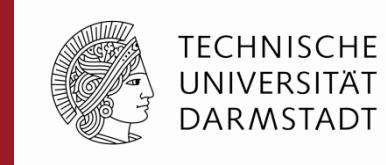


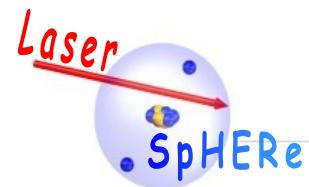
SFB 1245 Meet & Greet: Laser Spectroscopy in A01 and A03



Charge Radii and Nuclear Moments from Laser Spectroscopy
Wilfried Nörtershäuser

24.02.2016

From frequencies to nuclear moments
The principle of collinear laser spectroscopy
Collinear spectroscopy online: Where and why?
A01: Charge radius of ${}^8\text{B}$
A03: Nuclear moments of Fe and Pd isotopes



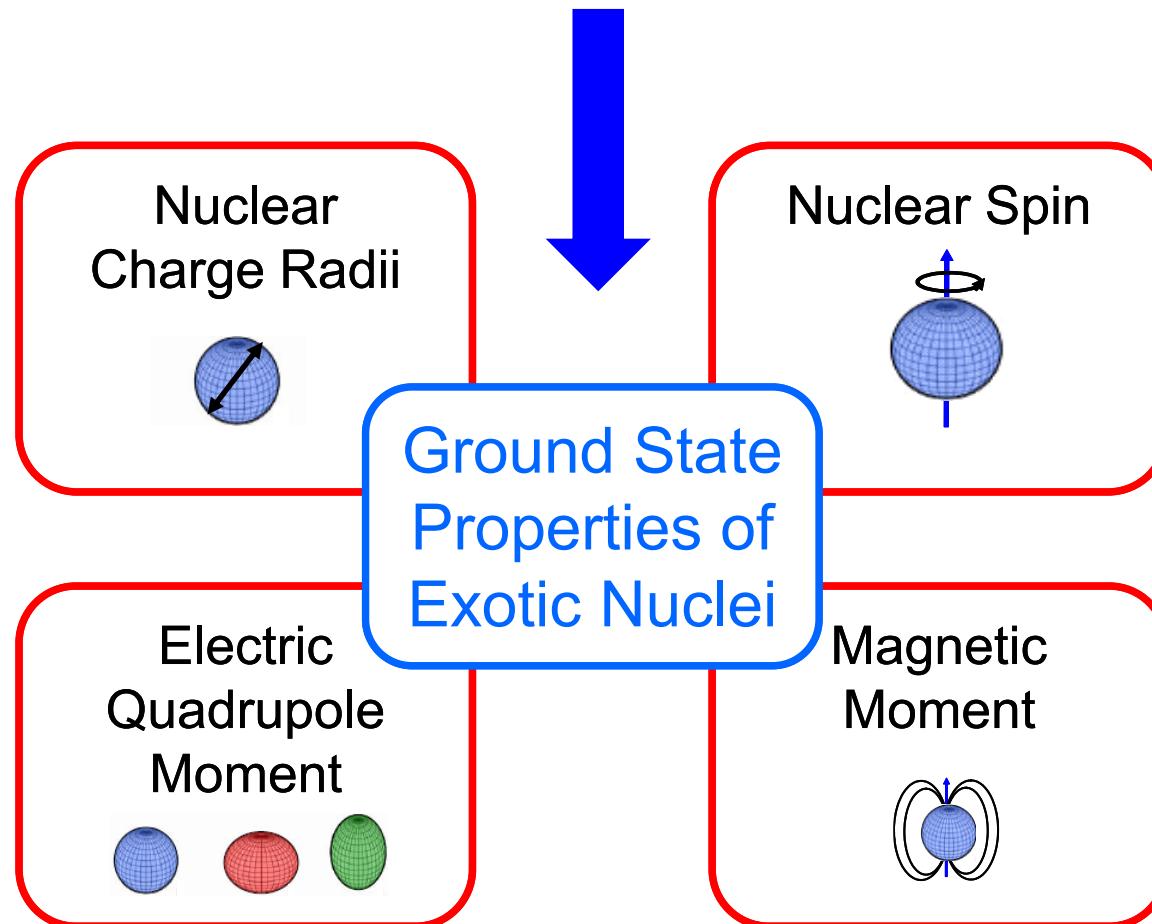
Laser Spectroscopy of
Highly Charged Ions and
Exotic Radioactive Nuclei



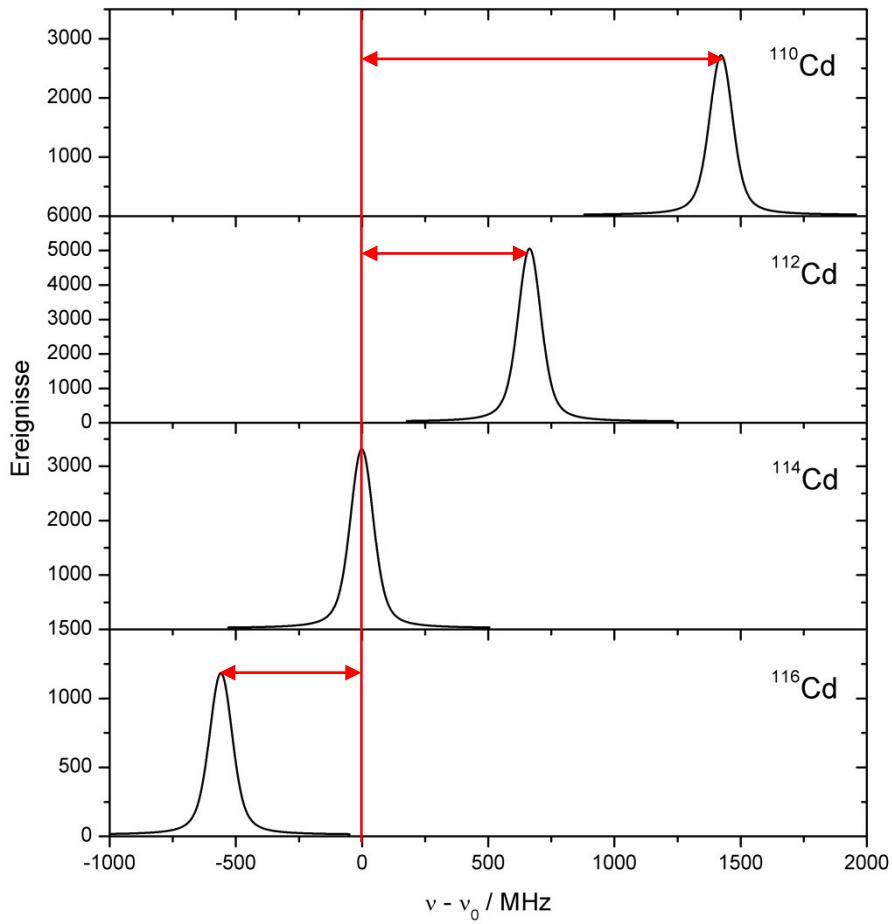
Nuclear Information from Laser Spectroscopy



TECHNISCHE
UNIVERSITÄT
DARMSTADT



Isotope Shift

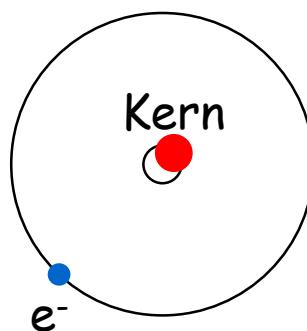


Isotope
shift

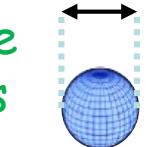


$$\delta_{\text{IS}}^{A,A'} = K \cdot \frac{M_{A'} - M_A}{M_A M_{A'}} + F \cdot \delta \langle r^2 \rangle^{A,A'}$$

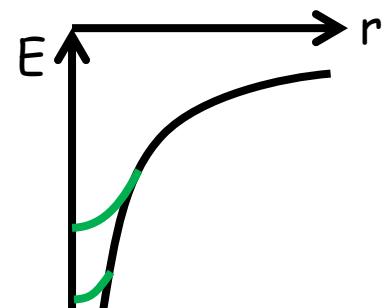
Mass effect



Charge
radius



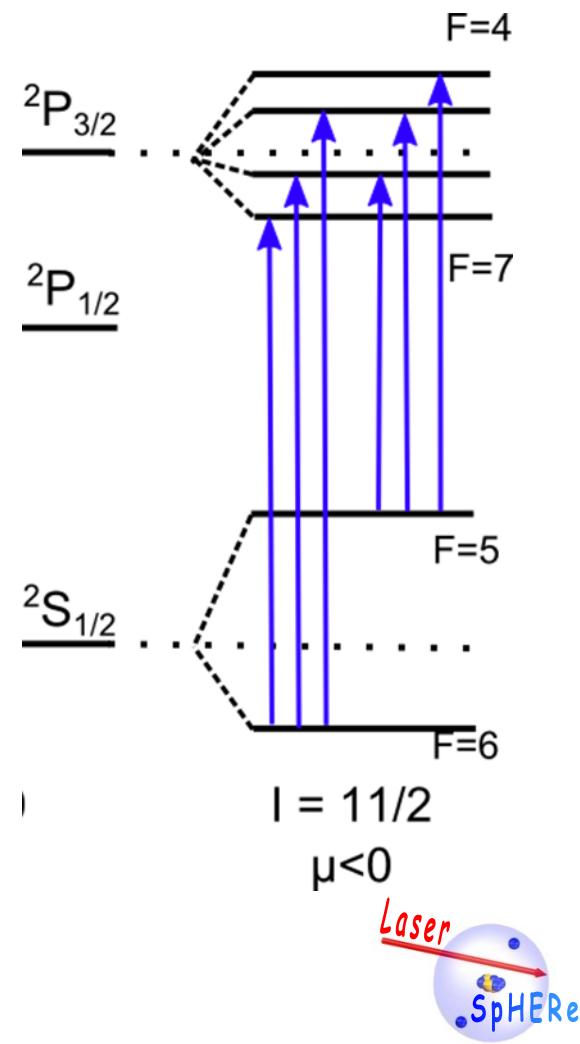
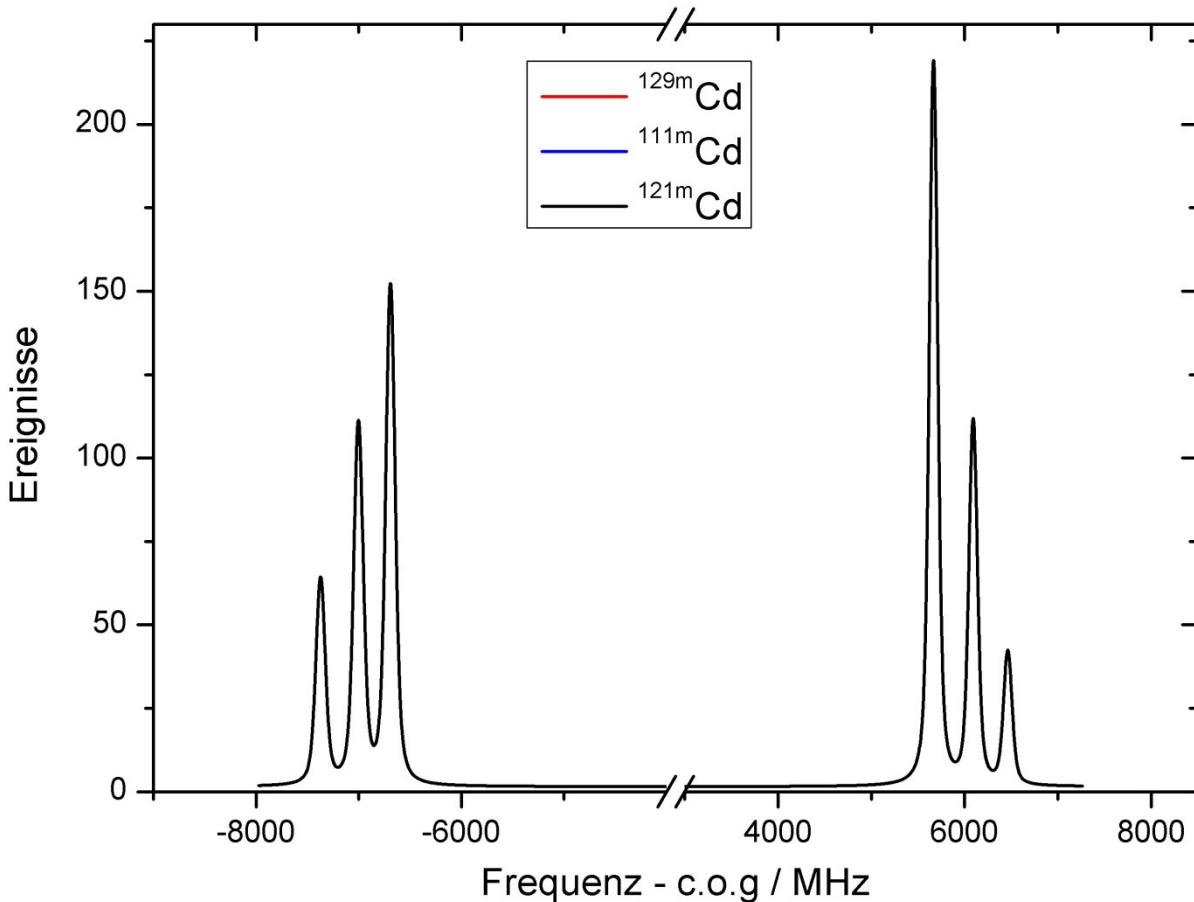
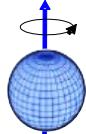
Field effect



