

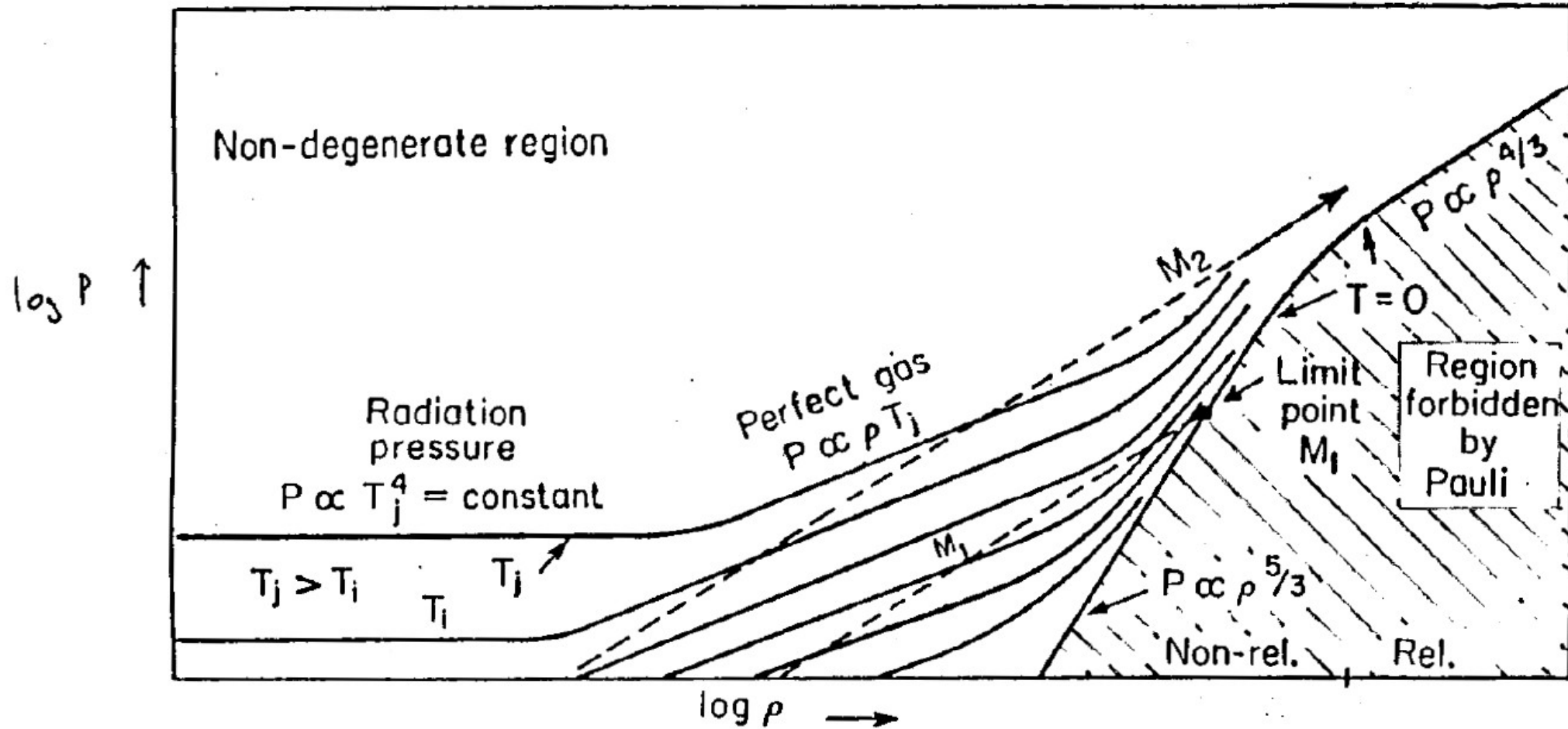


Stellar Evolution  
Course

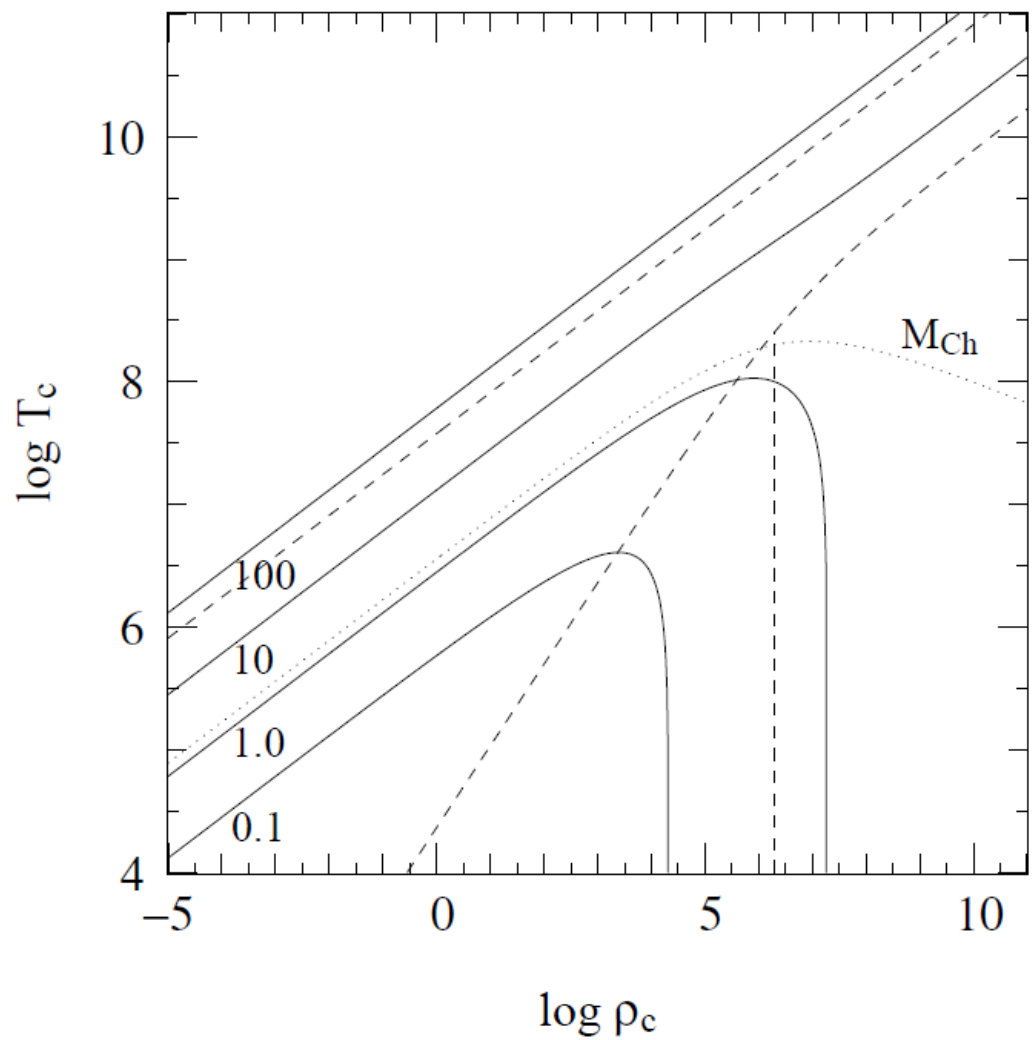
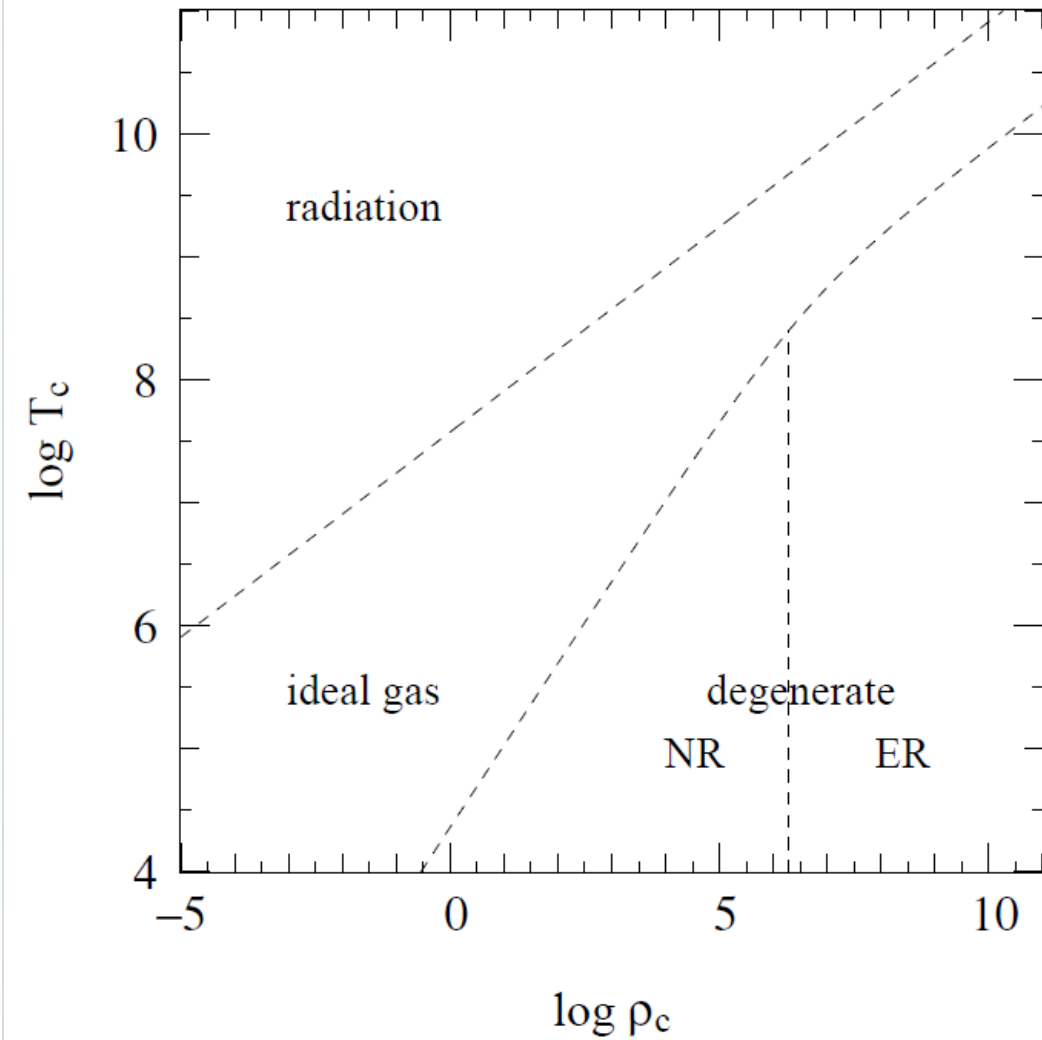
L7: Simple Models & Early Evolution  
&

