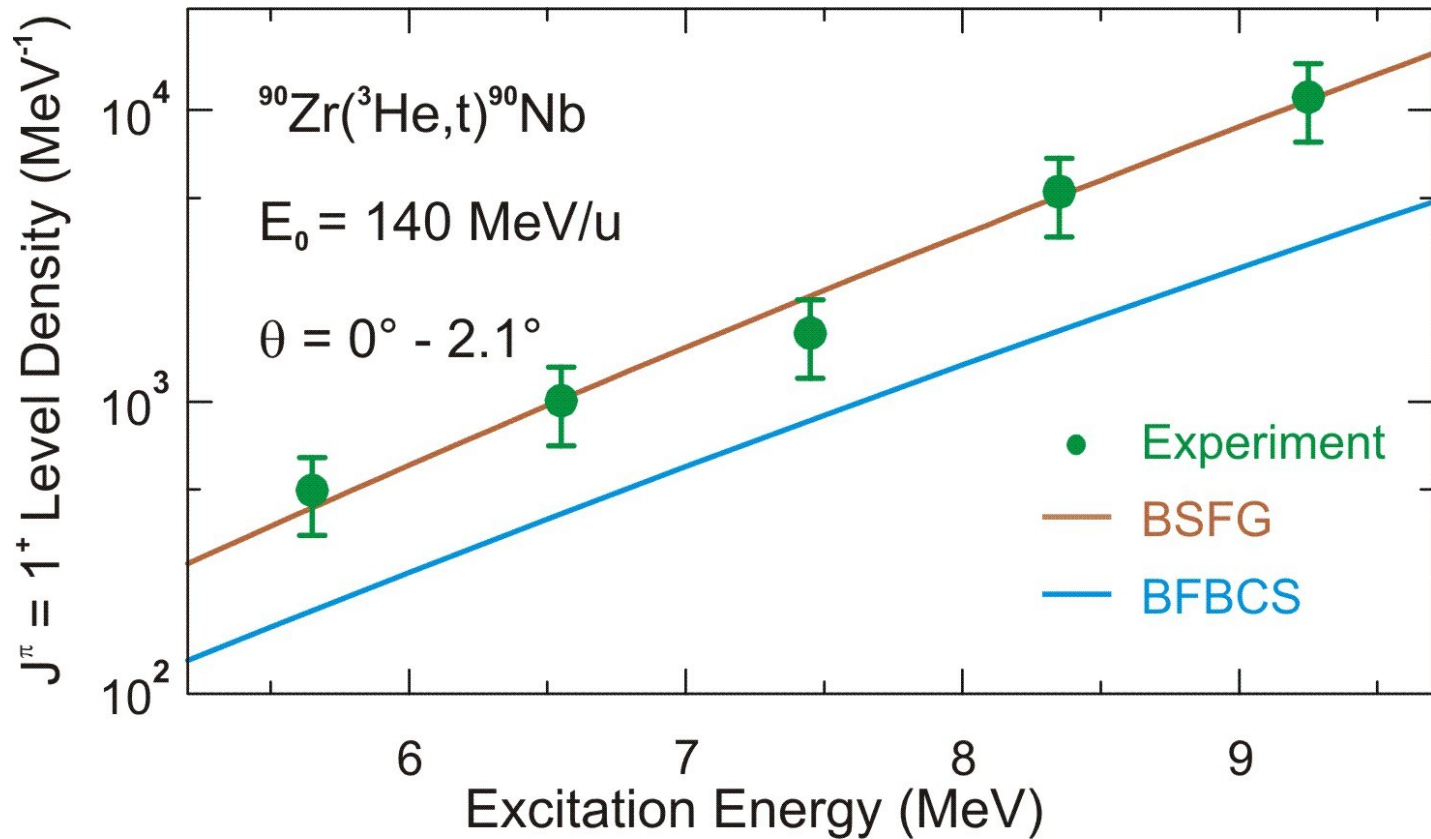
Collective vs. Non-collective Damping in ^{208}Pb



- **Collective part:** all scales
- **Non-collective part:** no prominent scales



Stochastic coupling



T. Rauscher et al. (1997)

P. Demetriou, S. Goriely (2001)

- Important for astrophysics network calculations

Autocorrelation function of stationary spectrum $d(E_x)$

$$C(\epsilon) = \frac{\langle d(E_x) \cdot d(E_x + \epsilon) \rangle}{\langle d(E_x) \rangle \cdot \langle d(E_x + \epsilon) \rangle}$$



Proportional to the mean level spacing

$$C(\epsilon = 0) - 1 \sim \langle D \rangle$$



Background?

Wavelet transform of spectrum $\sigma(E)$

$$C(\delta E, E_x) = \frac{1}{\sqrt{\delta E}} \int_{-\infty}^{\infty} \sigma(E) \Psi^* \left(\frac{E_x - E}{\delta E} \right) dE$$



Vanishing moments m of wavelet function Ψ

$$\int_{-\infty}^{\infty} E^n \Psi(E) dE = 0, \quad n = 0, 1 \dots m-1$$



Background suppression

Extraction of the mean level spacing