Hyperfine Structure



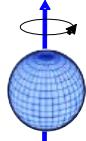
Spin



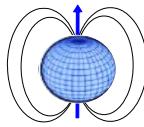
Hyperfine Structure



Spin

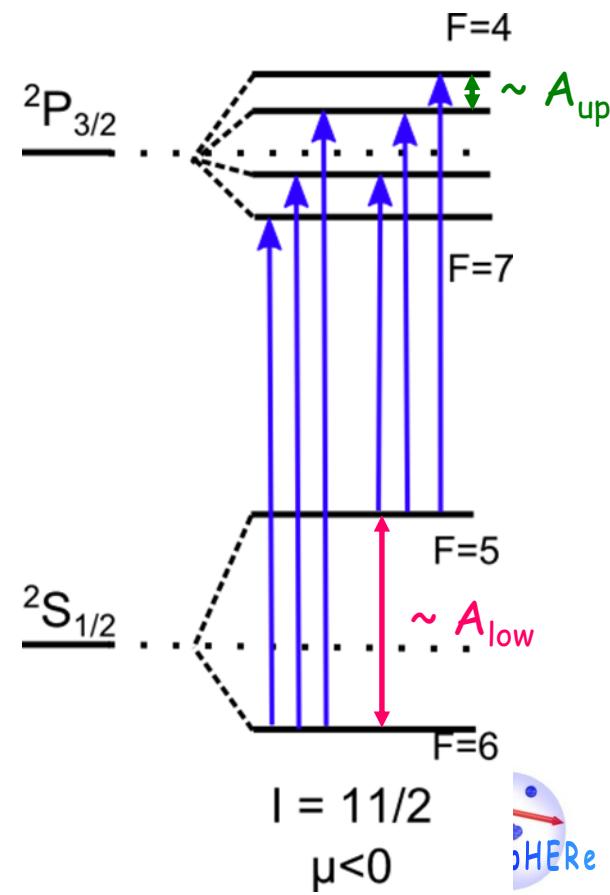
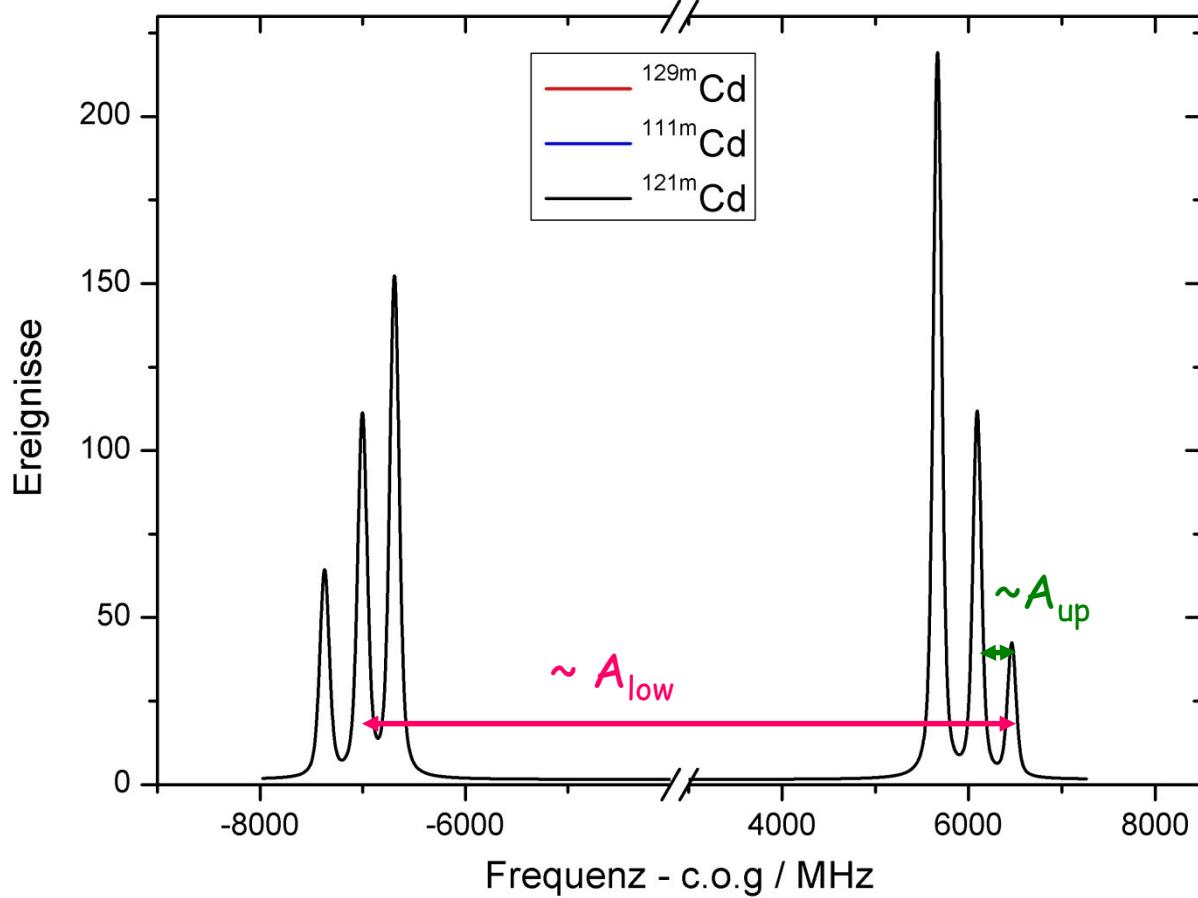


Magnetic Moment, μ_l



$$A = \frac{\mu_l H_e(0)}{I \cdot J},$$

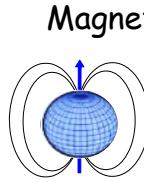
$H_e(0)$ = magnetic field at nuclear site



Hyperfine Structure



Spin

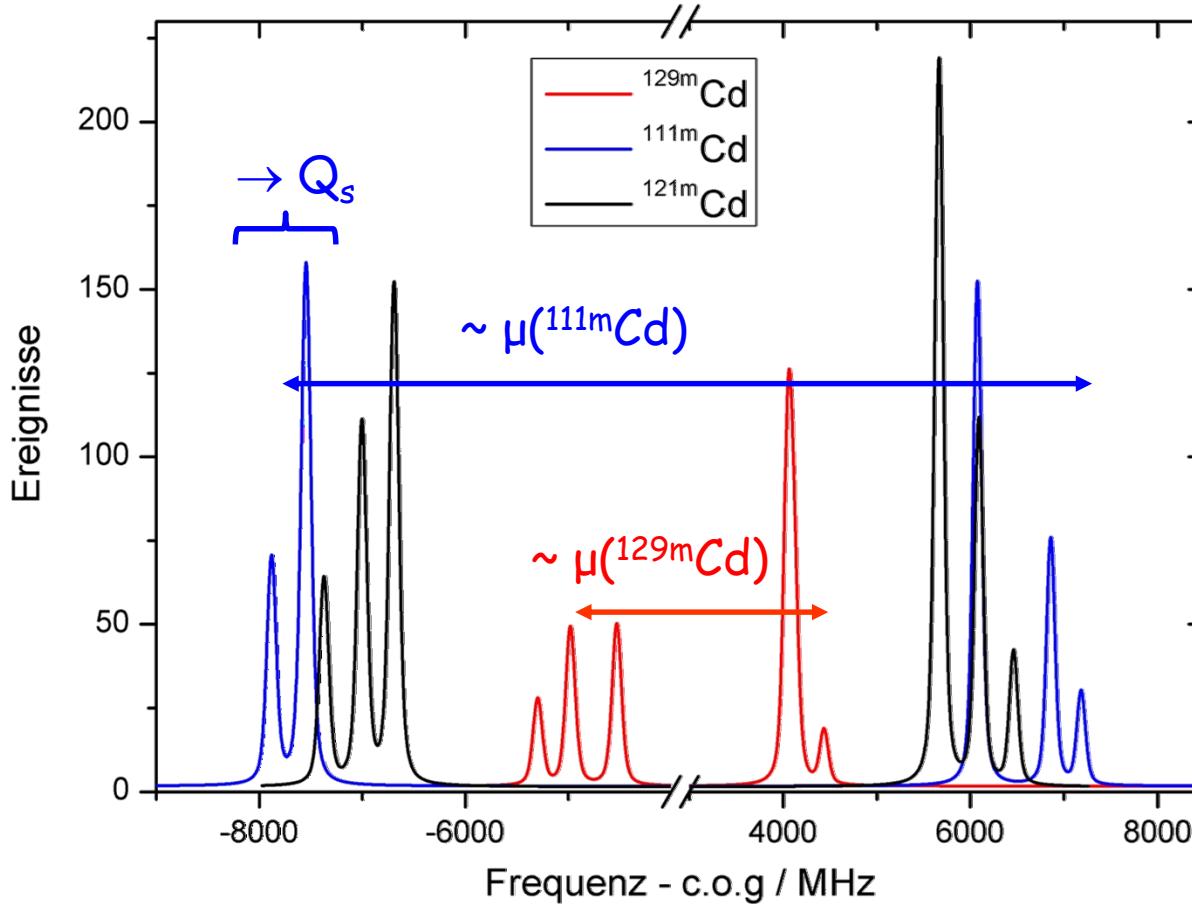


Magnetic Moment, μ_I

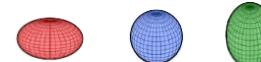
$$A = \frac{\mu_I H_e(0)}{I \cdot J},$$

$H_e(0)$ = magnetic field at nuclear site

↓



Spectroscopic quadrupole moment Q_s



$$B = eQ_s V_{zz}(0),$$

$V_{zz}(0)$ = electric field gradient
at nuclear site

F=4

$^2\text{P}_{3/2}$

F=7

$^2\text{S}_{1/2}$

F=5

F=6

$I = 11/2$
 $\mu < 0$



Evaluation of the Hyperfine Structure



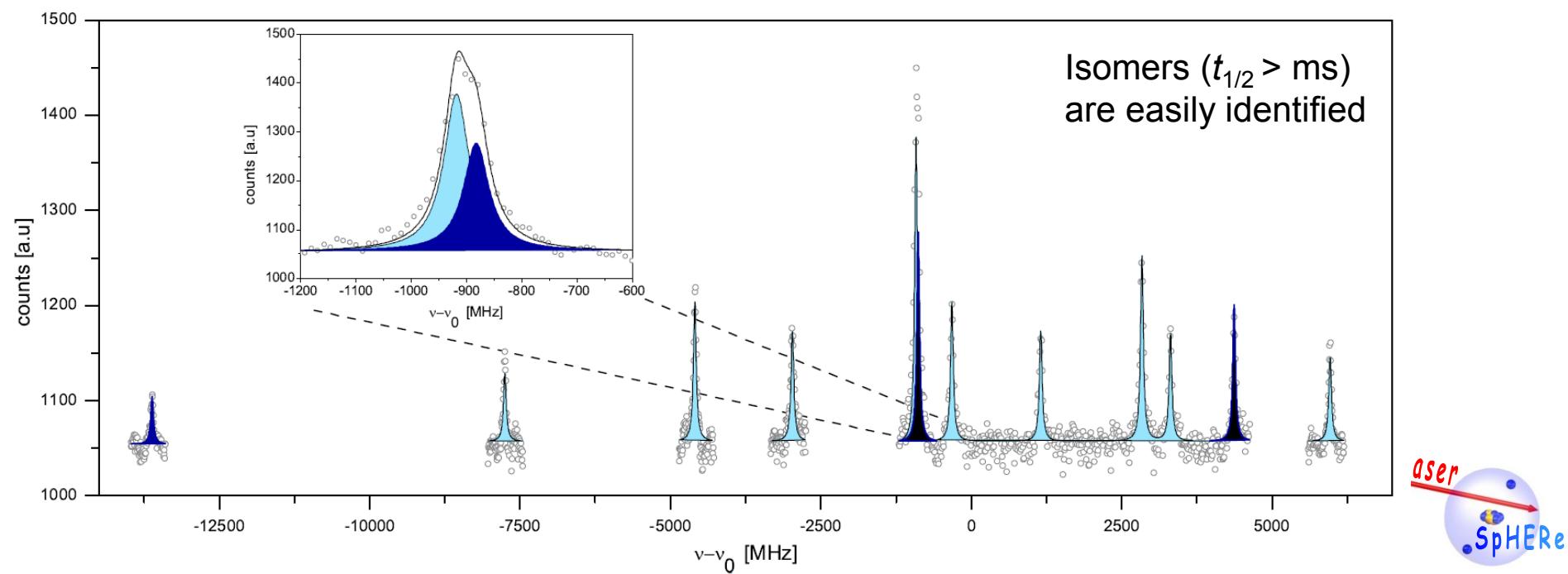
Peak Positions: $\nu = \nu_0 + \alpha_{\text{up}} A_{\text{up}} + \beta_{\text{up}} B_{\text{up}} - \alpha_{\text{low}} A_{\text{low}} - \beta_{\text{low}} B_{\text{low}}$

$$\alpha_{\text{up,low}}(I, J, F) = \frac{C}{2} = \frac{F(F+1) - I(I+1) - J(J+1)}{2} \quad \beta_{\text{up,low}}(I, J, F) = \frac{\frac{3}{4}C(C+1) - I(I+1)J(J+1)}{2(2I-1)(2J-1)I \cdot J}$$

choose I, Nonlinear Least Squares Fitting $\Rightarrow A_u, A_l, B_u, B_l, \nu_0, \chi^2_{\text{red}}$