L8: Late Evolution of  
Intermediate & Low-Mass Stars

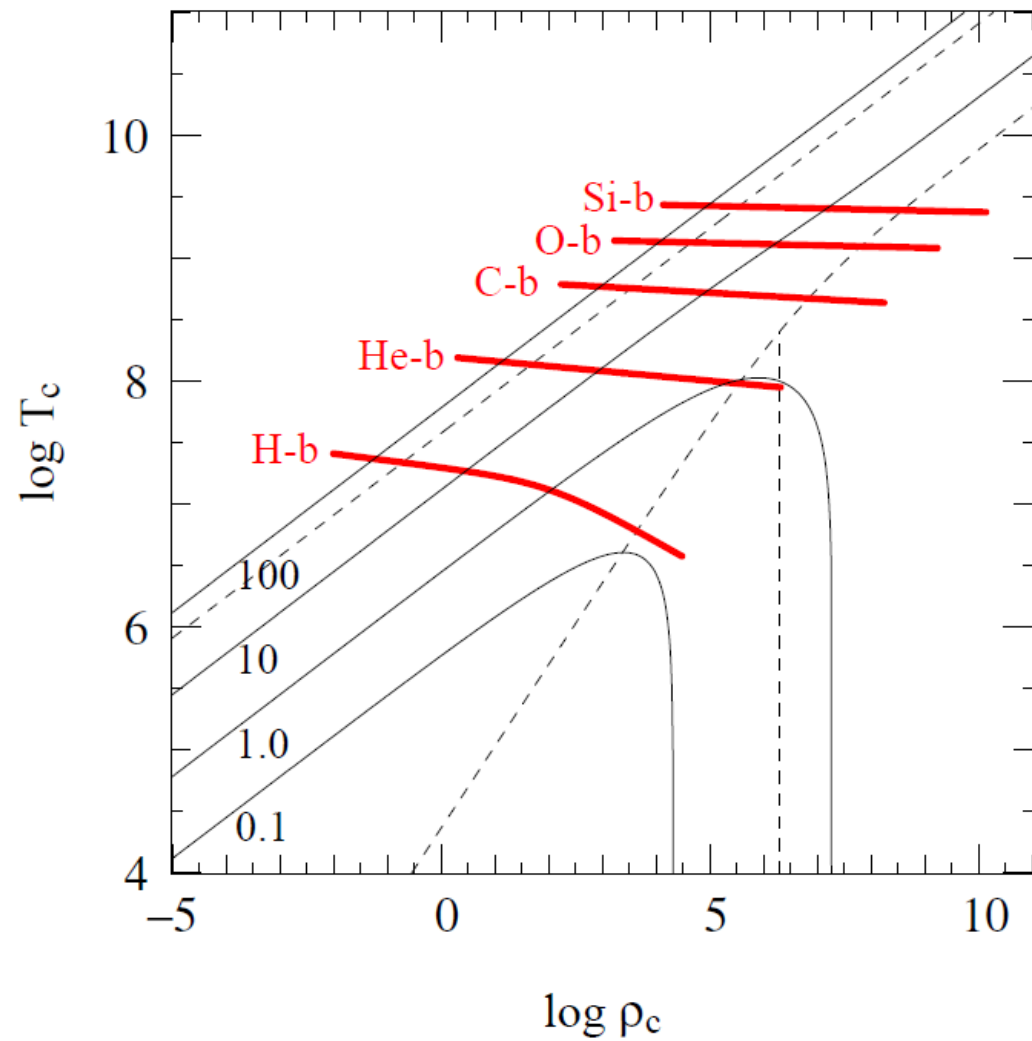
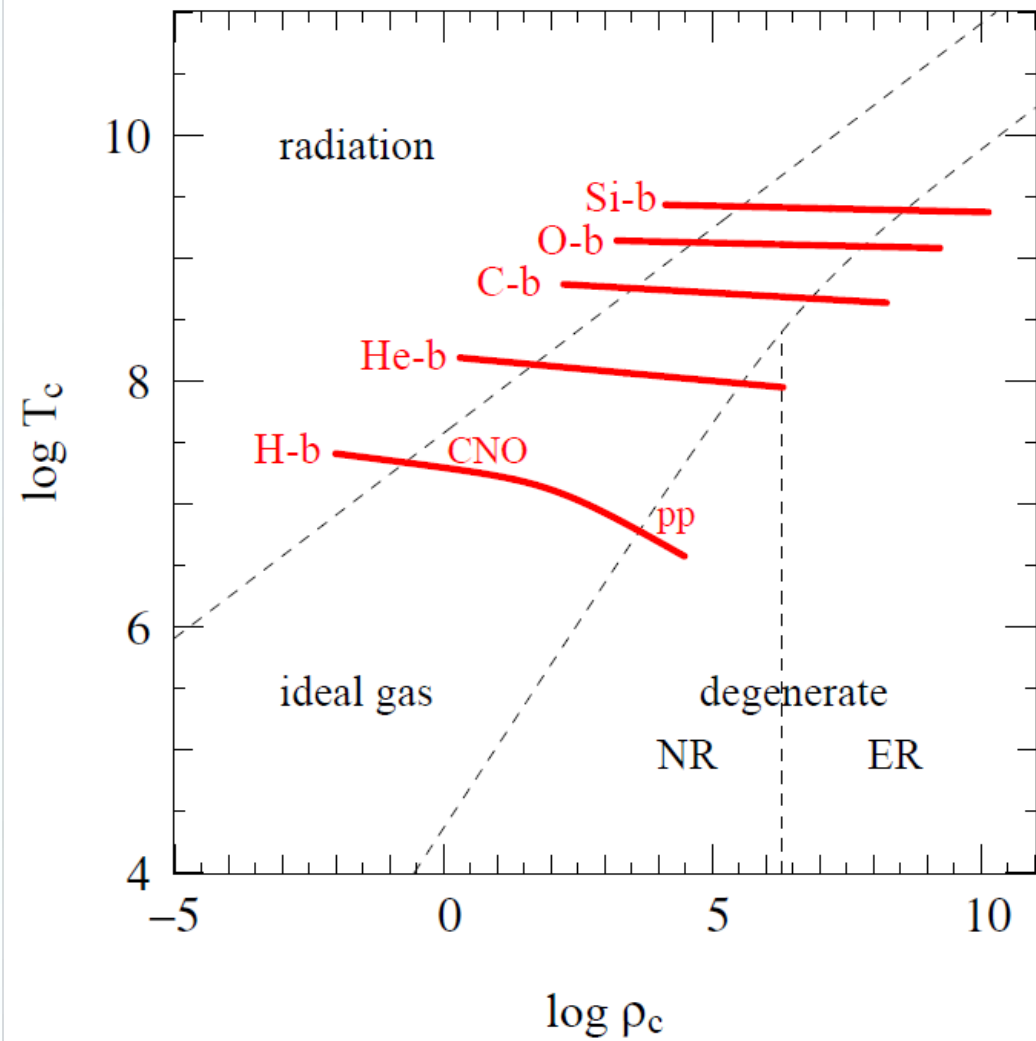
# Schematic Evolution in $P_c - \rho_c$



# Schematic Evolution in $T_c - \rho_c$

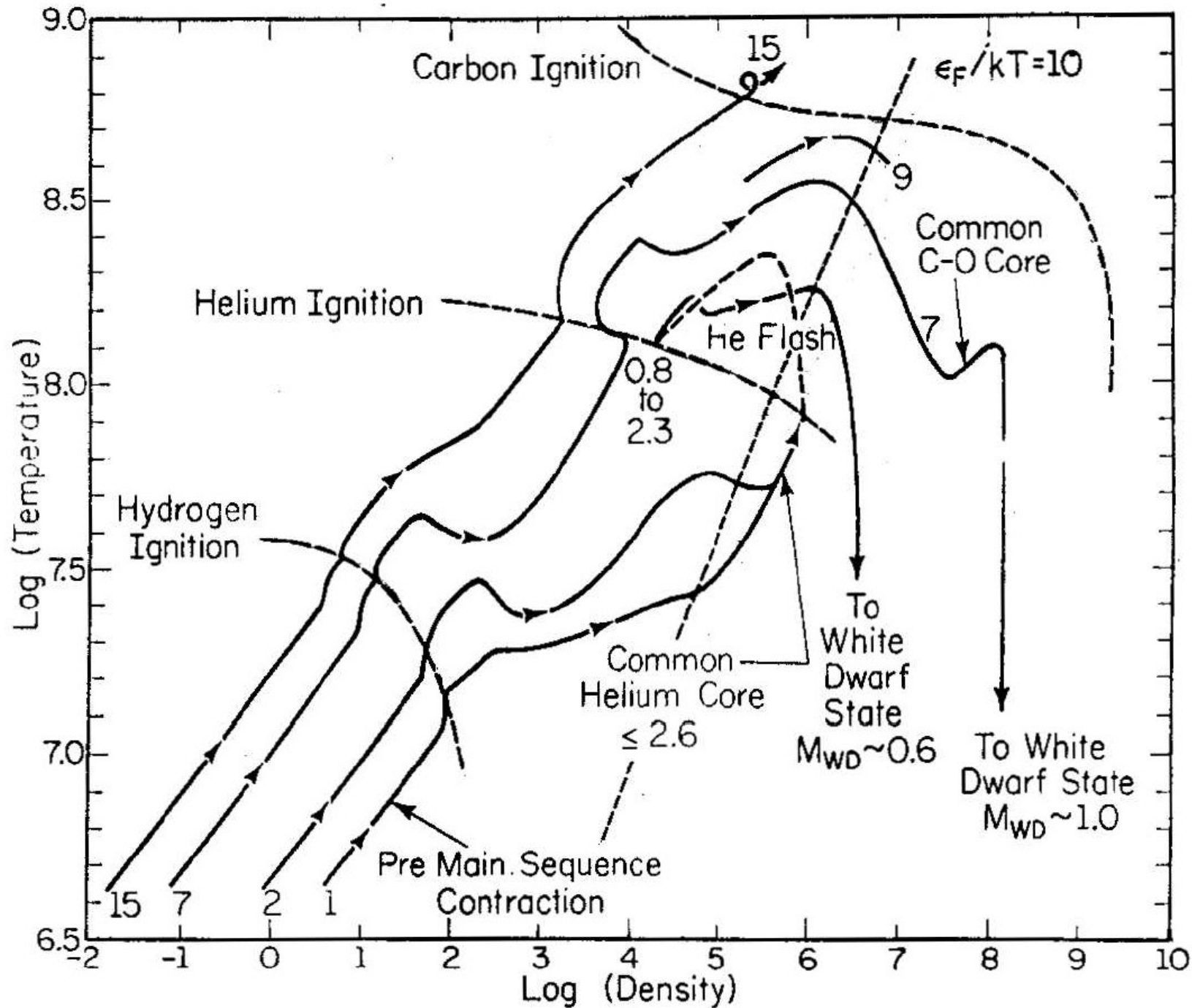


# Schematic Evolution in $T_c - \rho_c$





# Schematic Evolution in $T_c - \rho_c$

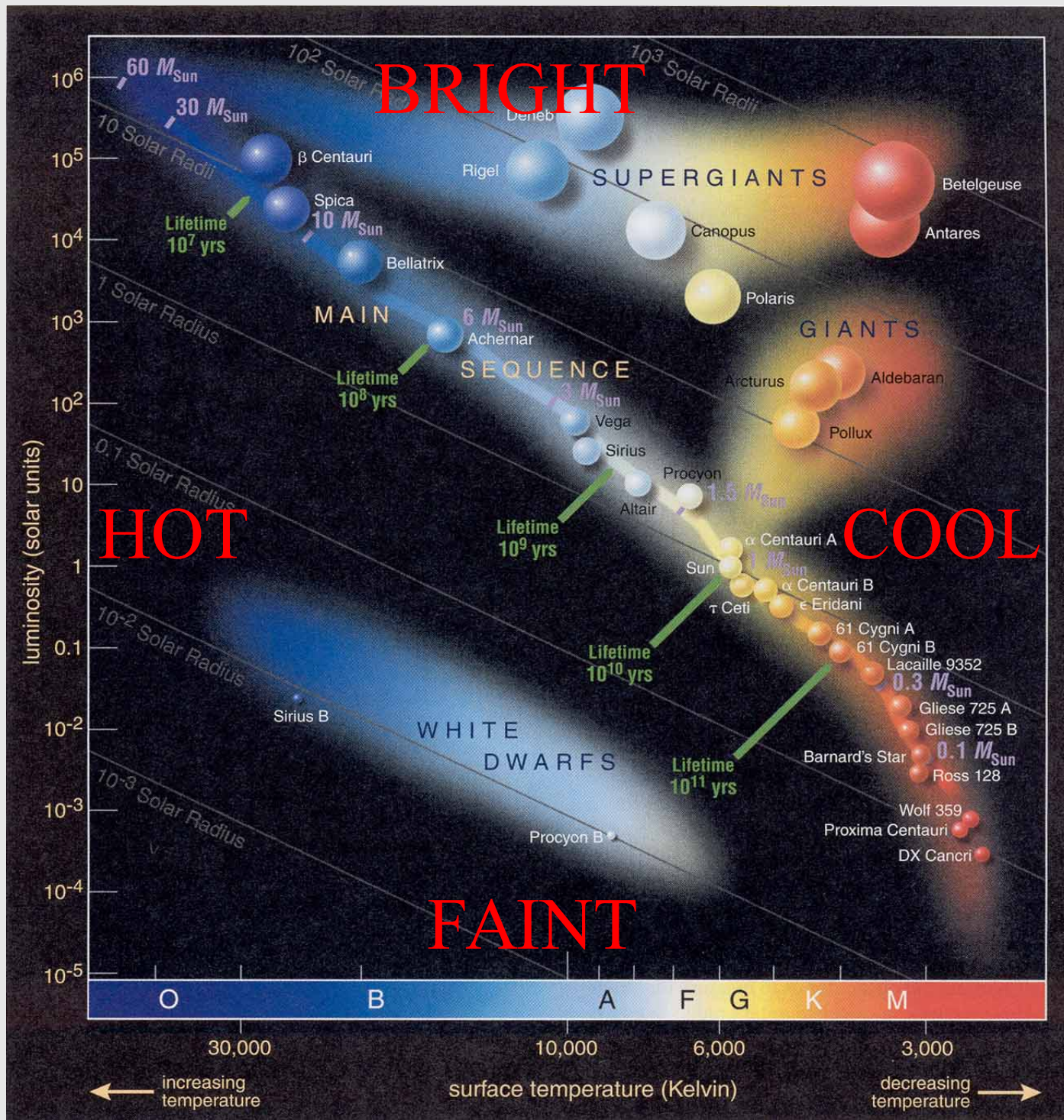


# Mass Domains

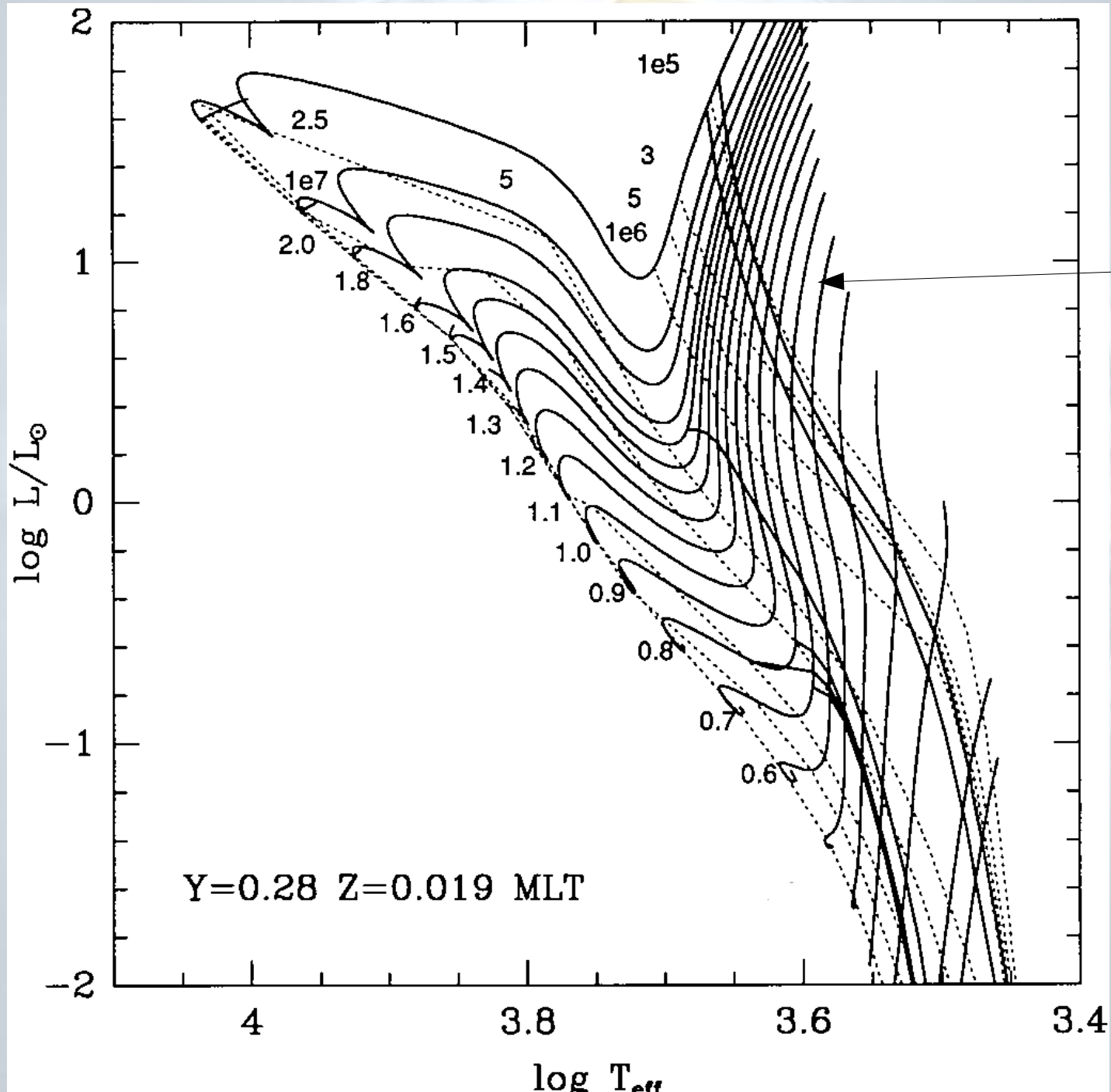
Stars: radiate energy produced internally & are bound by their own gravity