Isomer-Shift:

Isomer-Spin: I^m $\nu^m = \nu_{\text{IS}}^m + \alpha_{\text{up}}^m A_{\text{up}}^m + \beta_{\text{up}}^m B_{\text{up}}^m - \alpha_{\text{low}}^m A_{\text{low}}^m - \beta_{\text{low}}^m B_{\text{low}}^m$ $\delta\nu_{\text{Isomer}} = \nu_{\text{IS}} - \nu_{\text{IS}}^m$



Origin of Collinear Laser Spectroscopy



TECHNISCHE
UNIVERSITÄT
DARMSTADT

Volume 17, number 3

OPTICS COMMUNICATIONS

HIGH-RESOLUTION LASER SPECTROSCOPY IN FAST BEAMS

S.L. KAUFMAN

*Institut für Physik, Johannes Gutenberg-Universität,
D-6500 Mainz, Fed. Rep. of Germany*

Received 3 March [REDACTED]

Collinear Laser Spectroscopy on Fast Atomic Beams

K.-R. Anton, S. L. Kaufman,^(a) W. Klempert, G. Moruzzi,^(b) R. Neugart,
E.-W. Otten, and B. Schinzler

Institut für Physik, Johannes Gutenberg-Universität, D-6500 Mainz, Federal Republic of Germany

(Received 1 August [REDACTED])

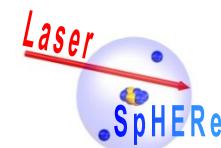
In collinear geometry we have observed laser-excited, narrow resonances in fast beams of Na and Cs atoms obtained from ion beams by charge transfer collisions. Being



E.-W. Otten

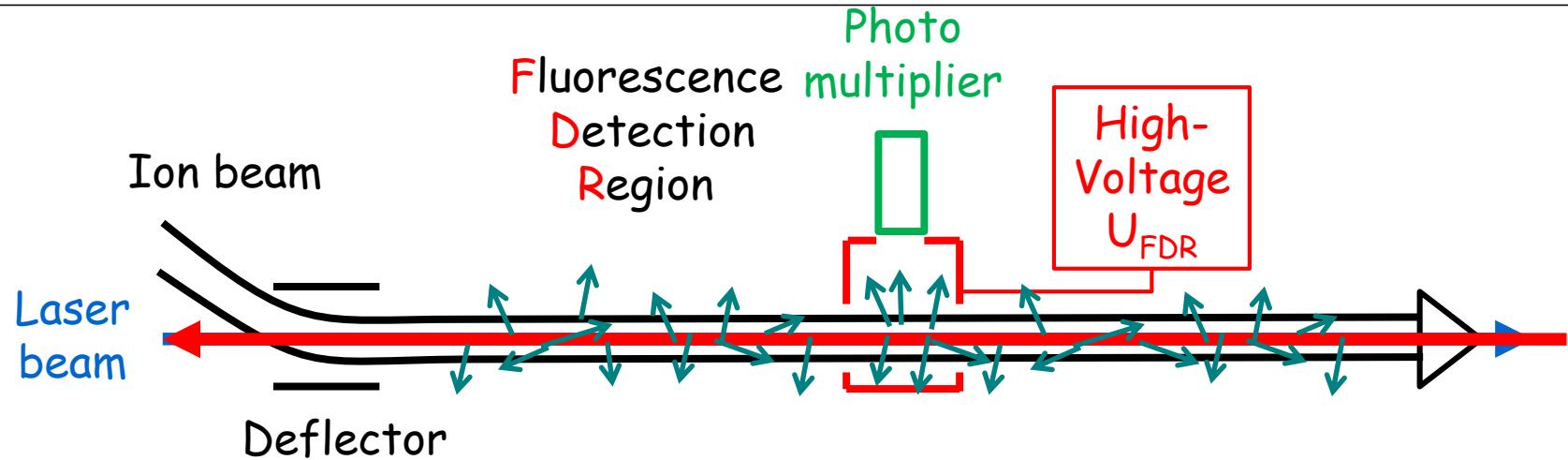


R. Neugart



1980 First results at ISOLDE/CERN →
COLLAPS

The Principle of Collinear Spectroscopy



Collinear Doppler shift:

$$\nu_{\text{ion}} = \nu_{\text{laser}} \cdot \gamma \cdot (1 - \beta)$$

$$\beta = v/c$$

Anticollinear Doppler shift:

$$\nu_{\text{ion}} = \nu_{\text{laser}} \cdot \gamma \cdot (1 + \beta)$$

$$\gamma = \frac{1}{\sqrt{(1 - \beta^2)}}$$

Resonance condition:

$$\nu_{\text{ion}} = \nu_0$$

Doppler-Tuning:

$$\beta = \beta(U, m)$$

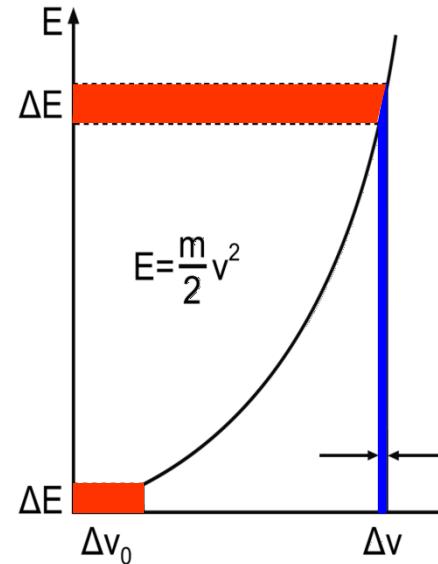
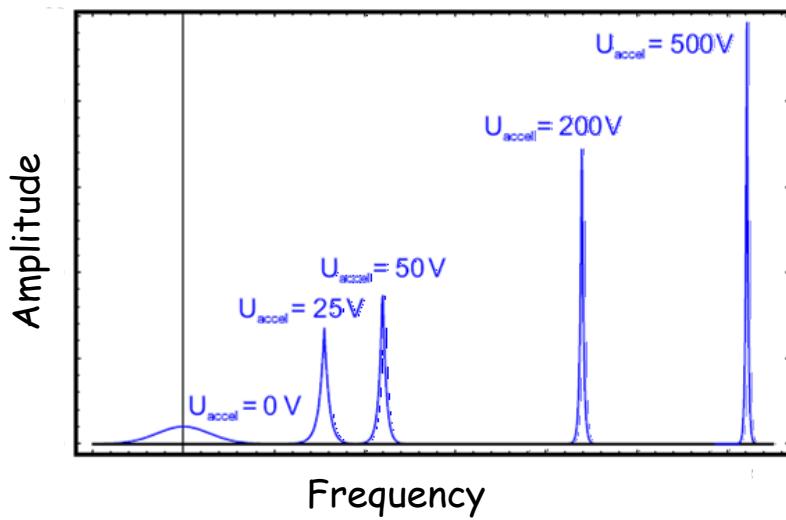
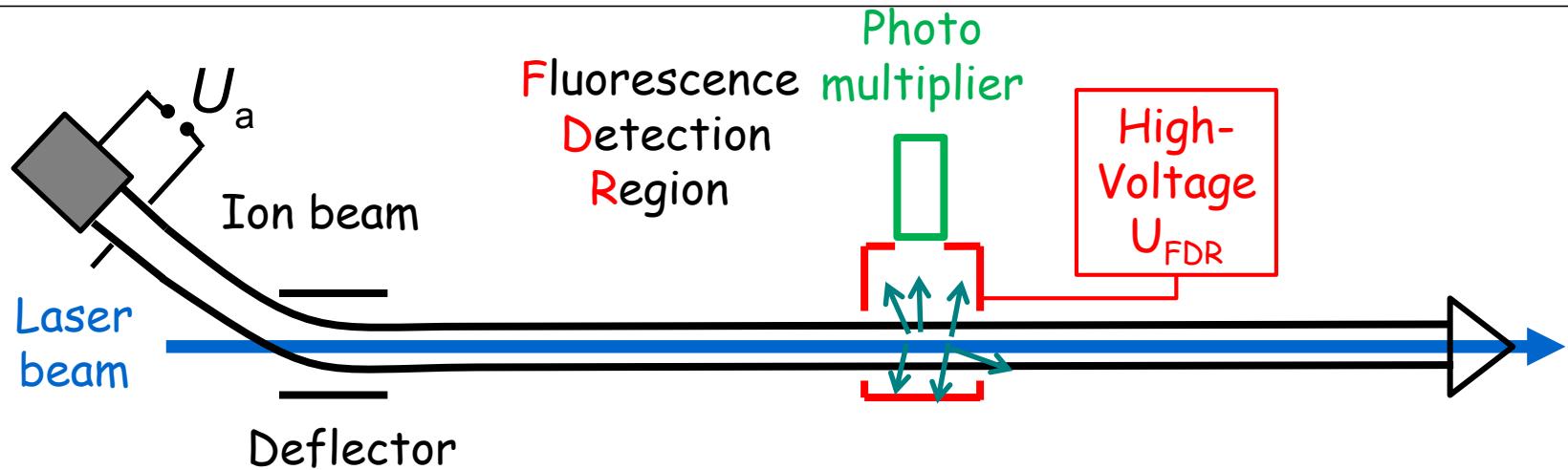
$$\Delta \nu_{\text{ion}} = \frac{\partial \nu_{\text{ion}}}{\partial U} \Delta U$$

$$\frac{\partial \nu_{\text{ion}}}{\partial U} = \frac{e \nu_0}{\sqrt{2eUMc^2}}$$

The Principle of Collinear Spectroscopy



TECHNISCHE
UNIVERSITÄT
DARMSTADT



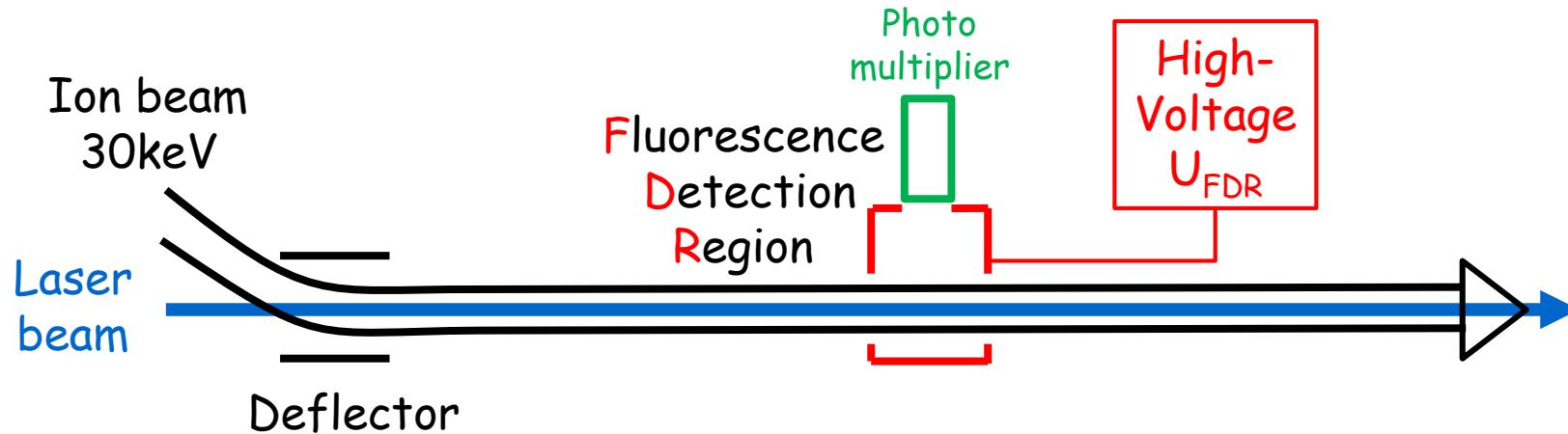
$$E = eU_a = 1/2mv^2$$

$$\delta E = mv \delta v$$

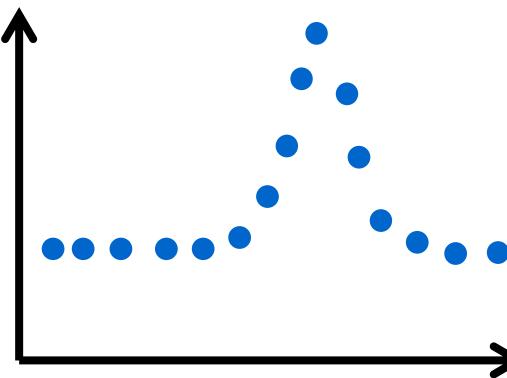
$$\delta\nu_{Doppler} = \nu_0 \delta v/c$$

$$= \nu_0 \frac{\delta E}{\sqrt{2eU_a mc^2}}$$

Data Taking in Collinear Spectroscopy

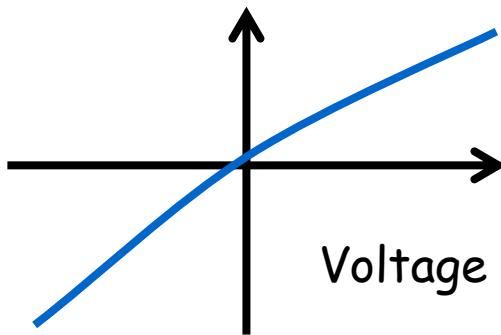


Count rate



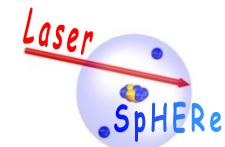
Voltage U_{FDR}

Frequency



Voltage

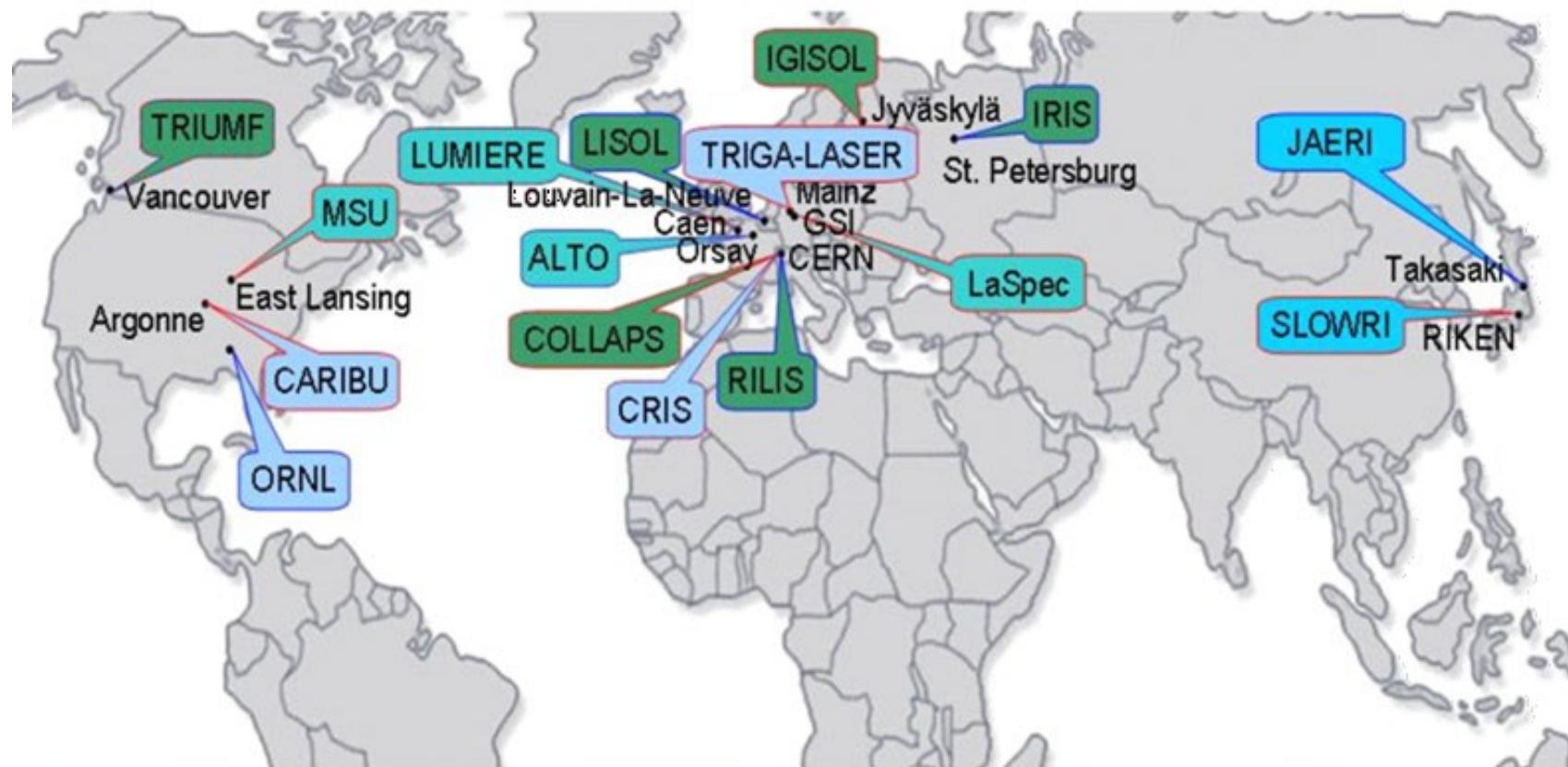
- universal
- fast
- sensitive
- high resolution



Collinear Spectroscopy at On-Line Facilities



TECHNISCHE
UNIVERSITÄT
DARMSTADT



operating facilities

facilities under
construction or test

planned facilities

collinear laser spectroscopy

laser ion source



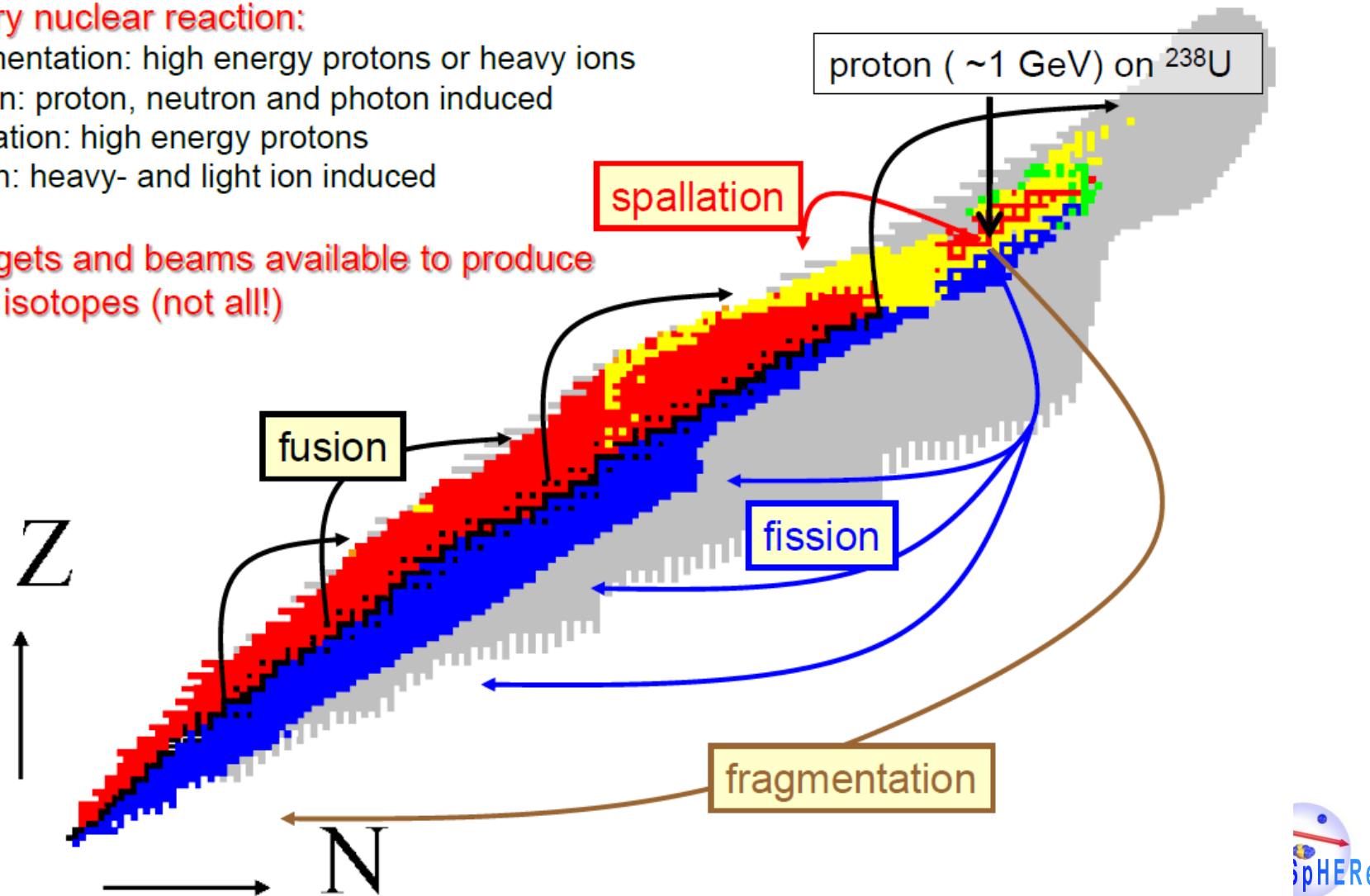
Reactions for Radioisotope Production



- Primary nuclear reaction:

- fragmentation: high energy protons or heavy ions
- fission: proton, neutron and photon induced
- spallation: high energy protons
- fusion: heavy- and light ion induced

⇒ targets and beams available to produce many isotopes (not all!)