- $0.08 M_{\text{sun}}$  inferior mass limit for core H-burning : **Brown Dwarfs**
- $0.08 M_{\text{sun}} - 0.5M_{\text{sun}}$ : H burning OK, degenerate before core He-burning (lifetime  $>$  Hubble time  $\rightarrow$  no He white dwarf from single stars)
- $0.5-7M_{\text{sun}}$ : core H OK, core He OK (He-flash below  $1.8 M_{\text{sun}}$ ), degenerate CO white dwarf
- $7-9 M_{\text{sun}}$ : Core C burning OK  $\rightarrow$  WD(?) or Complete destruction (?) or collapse through electron captures (?)
- $\sim 9 - 150 M_{\text{sun}}$ : core H, He, C, Ne, O, Si  $\rightarrow$  Fe cores
- $150-250 M_{\text{sun}}$ : Pair Creation/instability Supernovae





# Pre-Main Sequence



Hayashi  
Line  
(fully  
convective)

# Zero-Age MS: $L$ - $M$ & $R$ - $M$ Relations (Homology)

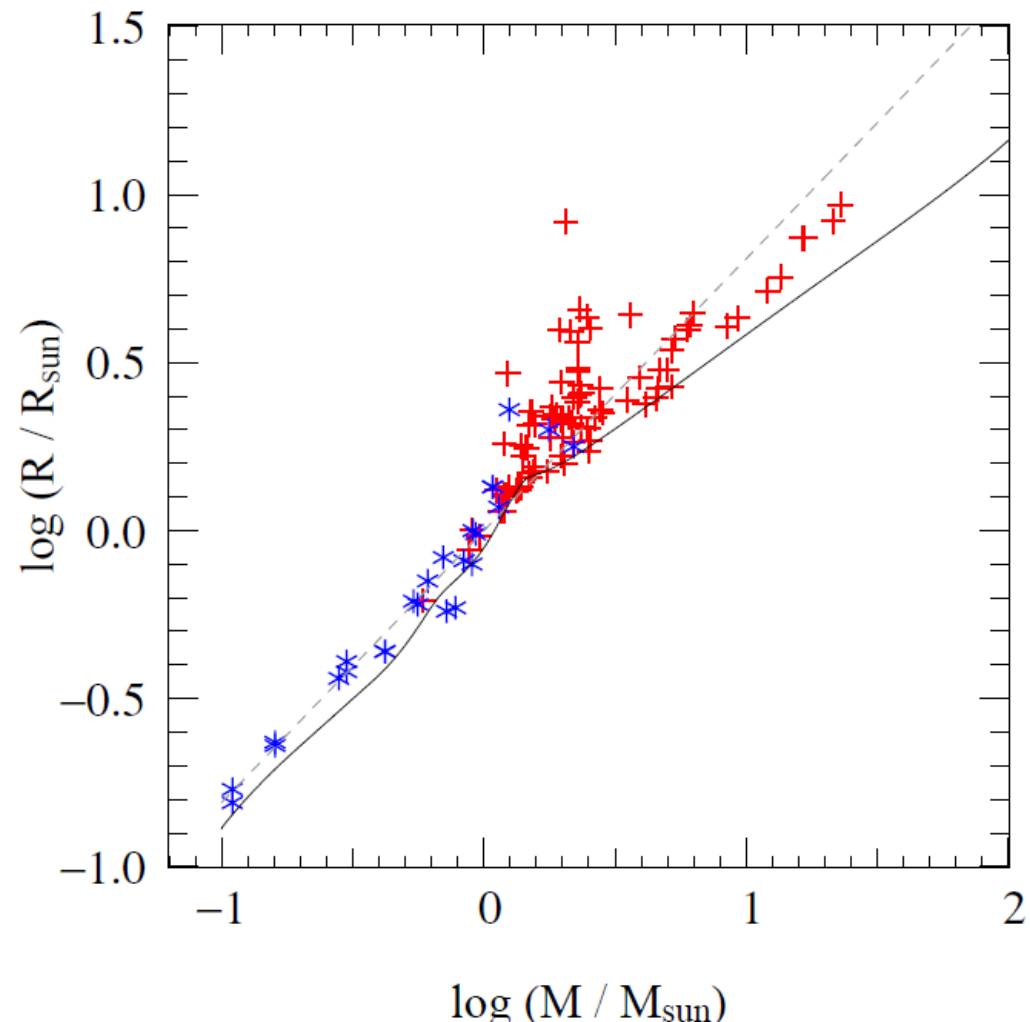
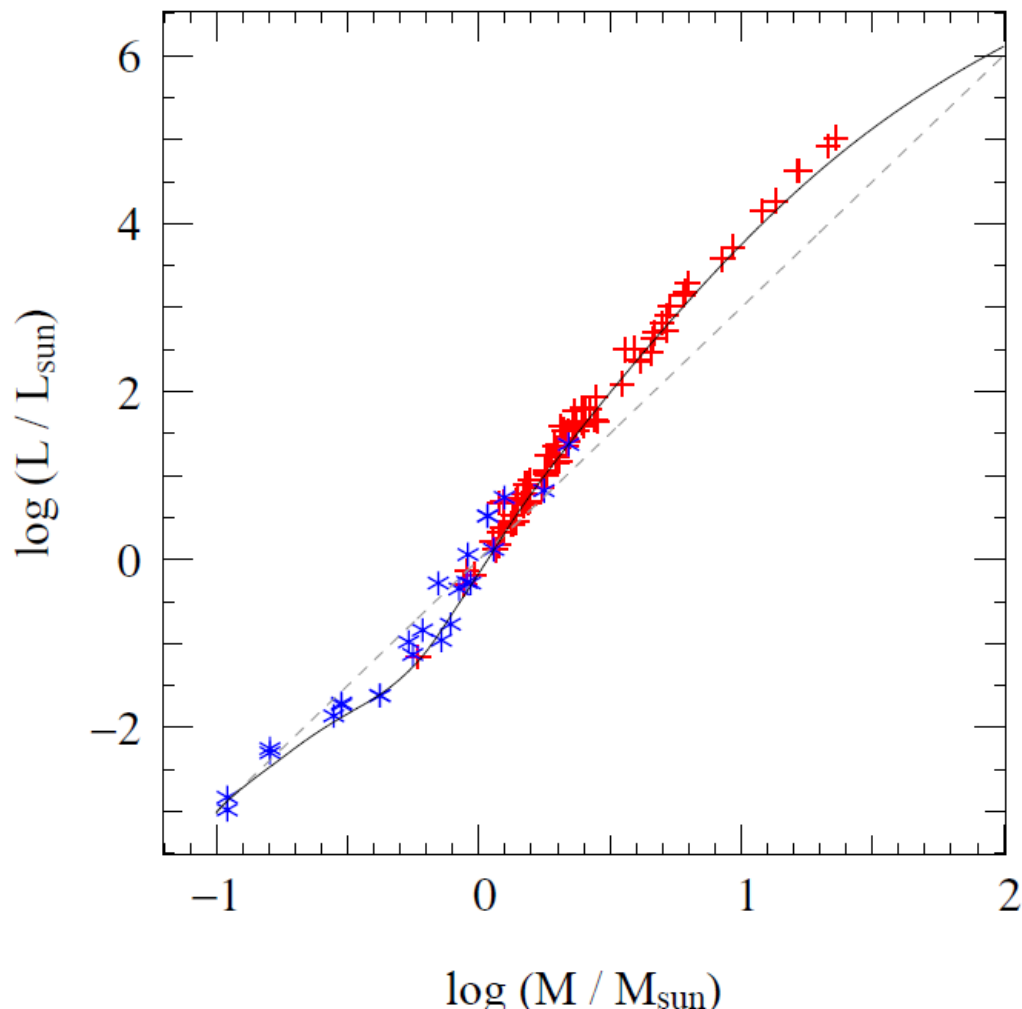
Low-mass stars

$$L \propto \frac{\beta^4 \mu^4 M^3}{\kappa}$$

High-mass stars

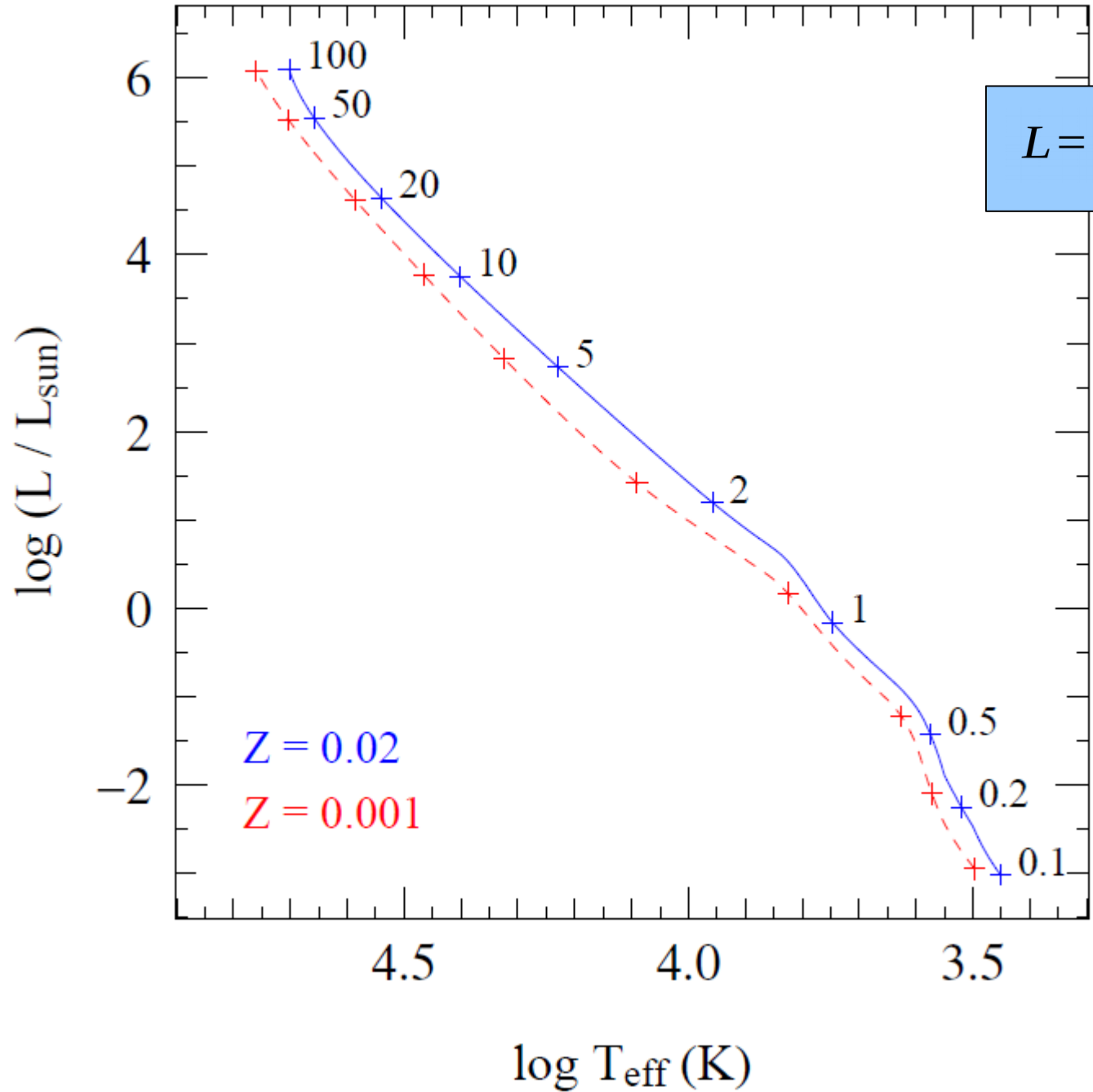
$$L \propto \frac{\mu^4 M}{\kappa}$$

$$R \propto \mu^{\frac{\nu-4}{\nu+3}} M^{\frac{\nu-1}{\nu+3}} .$$



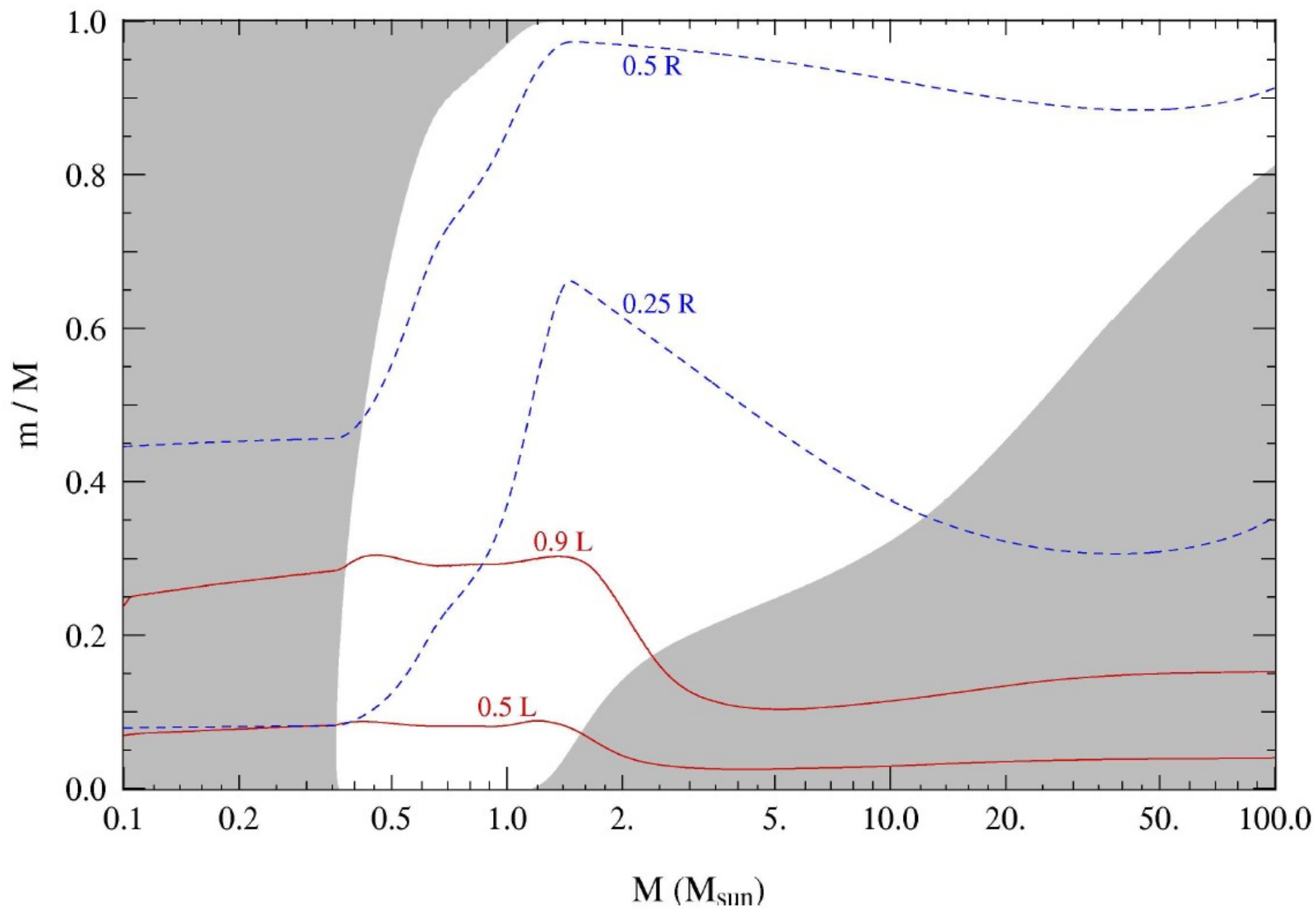


# ZAMS: $L$ - $T_{\text{eff}}$ ( $M$ )

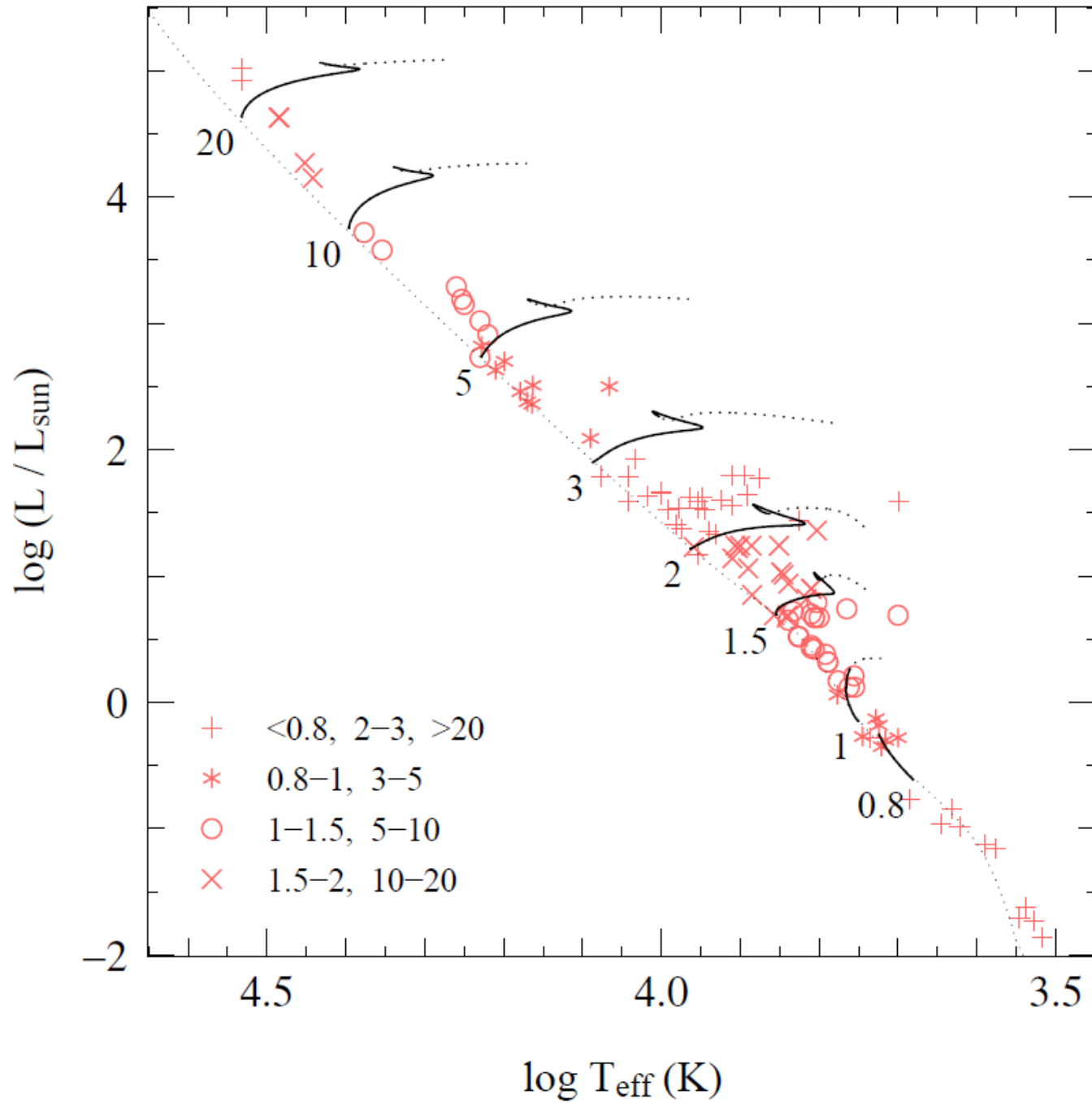




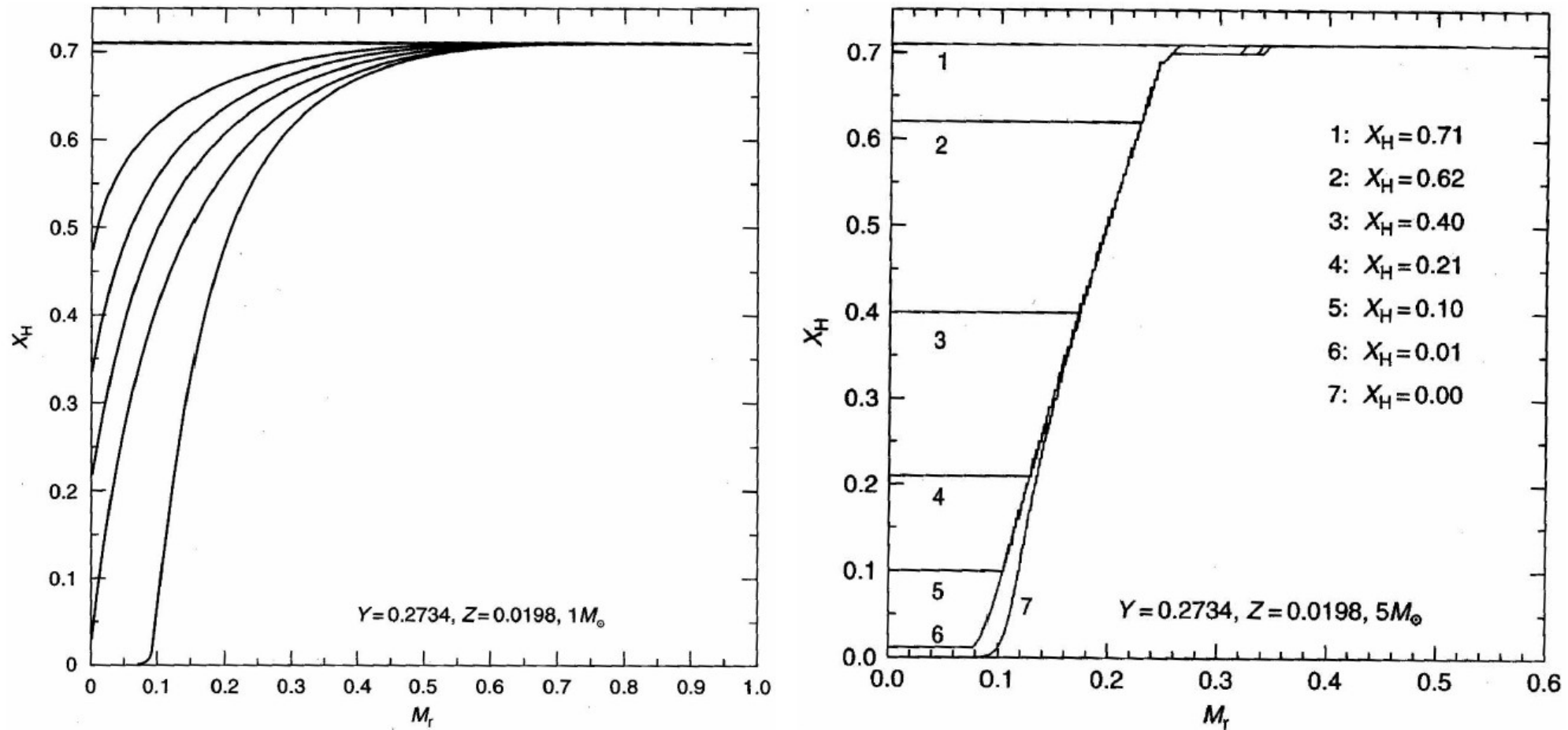
# Convective Regions on ZAMS for Different Masses