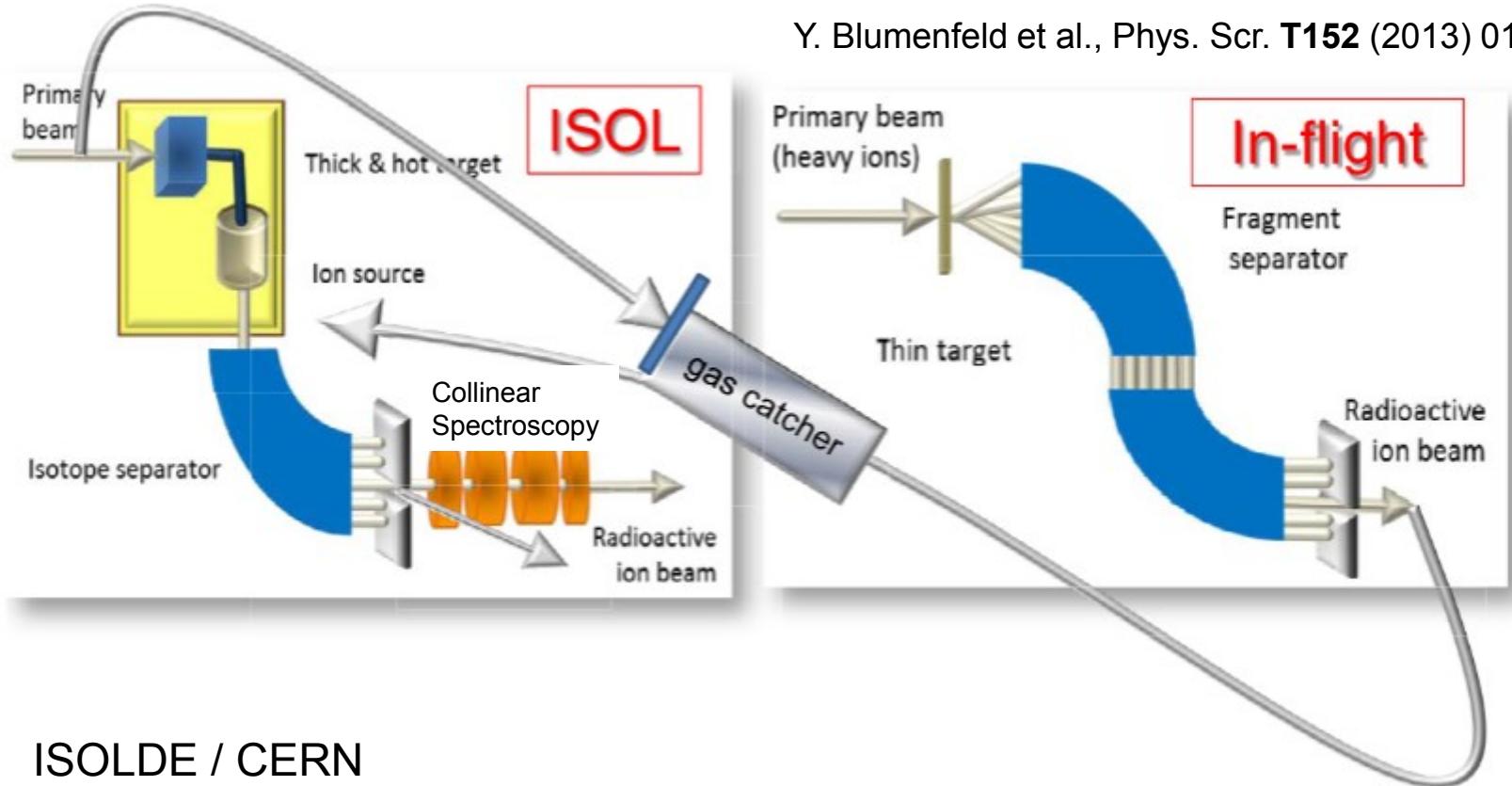


Production Techniques



TECHNISCHE
UNIVERSITÄT
DARMSTADT

Y. Blumenfeld et al., Phys. Scr. **T152** (2013) 014023



ISOLDE / CERN
TRIUMF, Vancouver
SPIRAL2 / GANIL

IGISOL Jyväskylä
CARIBU Argonne
TRIGA-SPEC Mainz

BECOLA - MSU
ATLAS Argonne
FRIB - Riken

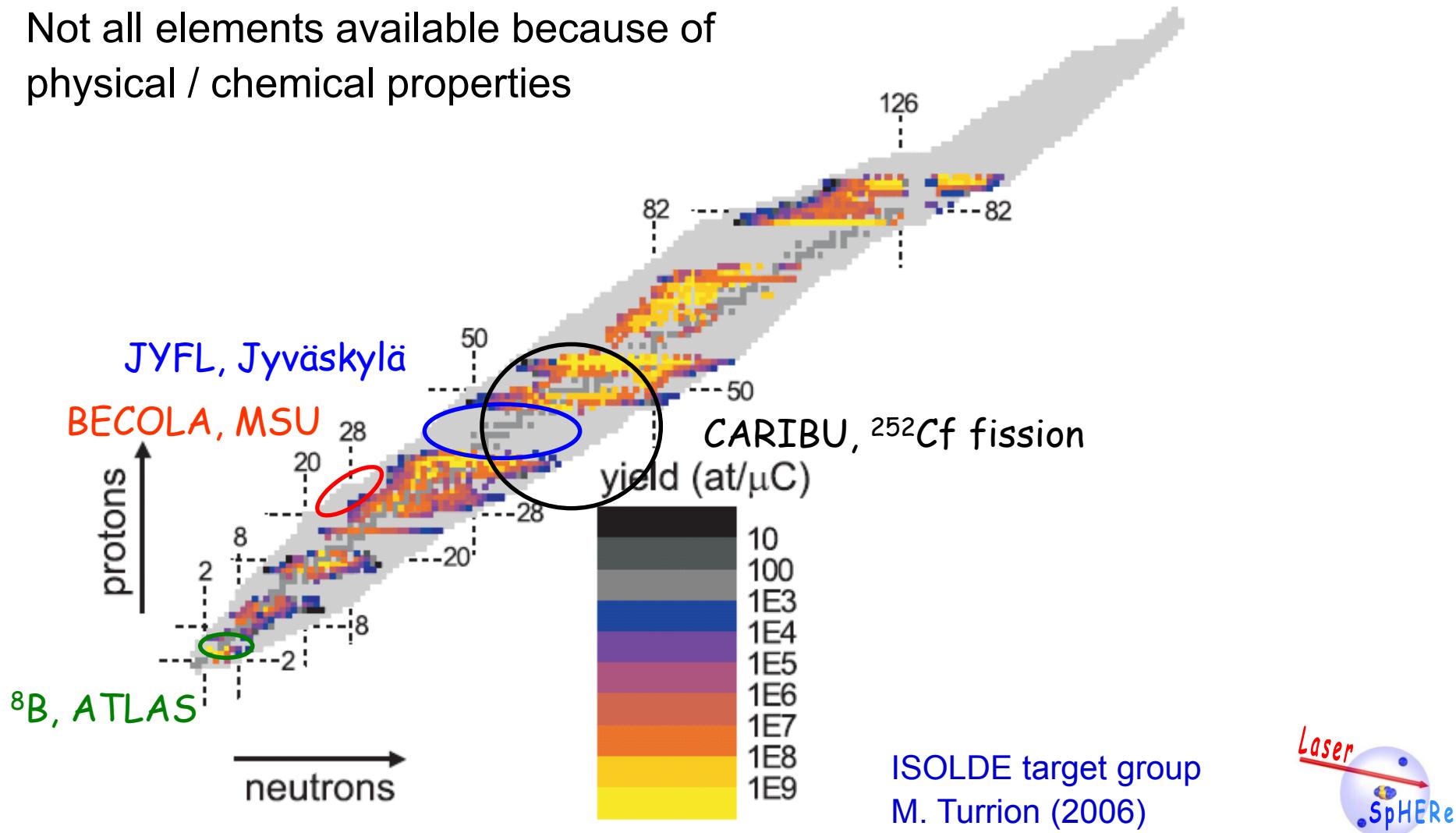


Radionuclides available at ISOLDE



TECHNISCHE
UNIVERSITÄT
DARMSTADT

Not all elements available because of
physical / chemical properties



Recent Laser Spectroscopic Work on Ground State Properties



TECHNISCHE
UNIVERSITÄT
DARMSTADT

Heavy Elements: Th-Isomer, Ra, Fr (Parity Violation, EDM),
(ISOLDE: CRIS, Tri μ p, TRIUMF)
Beyond Z=100 (SHIP)

Deformation in the
Z=82, N=126 Region
(ISOLDE:
COMPLIS,
RILIS,CRIS)

N=Z, ^{74}Rb
CKM-Unitarity
(TRIUMF)

Simple Structure in Complex Nuclei
(ISOLDE)

Sudden Appearance of
Deformation at N=60,
(JYFL)

Monopole Migration of SPE
due to Tensor Force (ISOLDE)

Z-Dependence of Radii
N=32 New Shell Closure? (JYFL, ISOLDE)

Island of Inversion (ISOLDE)

Halos and Clustering (TRIUMF, ISOLDE, GANIL, ATLAS)

→ Neutron Number

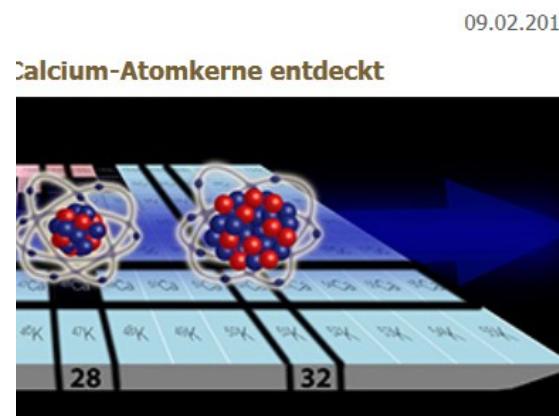
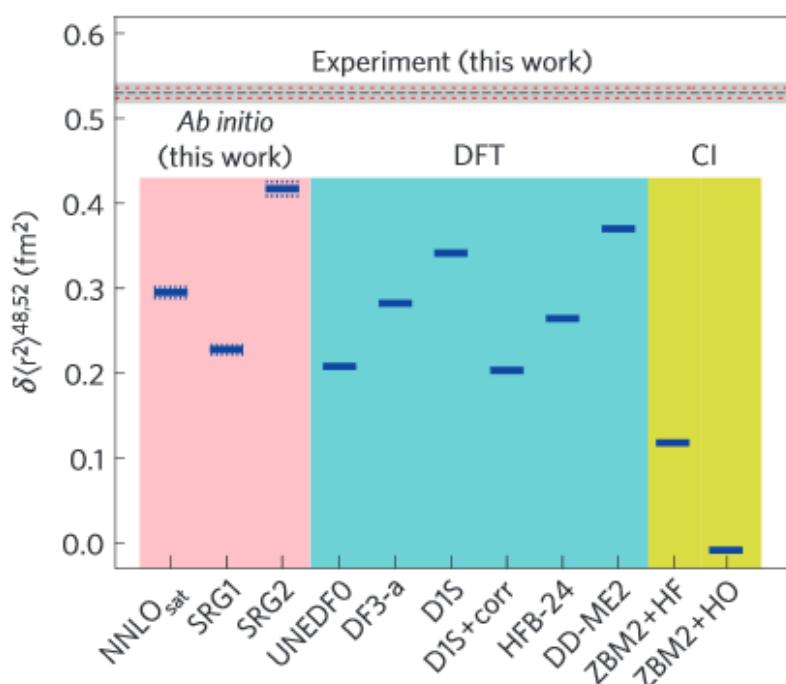
Recent Example



TECHNISCHE
UNIVERSITÄT
DARMSTADT

TU | Die Universität | Vorbeischauen | Studieren | Gemeinsam forschen | Karriere planen | Verbunden bleiben

Suche »



isotope. Die „doppelt magischen“ Isotope mit den Massenzahlen ungsradien. Die erstmalige Messung des Isotops Ca-52 ergab I: COLLAPS Collaboration / Ronald Fernando Garcia Ruiz

er noch für eine Überraschung gut: Nachdem erst von kurzem die Isotope mit den Massenzahlen 52 (Ca-52) und 54 (Ca-54) als weitere „magische“ und damit relativ stabile Kerne in der Isotopenreihe etabliert wurden, passen die Ergebnisse jüngster laserspektroskopischer Untersuchungen an Ca-52 nicht recht in dieses



TECHNISCHE
UNIVERSITÄT
DARMSTADT

Kontakt

Technische Universität Darmstadt

Kommunikation und Medien

S1|01 517
Karolinenplatz 5
64289 Darmstadt

Phone: +49 6151 16-20017
Fax: +49 6151 16-23750

E-mail: presse@tu-darmstadt.de

Publikation

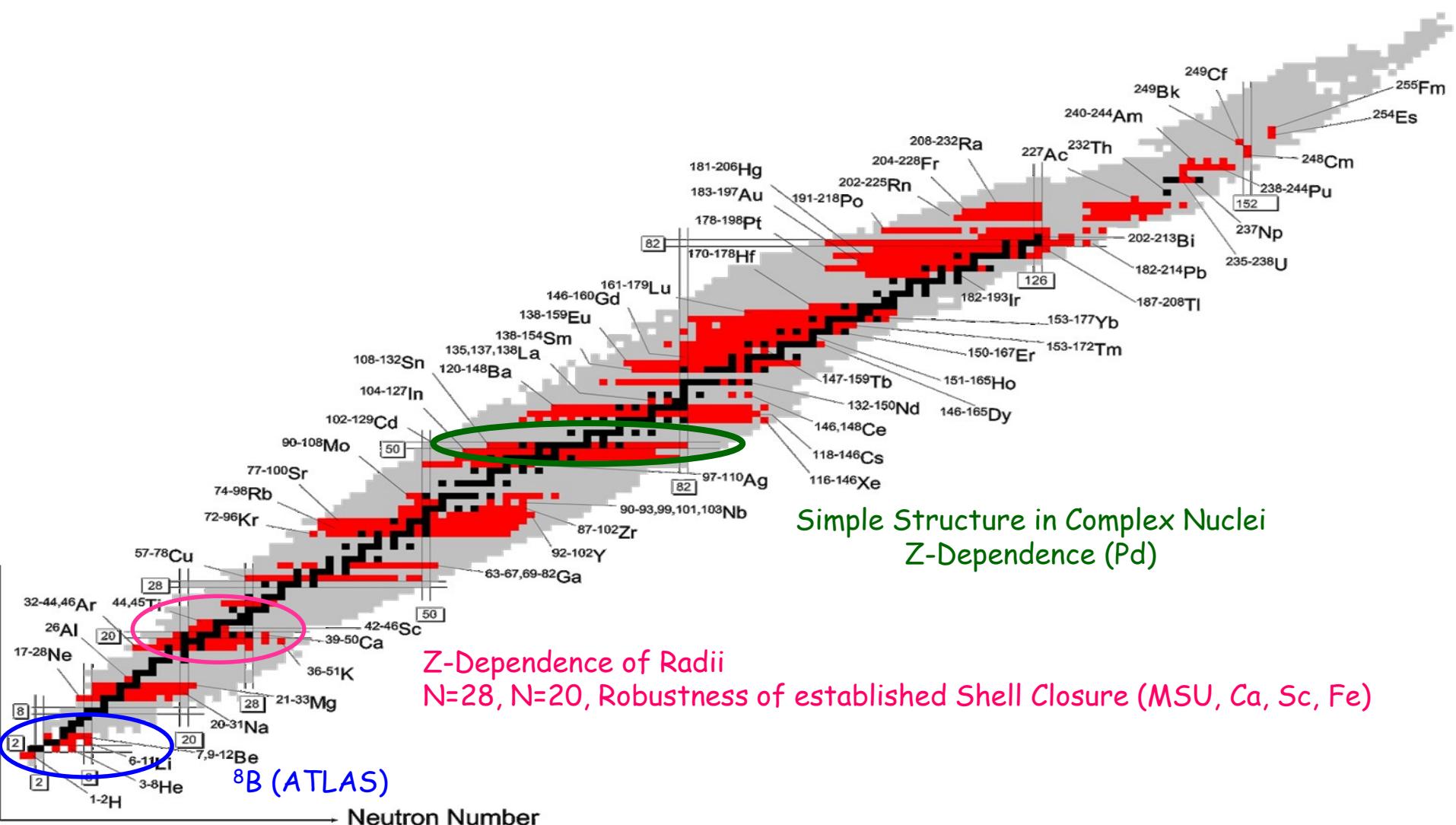
Unexpectedly large charge radii of neutron-rich calcium isotopes

R. F. Garcia Ruiz, M. L. Bissell, K. Blaum, A. Ekström, N. Frömmgen, G. Hagen, M. Hammen, K. Hebler, J. D. Holt, G. R. Jansen, M. Kowalska, K. Kreim, W. Nazarewicz, R. Neugart, G. Neyens, W. Nörtershäuser, T.

Recent Laser Spectroscopic Work on Ground State Properties



TECHNISCHE
UNIVERSITÄT
DARMSTADT



VOLUME 69, NUMBER 14

PHYSICAL REVIEW LETTERS

5 OCTOBER 1992

Proton Halo of ${}^8\text{B}$ Disclosed by Its Giant Quadrupole Moment

T. Minamisono,⁽¹⁾ T. Ohtsubo,⁽¹⁾ I. Minami,⁽¹⁾ S. Fukuda,⁽¹⁾ A. Kitagawa,^{(1),(a)} M. Fukuda,⁽¹⁾ K. Matsuta,⁽¹⁾ Y. Nojiri,⁽¹⁾ S. Takeda,⁽²⁾ H. Sagawa,⁽³⁾ and H. Kitagawa⁽⁴⁾

⁽¹⁾Department of Physics, and Laboratory of Nuclear Studies, Faculty of Science, Osaka University, 1-1 Machikaneyama, Toyonaka, Osaka 560, Japan

⁽²⁾Department of Chemistry, Faculty of Science, Osaka University, 1-1 Machikaneyama, Toyonaka, Osaka 560, Japan

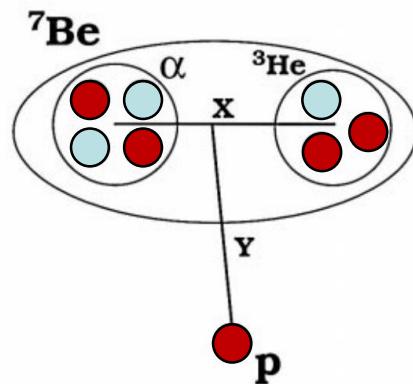
⁽³⁾Department of Physics, Faculty of Science, The University of Tokyo, 7-3-1 Hongo 7-3-1, Bunkyo, Tokyo 113, Japan

⁽⁴⁾Research Center for Nuclear Physics, Osaka University, 10-1 Mihogaoka, Ibaraki, Osaka 567, Japan

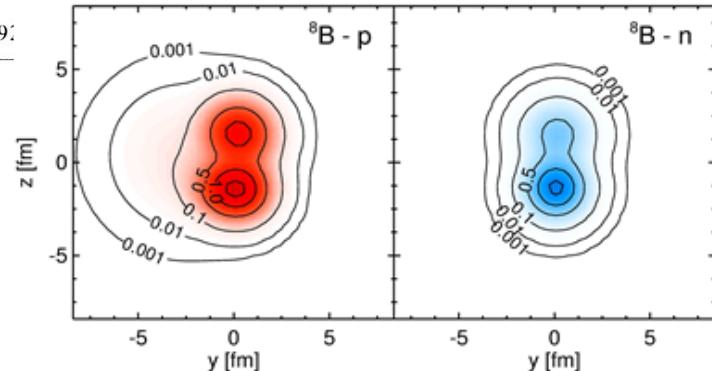
(Received 29 May 1992)

The quadrupole moment of the ${}^8\text{B}$ ($I^\pi=2^+$, $T_{1/2}=769$ msec) nucleus was measured as $|Q({}^8\text{B})|=68.3 \pm 2.1$ mb by use of modified β -NMR. This value is twice as large as the prediction of the Cohen-Kurath shell model. It is found by subtracting the contribution of deeply bound neutrons that the protons in ${}^8\text{B}$ carry more than 90% of the observed moment. The anomalous value is accounted for fairly well by the proton halo due to the loosely bound valence configuration. This is the first experimental evidence for the existence of a proton halo covering a neutron core.

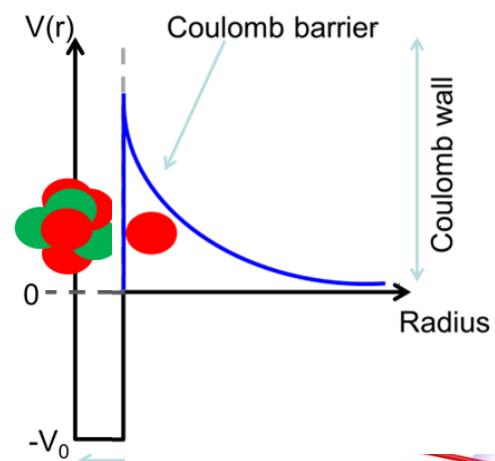
PACS numbers: 21.10.Ky, 21.10.Ft, 27.20.+n



M.H. Smedberg *et al.*, Physics Letters B 452 1999 1-7



FMD Model calculation (T. Neff, GSI)



Isotope Shift Measurement: The Challenge of Light Isotopes



TECHNISCHE
UNIVERSITÄT
DARMSTADT

$$\delta\nu_{IS} = \delta\nu_{MS} + \delta\nu_{FS}$$

$$F_{el} \delta\langle r_c^2 \rangle$$

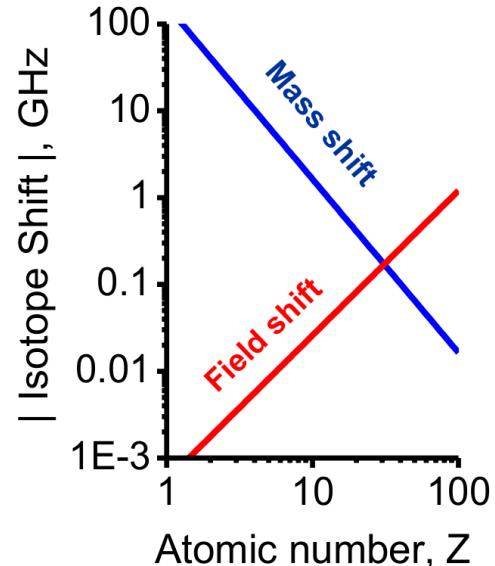
||

Theory: Accuracy of ~100kHz

$$\delta\nu_{MS} \approx 35 \text{ GHz}$$

$$\delta\nu_{FS} \approx 10 \text{ MHz/fm}^2$$

$$R_c({}^8\text{B}) = \sqrt{R_c^2({}^{11}\text{B}) + \delta\langle r_c^2 \rangle^{11,8}}$$



What we need now:

- suitable transitions in boron
- boron source
- laser spectroscopy



Charge Radii of Light Isotopes



Measure !

Calculate

$$\delta\nu_{\text{IS}}^{AA'} = K_{\text{MS}} \cdot \frac{M_{A'} - M_A}{M_A M_{A'}}$$

+

Calculate

$$\frac{2\pi Ze}{3} \Delta |\Psi(0)|^2$$

Get !

$$\delta \langle r^2 \rangle^{AA'}$$

${}^{8,4}\text{He}$, $2\ 3S_1 \rightarrow 3\ 3P_2$ 64 702.5086(9) MHz

${}^{11,6}\text{Li}$, $2s \rightarrow 3s$ 36 554.323(9) MHz

${}^{11,9}\text{Be}^+$, $2s_{1/2} \rightarrow 2p_{1/2}$ 31 560.294(24) MHz

1.008 MHz/fm²

1.570 MHz/fm²

17.02 MHz/fm²

Yan & Drake, PRA 61, 022504 (2000)

Puchalski & Pachucki PRA 78,058512 (2008)

W. Nörtershäuser et al. PRA 83, 012516 (2011)

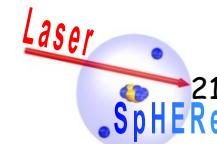
(1) Precise Solution of Nonrelativistic Schrödinger
Equation with Fully Correlated Wavefunctions

(2) Relativistic Corrections

(3) QED Corrections

(4) Nuclear Polarizability

$N_e \leq 3 !!$



Absolute Nuclear Charge Radii

$$R_c(^{A'}\text{Li}) = \sqrt{R_c^2(^A\text{Li}) + \delta \langle r_c^2 \rangle^{A,A'}}.$$



Laser Spectroscopy
Isotope Shift
Model independent !

Elastic Electron Scattering

${}^4\text{He}$: 1.681 (4) fm,

${}^6\text{Li}$: 2.589 (39) fm

${}^9\text{Be}$: 2.519 (12) fm

${}^{10}\text{B}$: 2.45(12), 2.58(5)

A01: Improve absolute charge radii by elastic electron scattering at S-DALINAC.

New Perspectives: Four-Electron Systems



PHYSICAL REVIEW A 89, 012506 (2014)



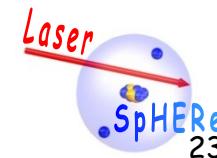
Isotope shift in a beryllium atom

Mariusz Puchalski,^{1,*} Krzysztof Pachucki,² and Jacek Komasa¹

TABLE III. Contributions to the ^{11}Be – ^9Be isotope shift of the $3^1\text{S} - 2^1\text{S}$, $2^1\text{P} - 2^1\text{S}$ transition and ionization potential IP(2^1S) in MHz, with exclusion of the finite-size correction. The second uncertainty of $\Delta\nu_{\text{ms}}^{\text{the}}$ is due to the atomic mass. The nucleus polarizability $\tilde{\alpha}_{\text{pol}}(^{11}\text{Be}) = 6.90(69) \times 10^{-7} \text{ m}^{-3}$ [11], $\tilde{\alpha}_{\text{pol}}(^9\text{Be}) = 2.90(29) \times 10^{-7} \text{ m}^{-3}$ [35].

Contribution	$3^1\text{S} - 2^1\text{S}$	$2^1\text{P} - 2^1\text{S}$	IP(2^1S)
$\Delta\nu^{(2,1)}$	18 907.131(15)	16 020.271(15)	25 558.619(2)
$\Delta\nu^{(2,2)}$	-3.198 2(5)	2.178 8(1)	-5.474 2
$\Delta\nu^{(4,1)}$	2.46(3)	-8.013(12)	3.604(2)
$\Delta\nu^{(5,1)}$	-0.135(4)	0.819(6)	-0.209(2)
$\Delta\nu^{(6,1)}$	-0.041(20)	-0.034(17)	-0.048(24)
$\Delta\nu_{\text{pol}}$	0.034(3)	0.066(7)	0.037(4)
$\Delta\nu_{\text{ms}}^{\text{the}}$	18 906.25(4)(1)	16 015.29(3)(1)	25 556.53(3)(1)
$C(\text{MHz}/\text{fm}^2)$	-4.772(8)	-9.334(16)	-5.225(9)

→ charge radius of ^{14}Be ,
 → $^{10,12,14}\text{Be}$ charge radii from 2nd transition



Now even 5-Electron Systems in Reach



TECHNISCHE
UNIVERSITÄT
DARMSTADT

PHYSICAL REVIEW A 92, 062501 (2015)



Explicitly correlated wave function for a boron atom

Mariusz Puchalski,¹ Jacek Komasa,¹ and Krzysztof Pachucki²

¹*Faculty of Chemistry, Adam Mickiewicz University, Umultowska 89b, 61-614 Poznań, Poland*

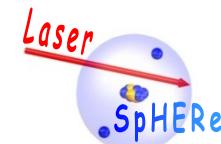
²*Faculty of Physics, University of Warsaw, Pasteura 5, 02-093 Warsaw, Poland*

(Received 22 October 2015; published 4 December 2015)

We present results of high-precision calculations for a boron atom's properties using wave functions expanded in the explicitly correlated Gaussian basis. We demonstrate that the well-optimized 8192 basis functions enable a determination of energy levels, ionization potential, and fine and hyperfine splittings in atomic transitions with nearly parts per million precision. The results open a window to a spectroscopic determination of nuclear properties of boron including the charge radius of the proton halo in the ^8B nucleus.