# ZAMS $\rightarrow$ TAMS (termination age MS)

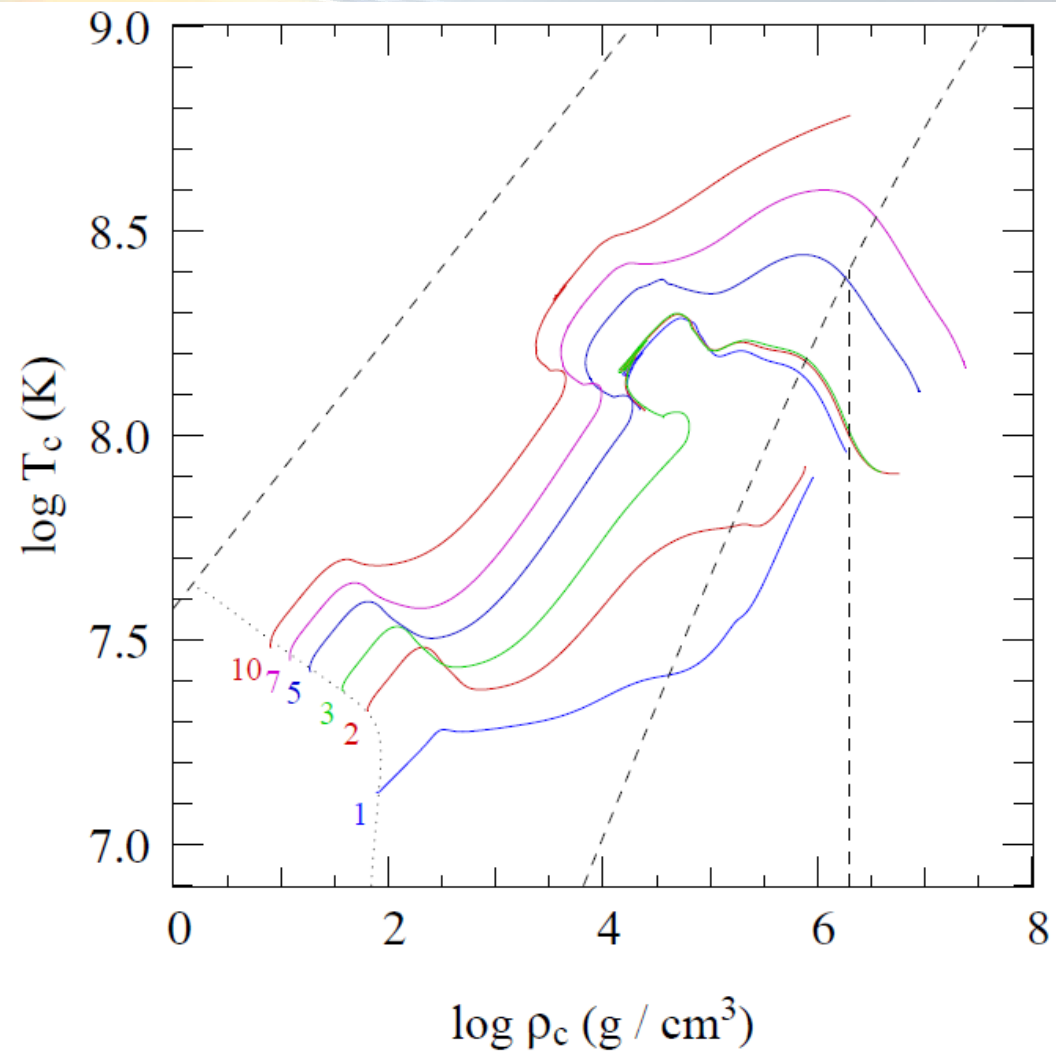
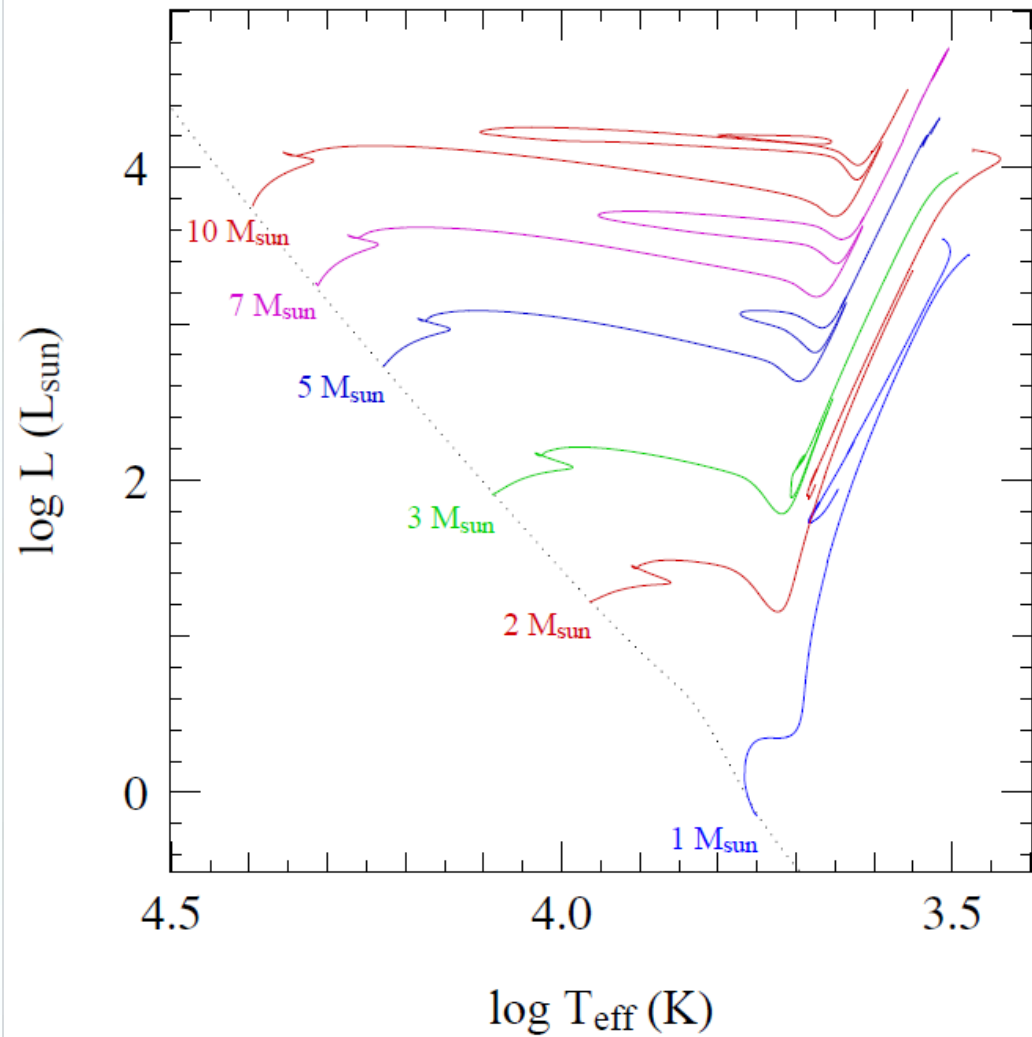


# Evolution of Composition Inside Stars

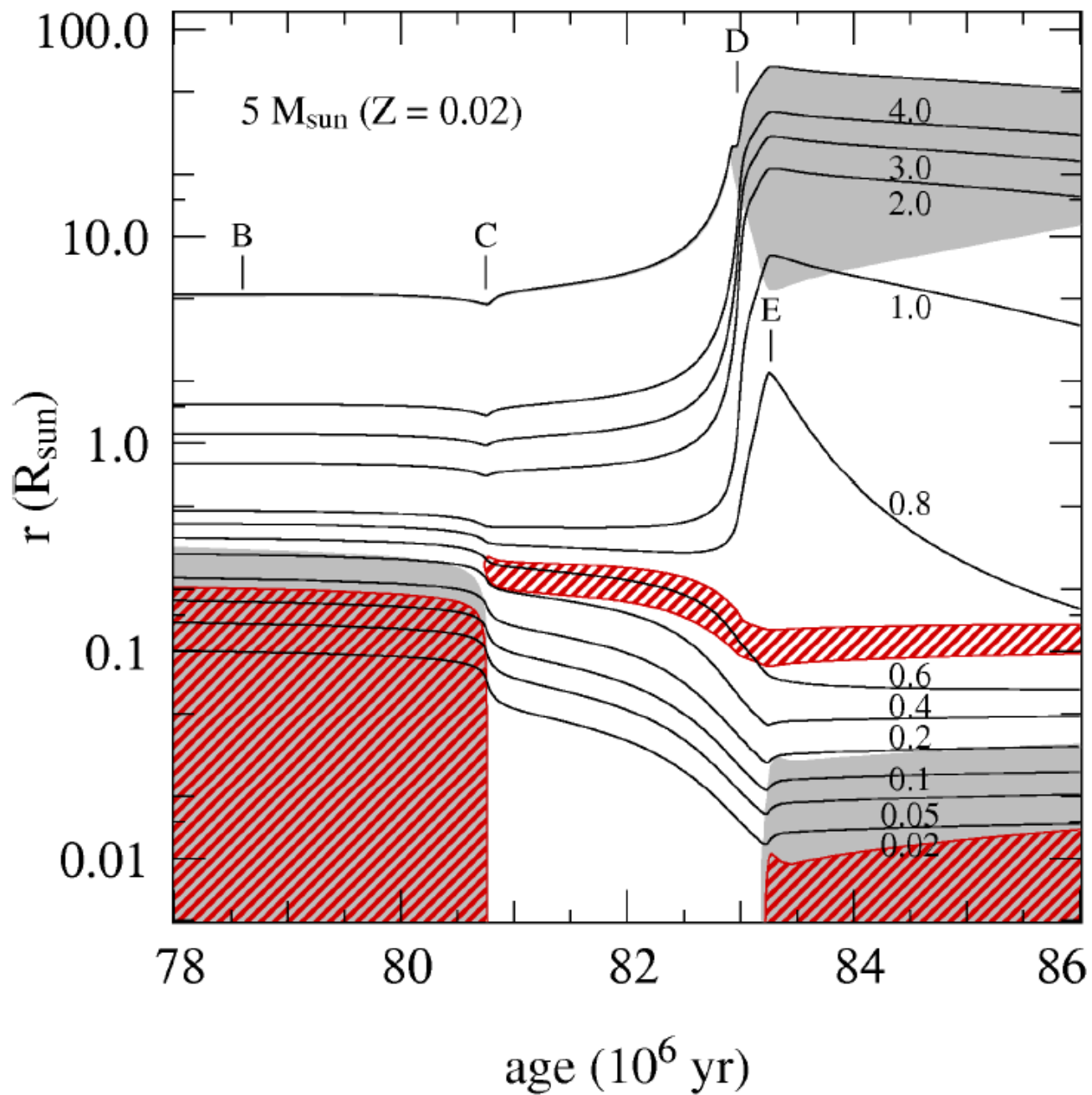


**Figure 8.10.** Hydrogen abundance profiles at different stages of evolution for a  $1 M_\odot$  star (left panel) and a  $5 M_\odot$  star (right panel) at quasi-solar composition. Figures reproduced from SALARIS & CASSISI.

# Post-MS Evolution (He-burning)

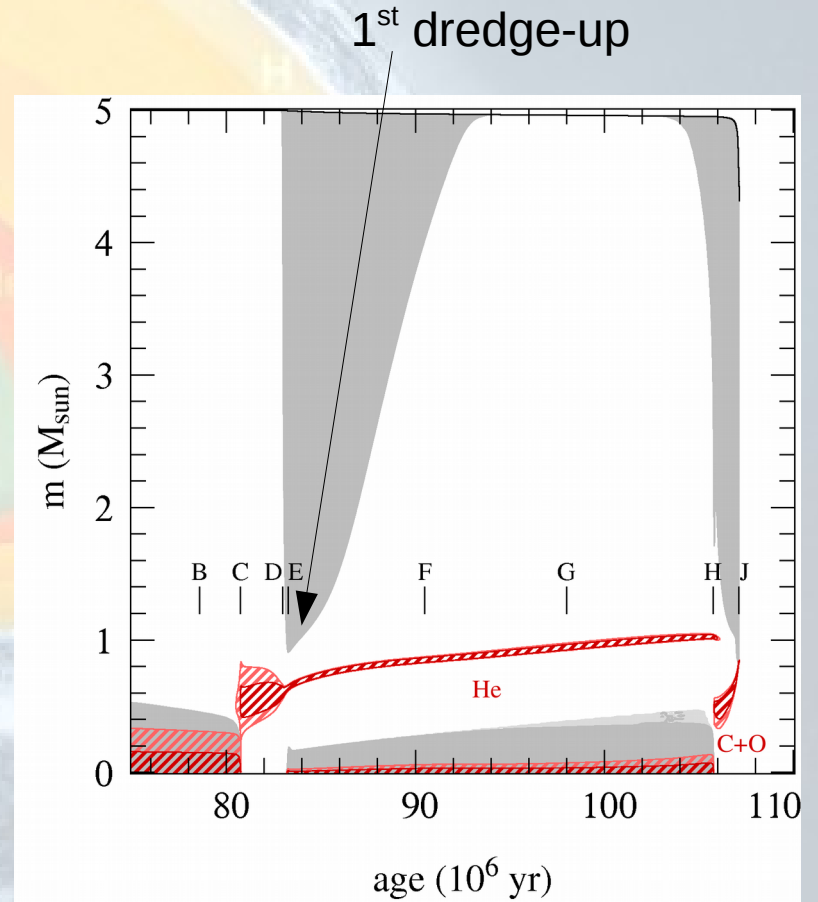
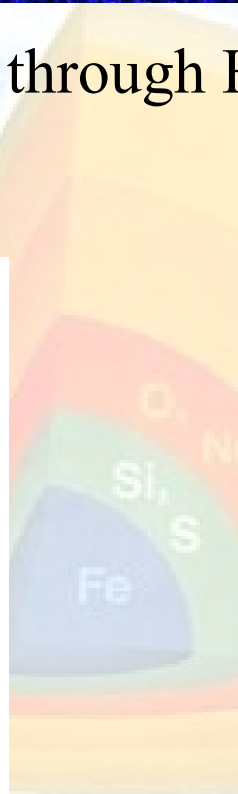
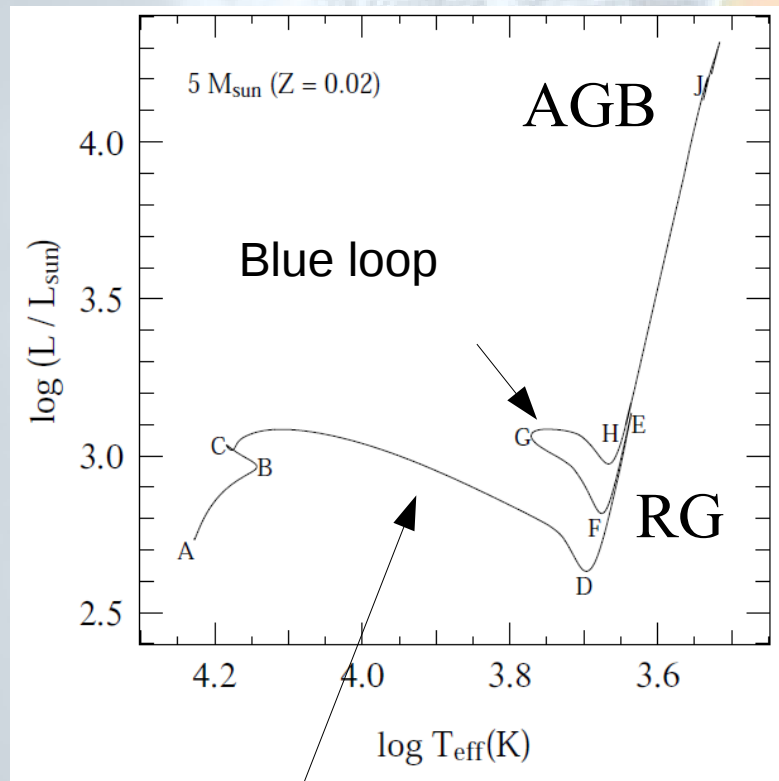