DOI: [10.1103/PhysRevA.92.062501](https://doi.org/10.1103/PhysRevA.92.062501)

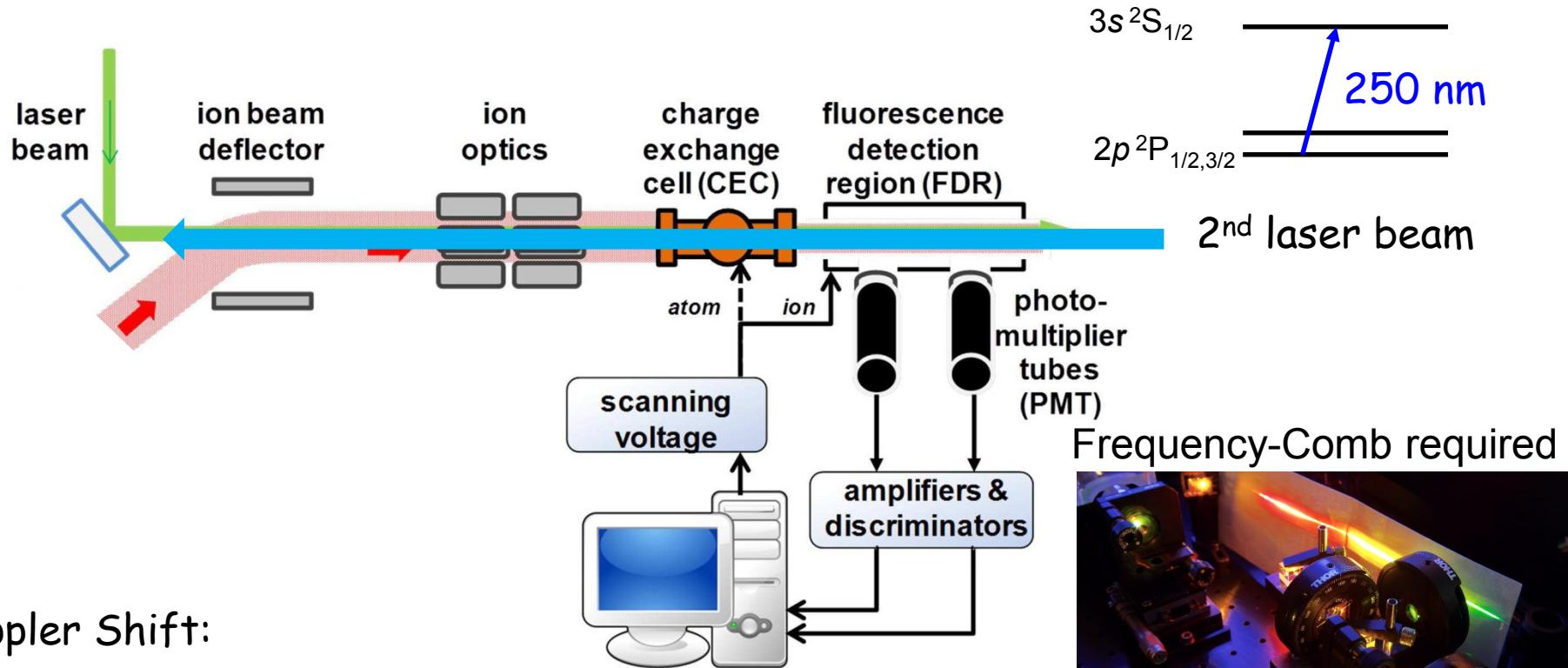
PACS number(s): 31.15.ac, 31.30.J–



Simplified Setup for ${}^8\text{B}$ Spectroscopy



TECHNISCHE
UNIVERSITÄT
DARMSTADT

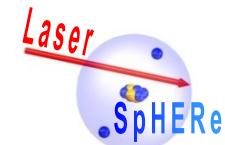
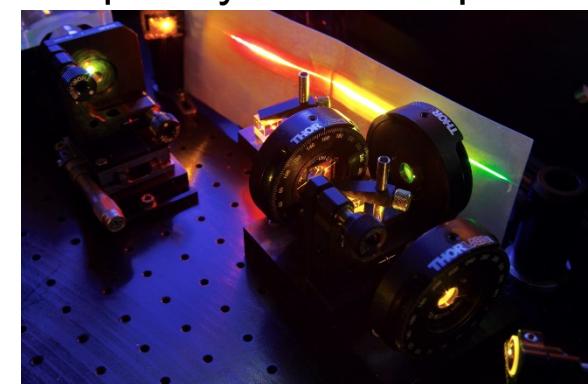


Doppler Shift:

$$\nu_c = \nu_0 \cdot \gamma \cdot (1 + \beta)$$

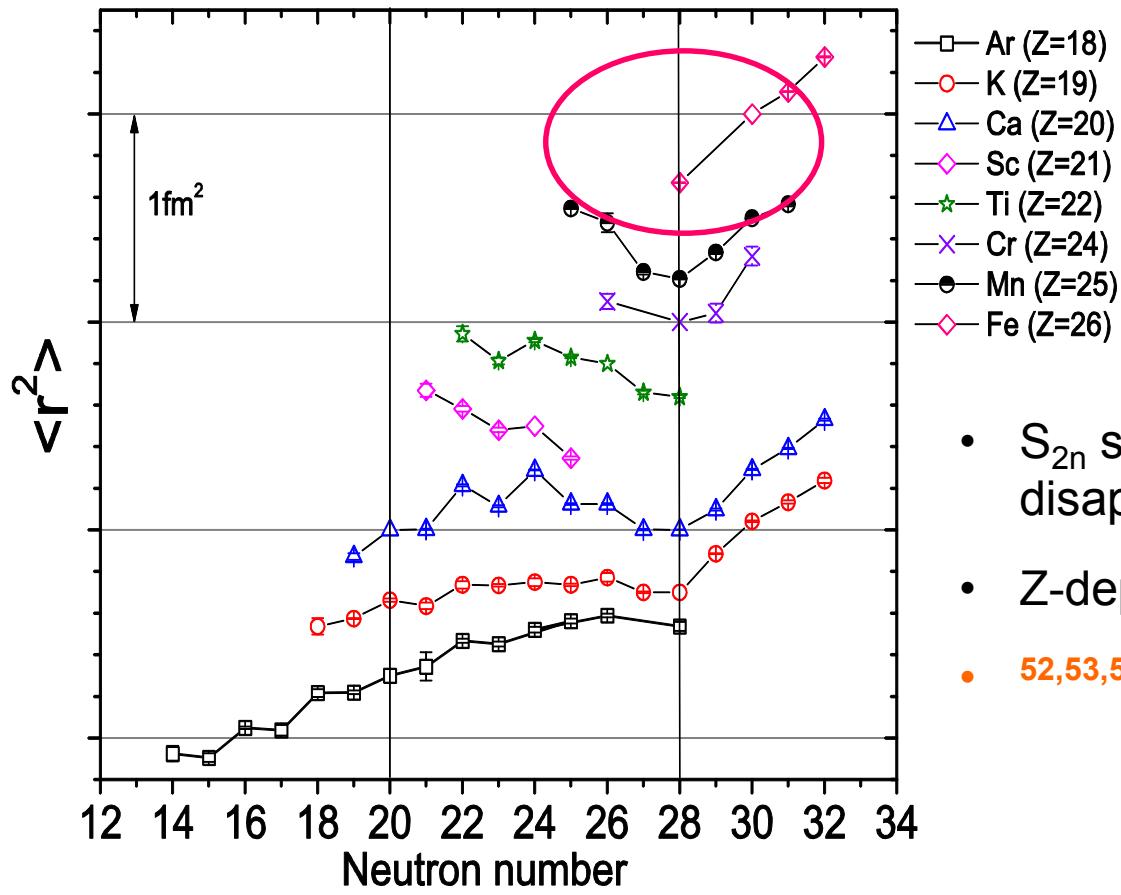
$$\nu_a = \nu_0 \cdot \gamma \cdot (1 - \beta)$$

$$\nu_a \cdot \nu_c = \nu_0^2$$

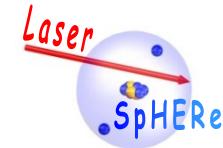


N=28: Moments and Charge radii of Fe

Charge radii and magnetic moments from collinear laser spectroscopy ◀ A01



- S_{2n} signature of shell closure at $N = 28$ disappears at $Z = 24$
- Z-dependence of the $N = 28$ shell closure
- **52,53,55Fe** at BECOLA/NSCL

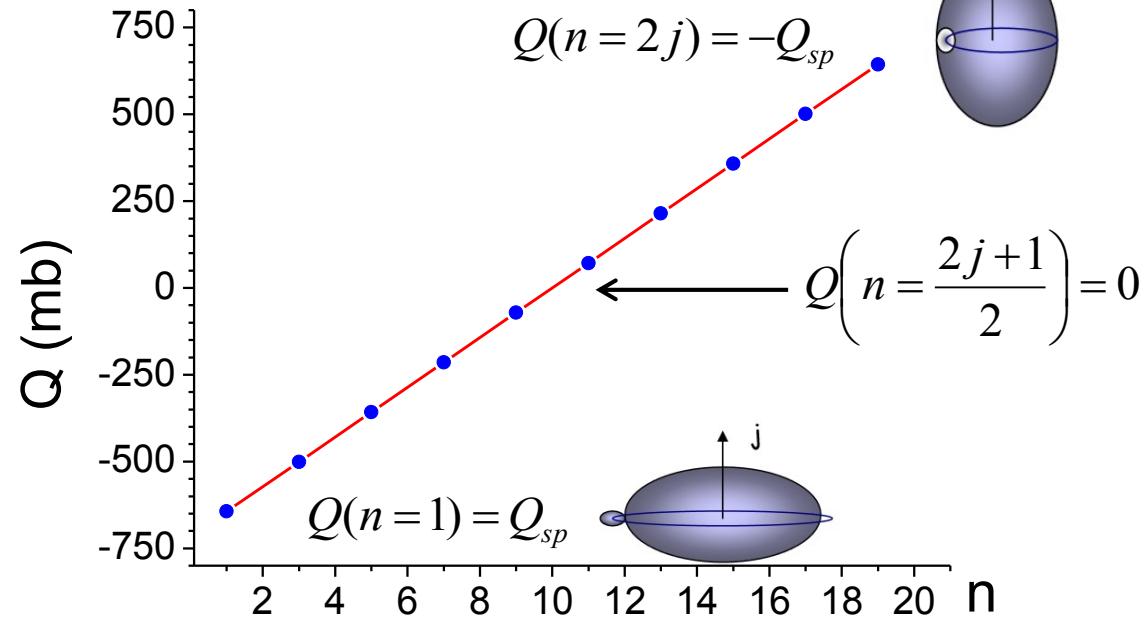


Quadrupole Moments of Pd 11/2 Isomers - Motivation



$$Q_{sp} = -e^{\text{eff}} \frac{2j-1}{2j+2} \langle r_j^2 \rangle$$

$$Q(n) = Q_{sp} \left(\frac{2j+1-2n}{2j-1} \right)$$



- slope determined by Q_{sp}
- single neutron \rightarrow oblate deformation ($Q < 0$)
- single neutron hole \rightarrow prolate deformation ($Q > 0$)