# Post-MS Evolution: Mirror Effect



# Intermediate Mass Stars

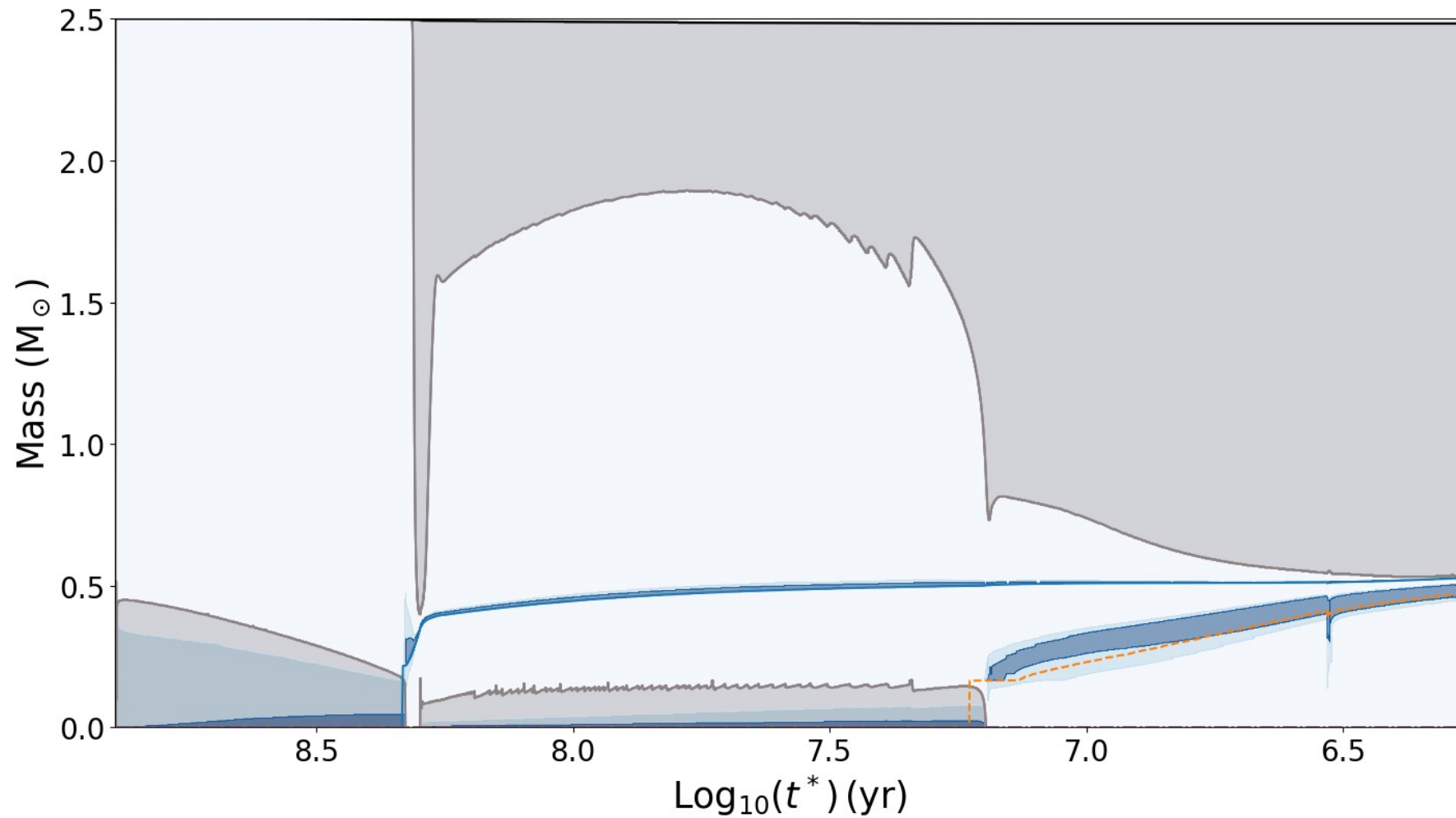
5  $M_{\odot}$  star: Evolution through H- and He-burning



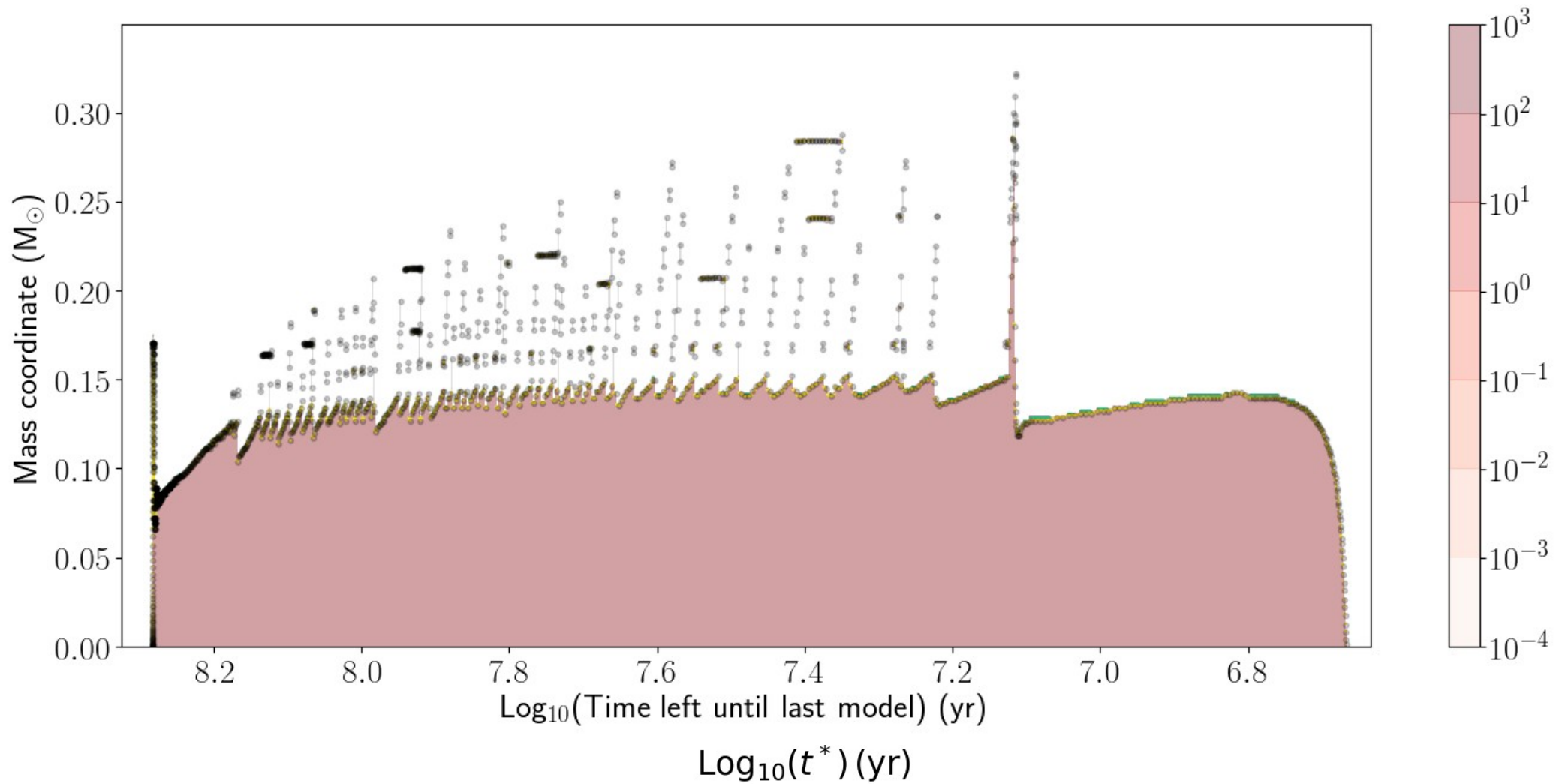
Hertzprung gap



# 2.5 $M_{\odot}$ MESA model



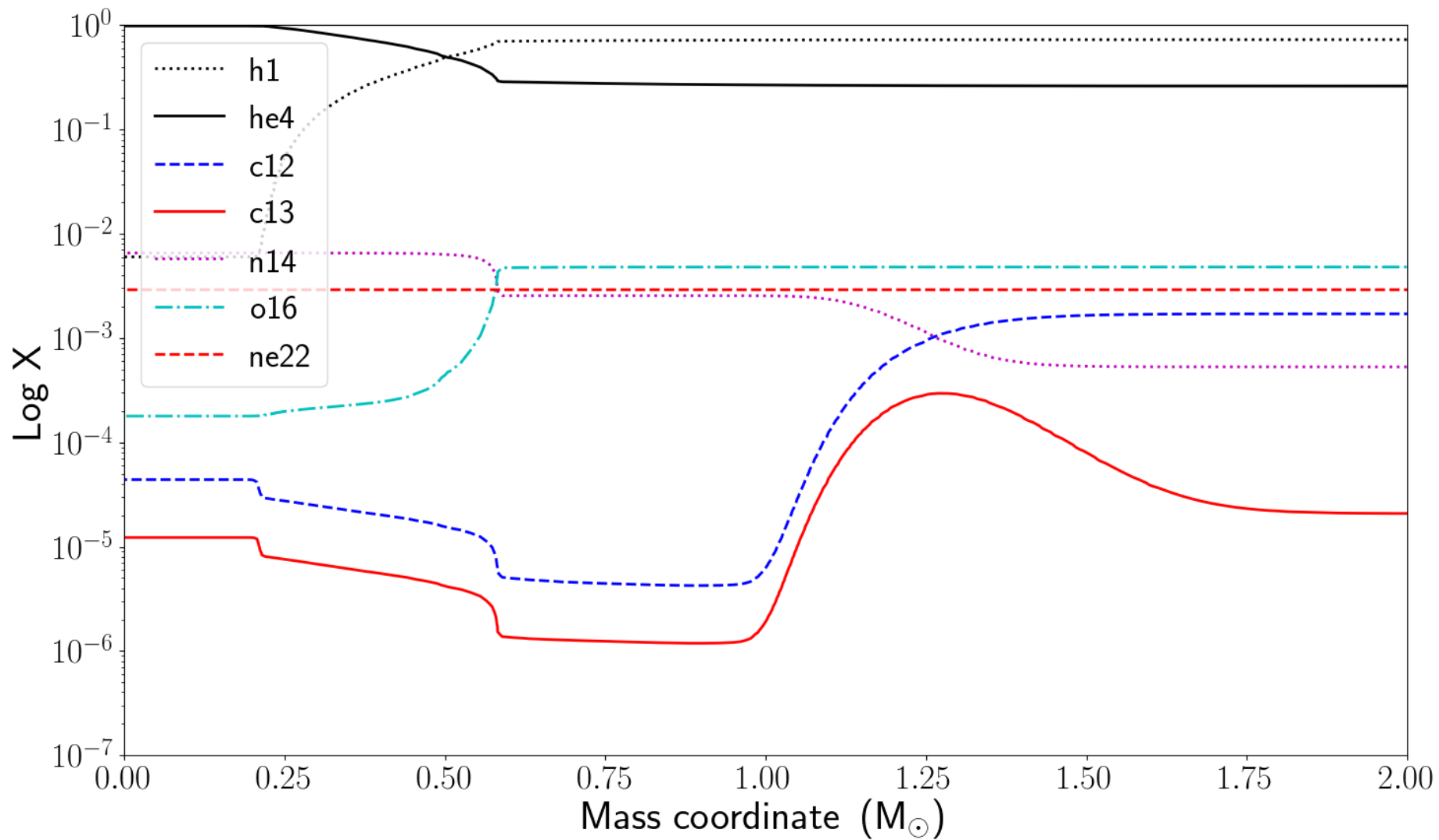
# 2.5 $M_{\odot}$ MESA model



Den Hartogh et al (in prep)