Extraction of Q_{sp} :

$$Q_{sp} = \frac{Q(n=1) - Q(n=2j)}{2}$$

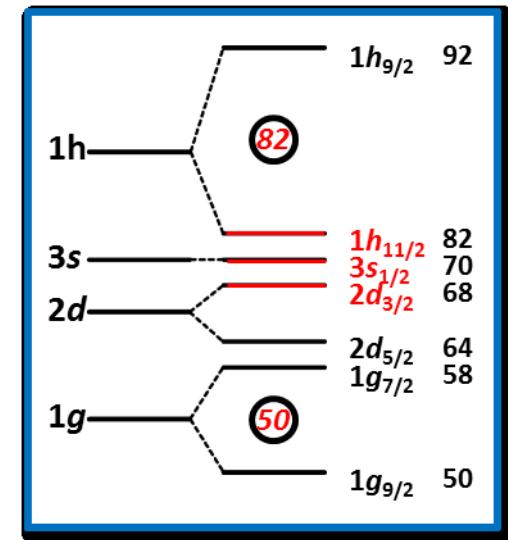
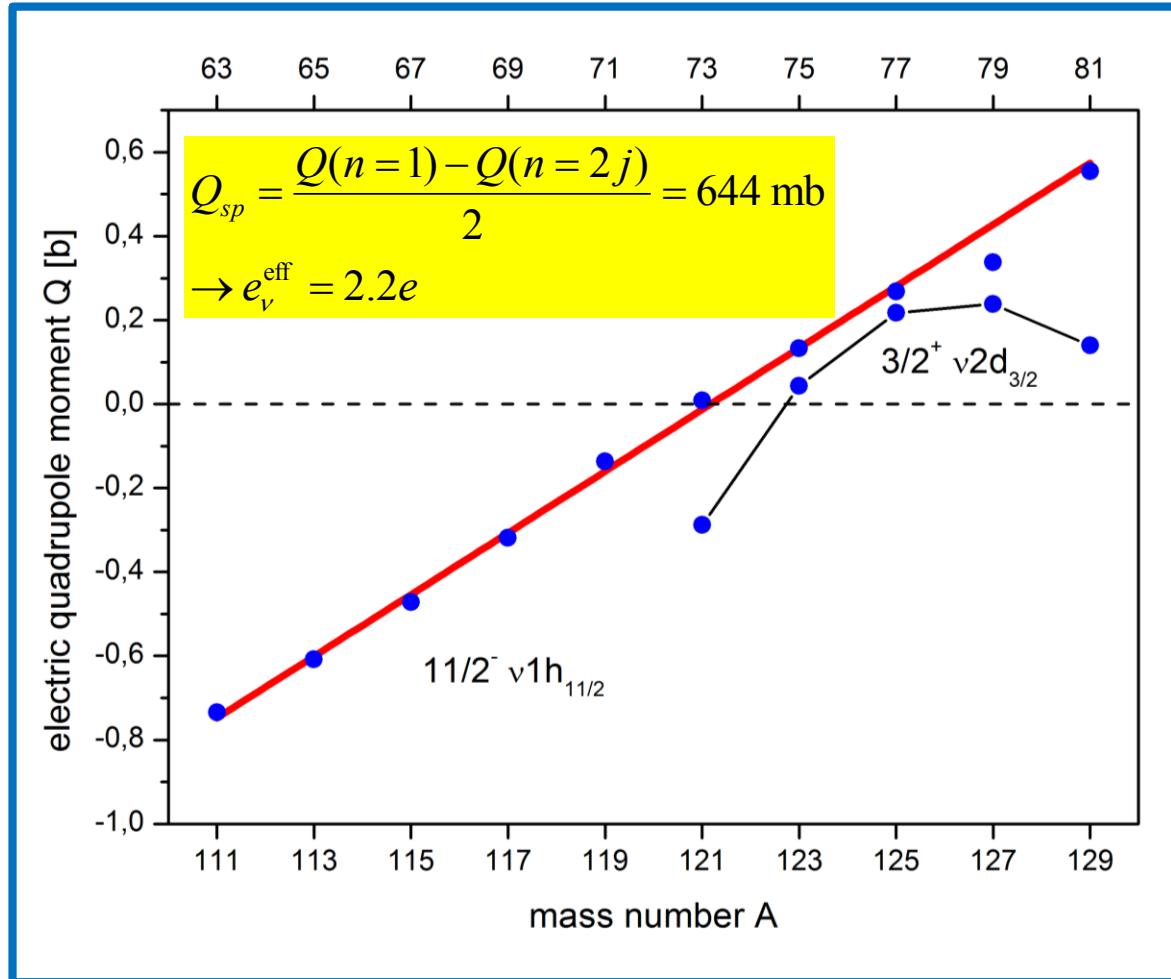


A03: Research plan

Quadrupole Moments of Pd 11/2 Isomers - Motivation



TECHNISCHE
UNIVERSITÄT
DARMSTADT



Capacity of $1h_{11/2}$ niveau:
12 neutrons
 \rightarrow 6 quad. moments
But: 10 quad. moments

Neutron pairs shared
between the neighboring
levels.

D. T. Yordanov et al., Phys. Rev. Lett. **110**, 192501 (2013)

→ Check for Z=46 (Palladium, Pd)



Summary

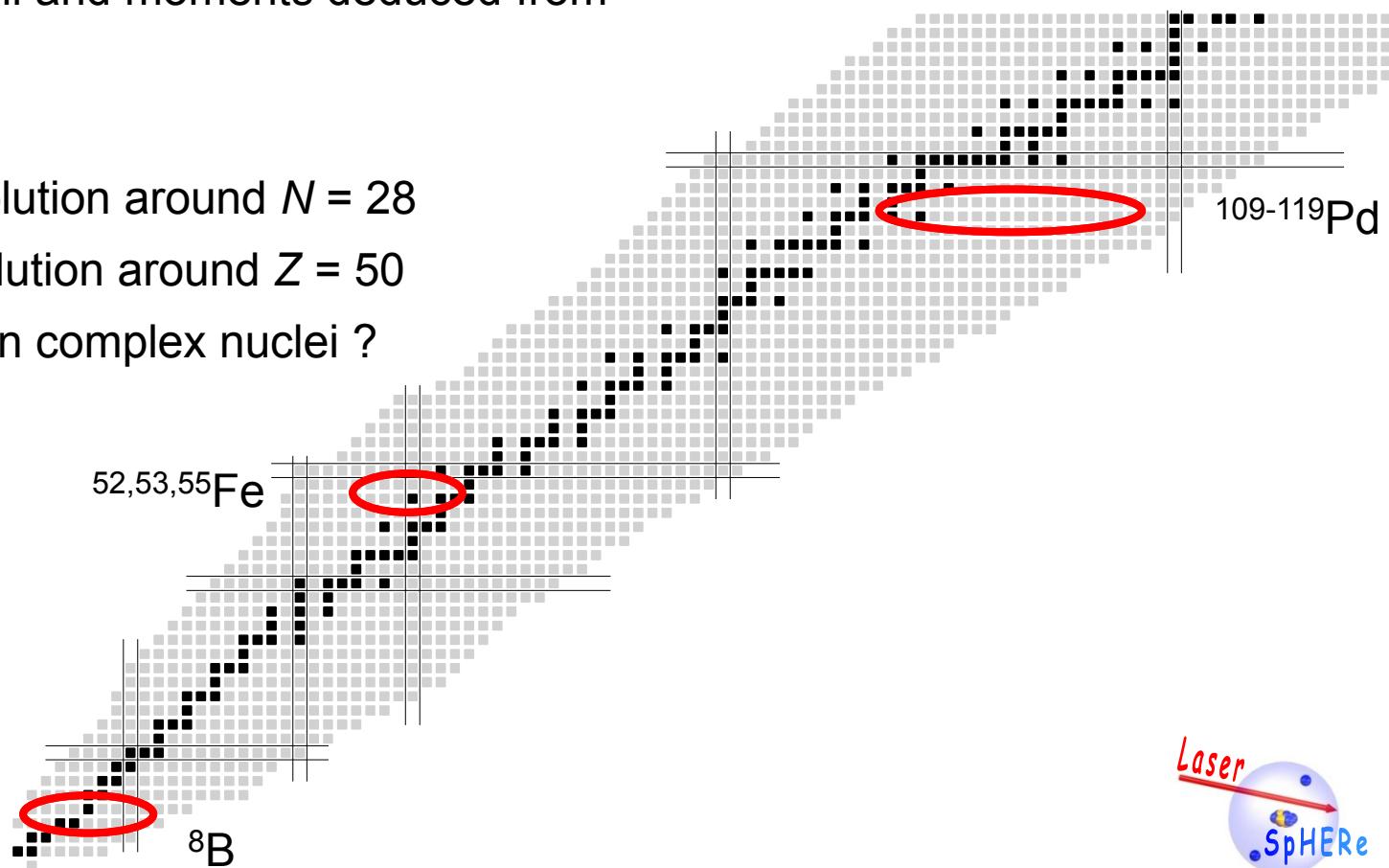


A01
A03

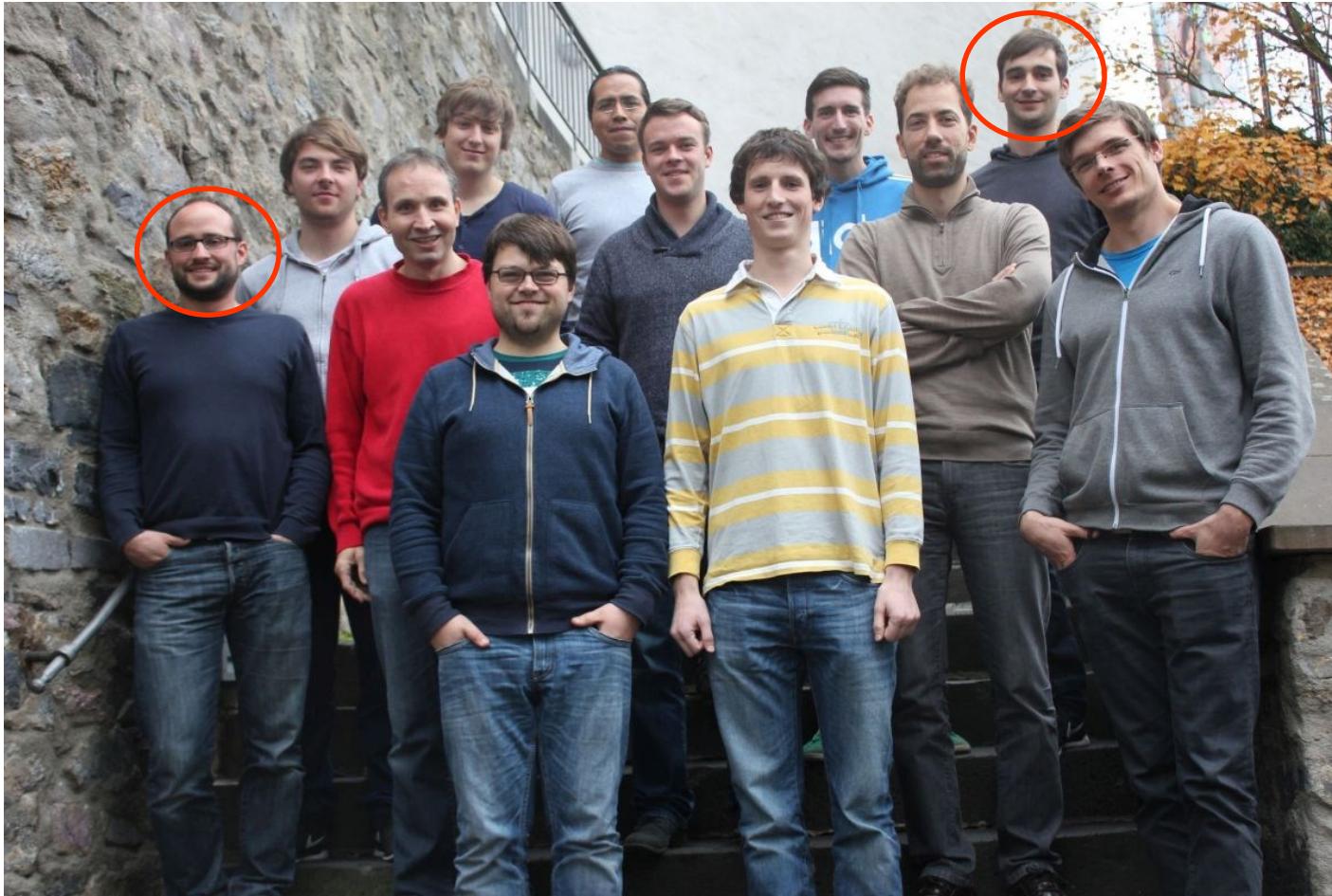
Key experiments on electromagnetic observables using laser spectroscopy

Nuclear charge radii and moments deduced from
laser spectroscopy

- ${}^8\text{B}$ Proton Halo
- ${}^{52,53,55}\text{Fe}$ shell evolution around $N = 28$
- ${}^{109-119}\text{Pd}$ shell evolution around $Z = 50$
simple structure in complex nuclei ?



Jörg Krämer



Bernhard Maas Involvement in A01/A03



Dominic Rossi
(Tom Aumann's group)