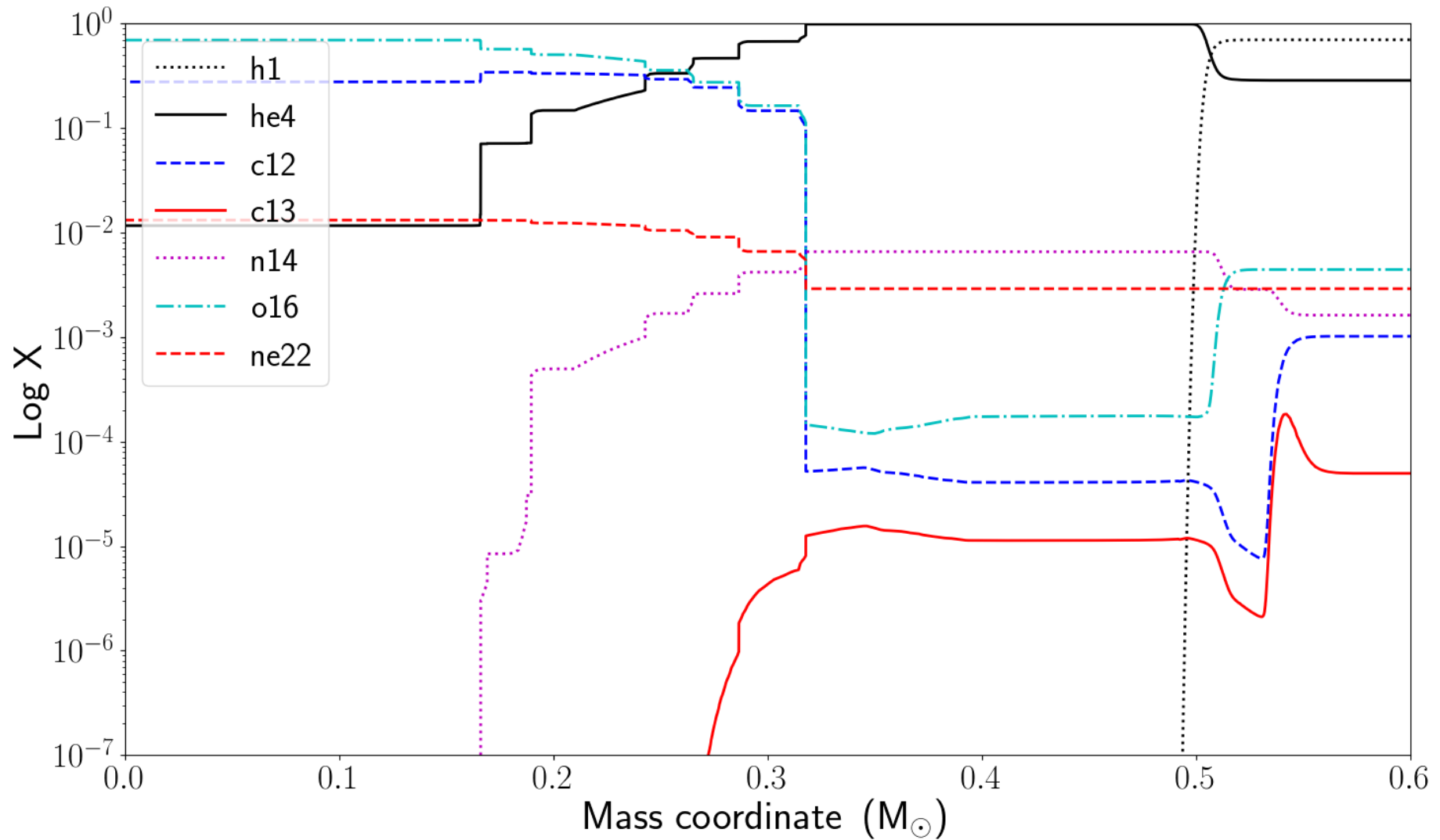
# 2.5 Mo: Abundance Evolution

End MS



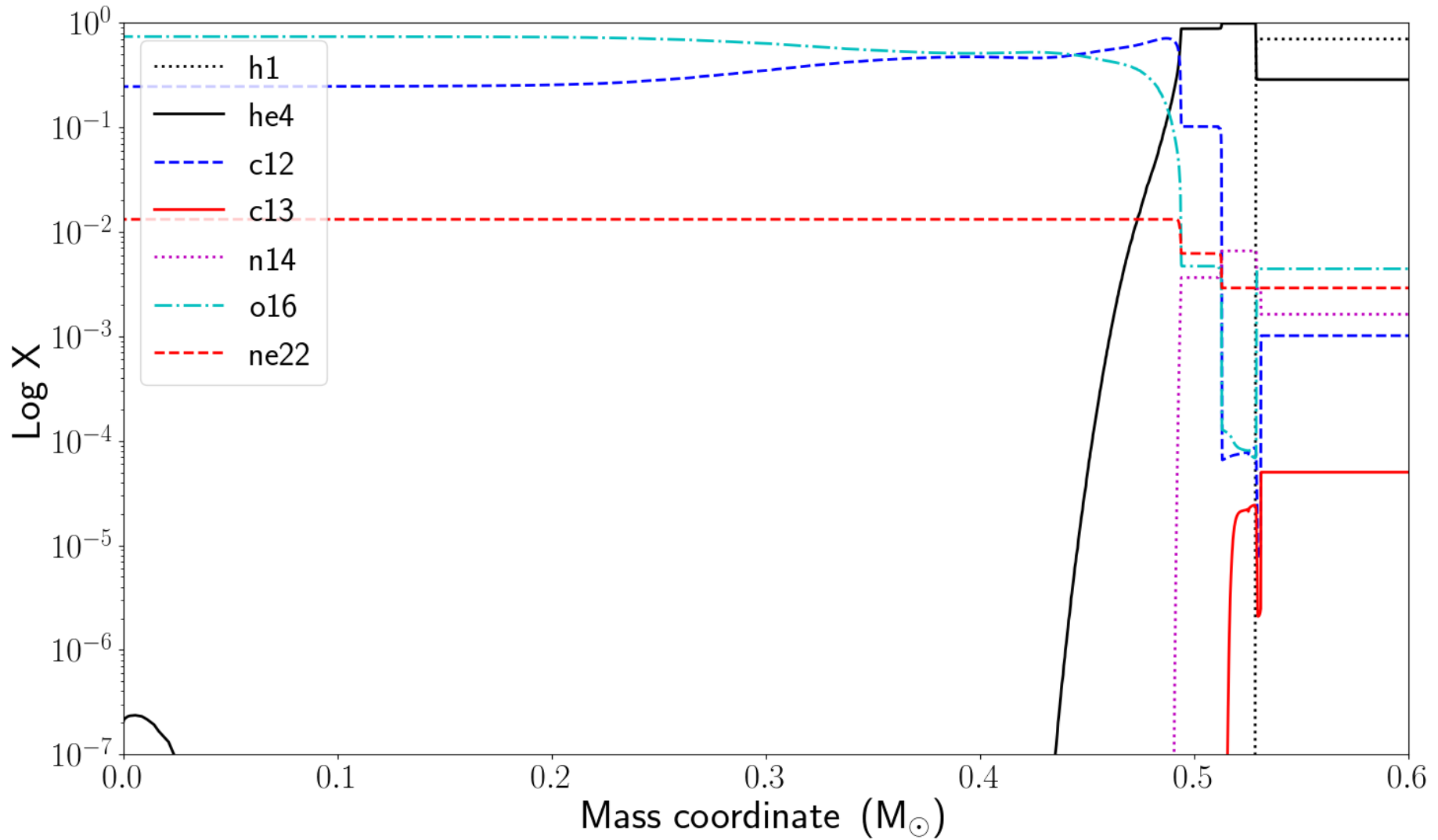
# 2.5 Mo: Abundance Evolution

## End He-burning

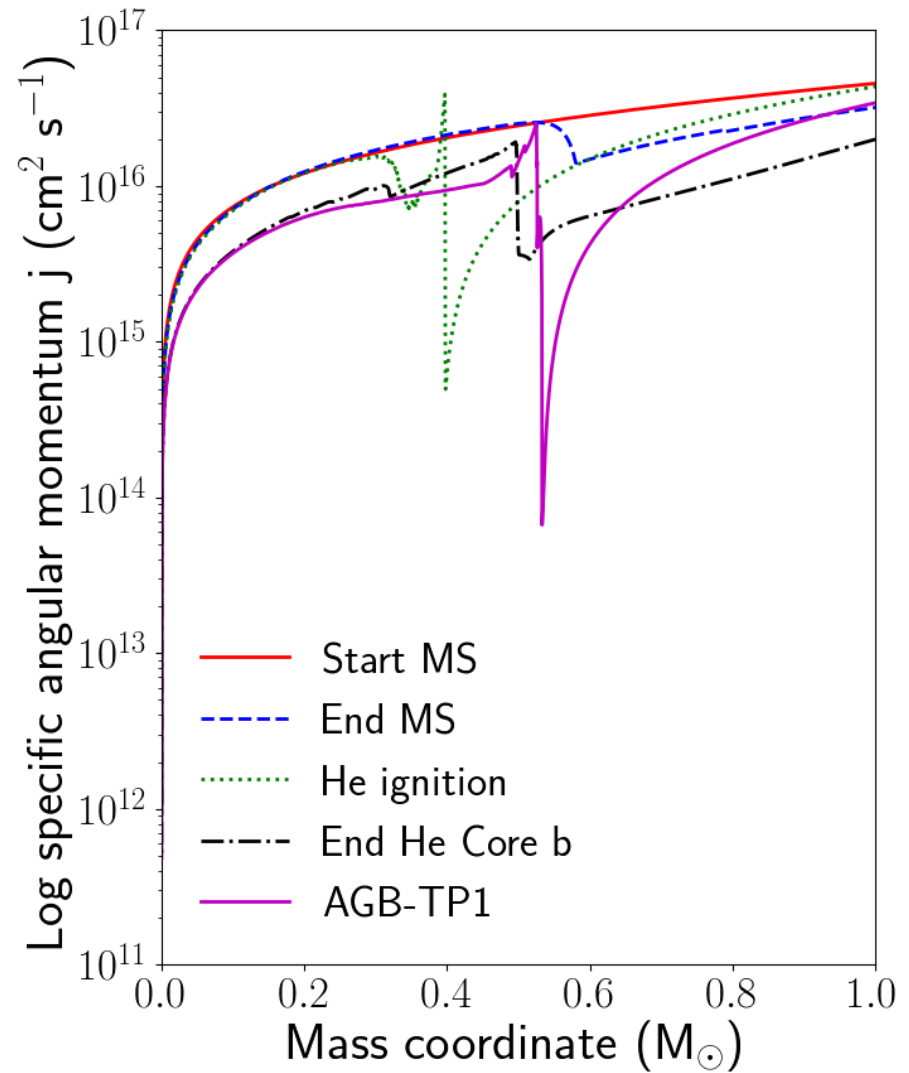
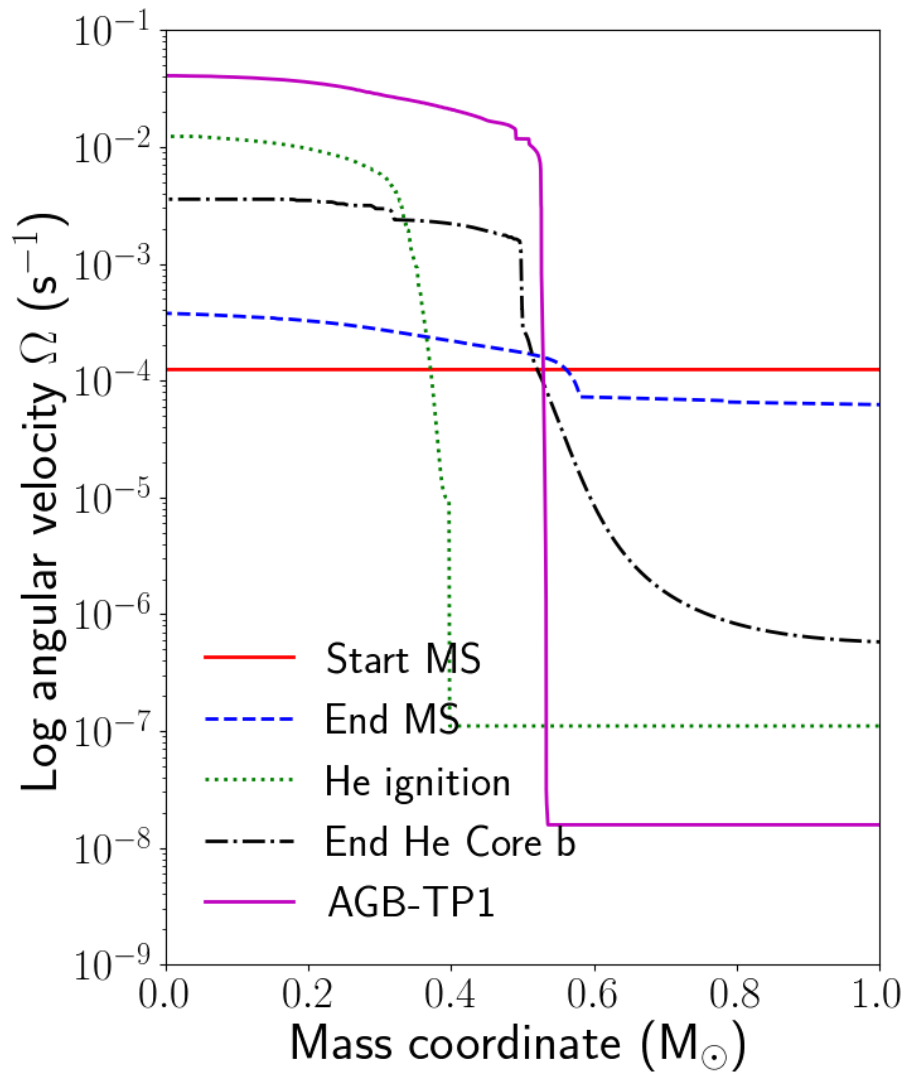


# 2.5 Mo: Abundance Evolution

Start AGB

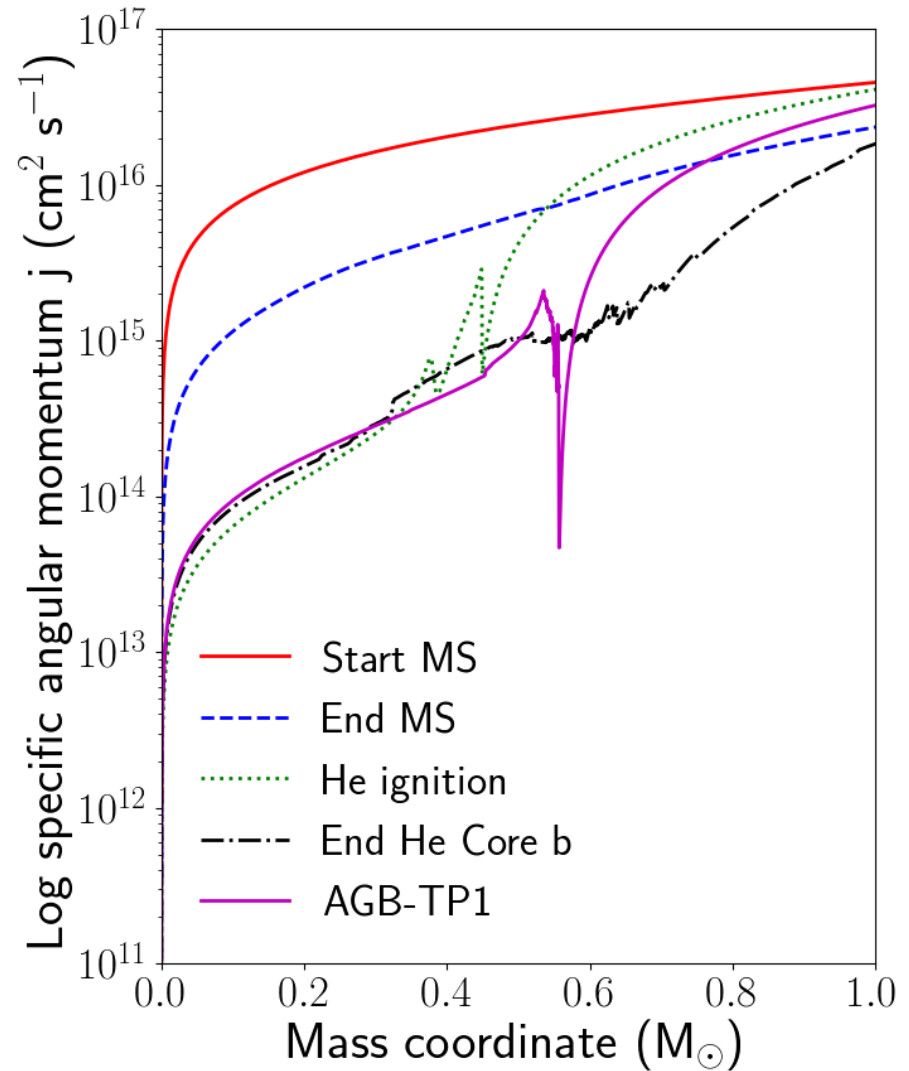
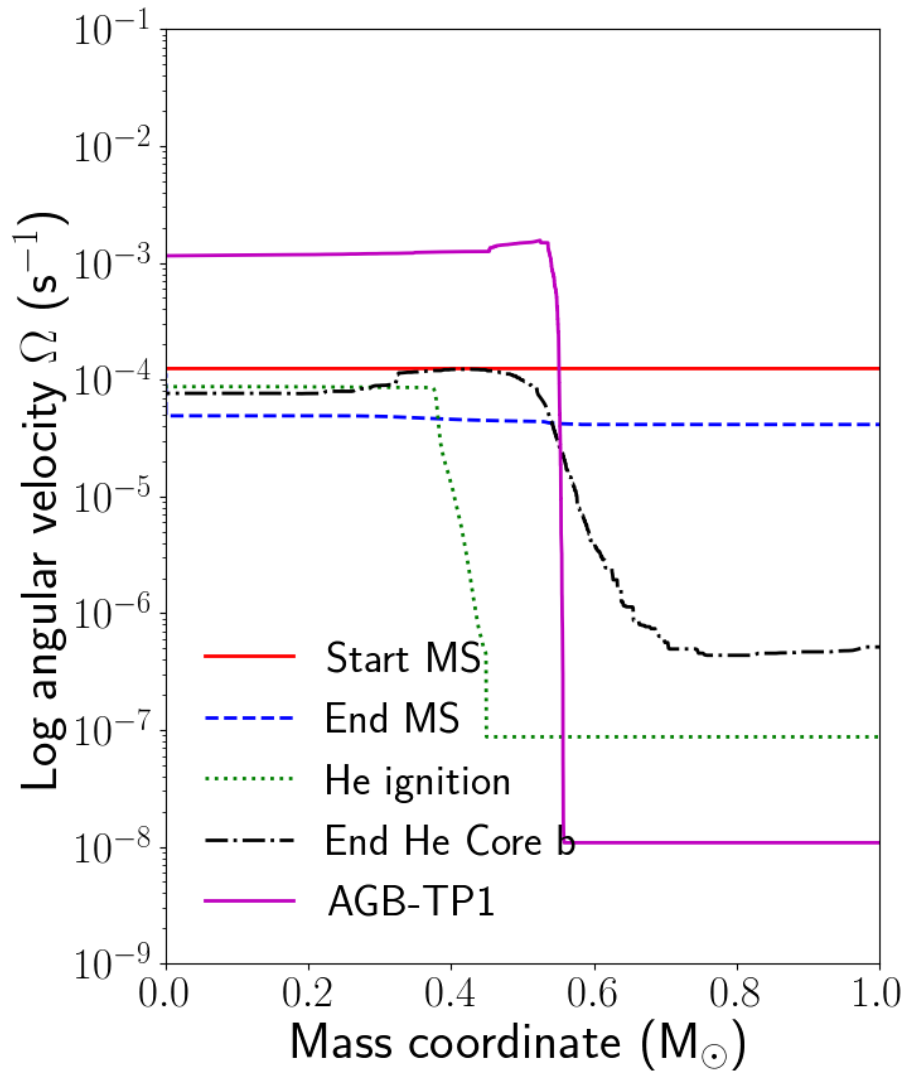


# 2.5 $M_{\odot}$ : Rotation Evolution (no B-fields)

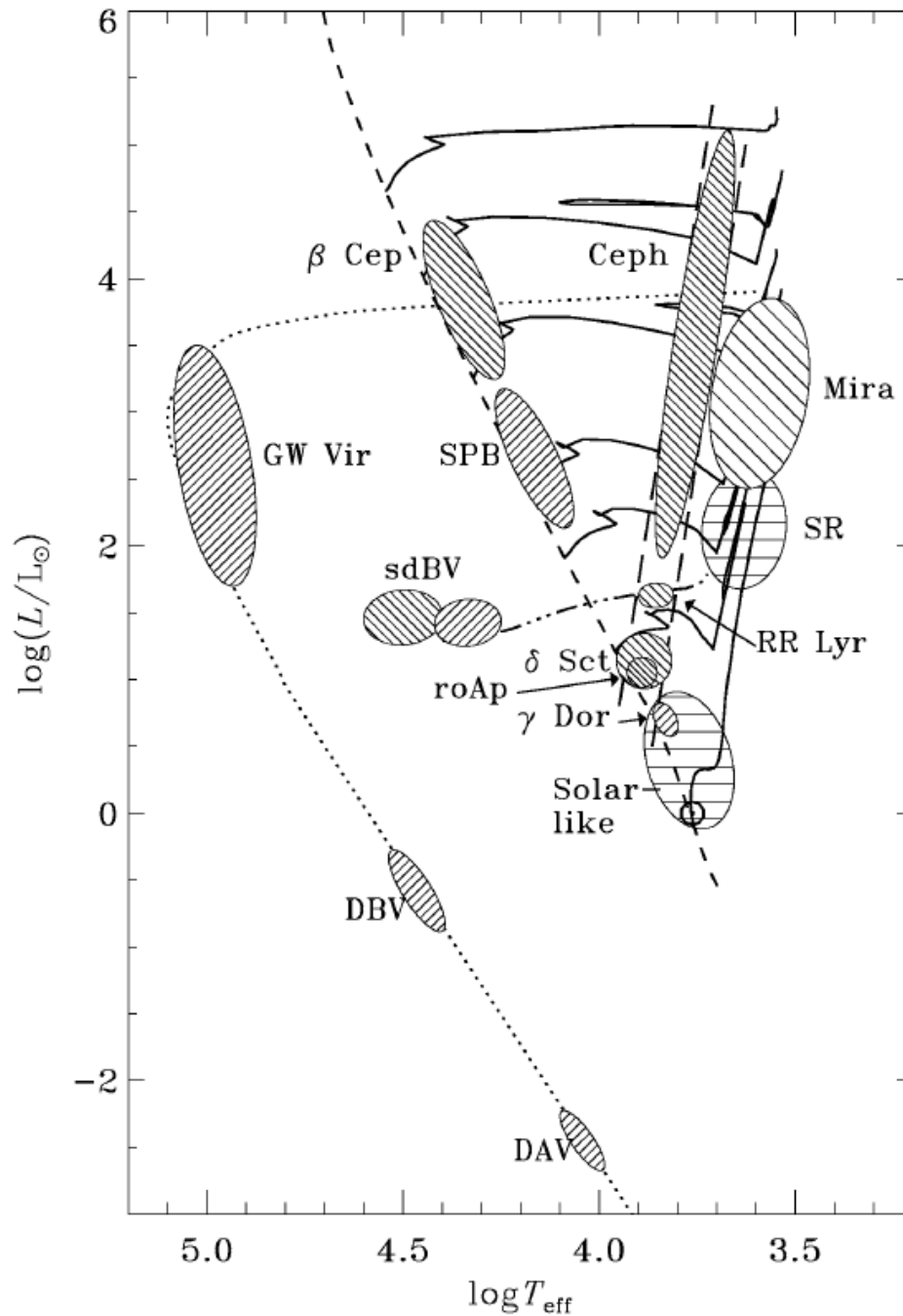




# 2.5 $M_{\odot}$ : Rotation Evolution (with B-fields)

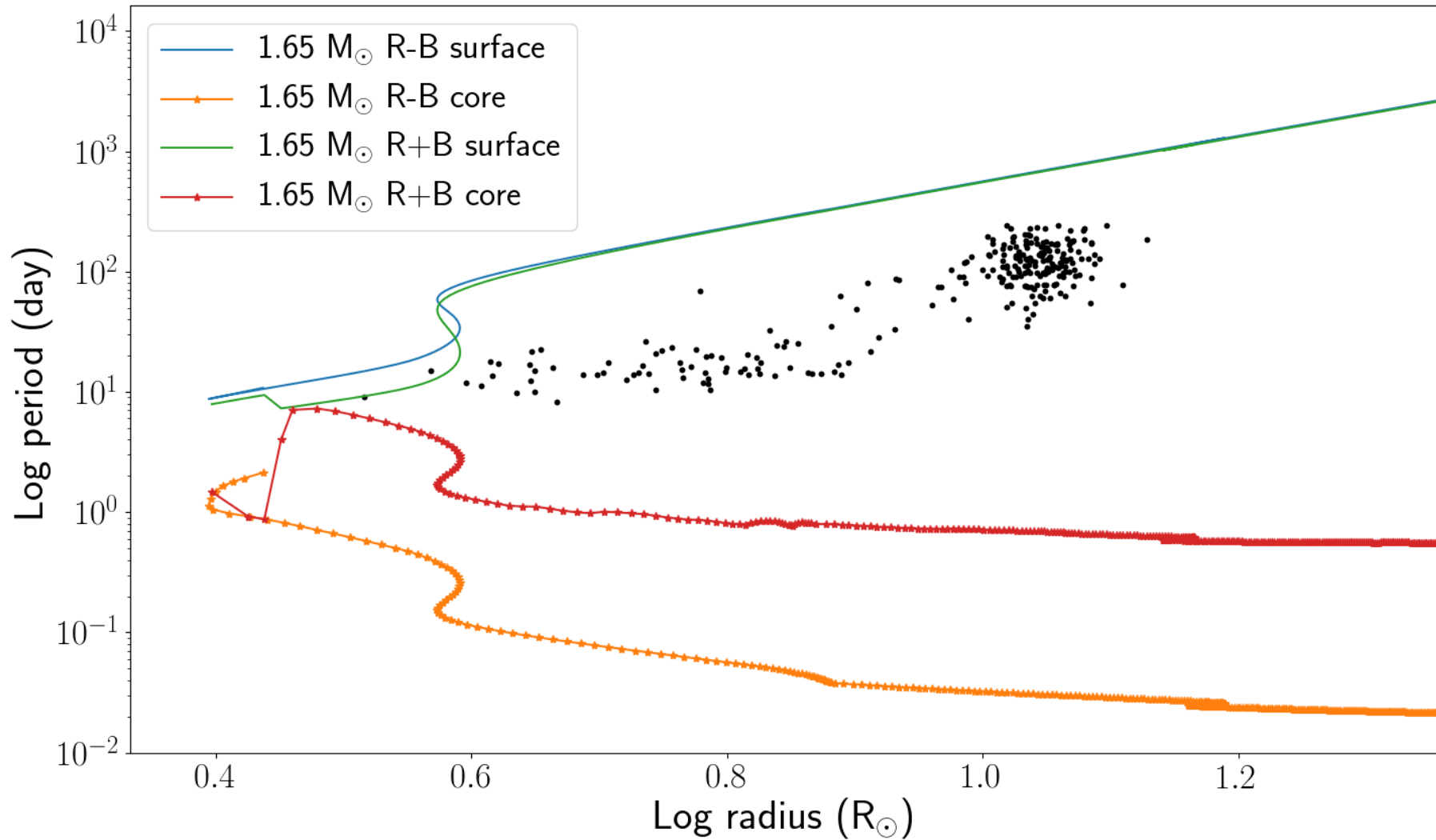


# Pulsation Across the HRD



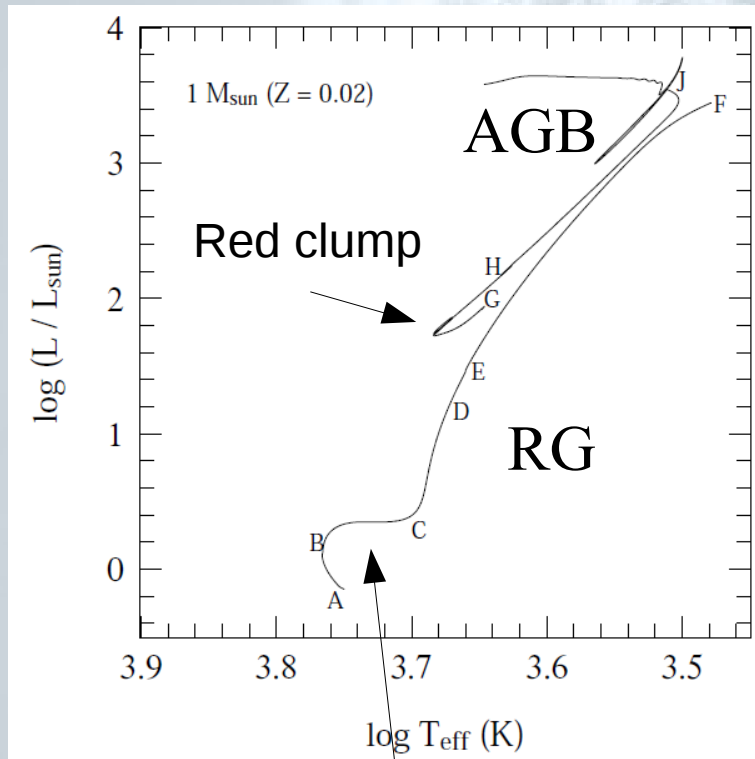
**Figure 9.10.** Occurrence of various classes of pulsating stars in the H-R diagram, overlaid on stellar evolution tracks (solid lines). Cepheid variables are indicated with 'Ceph', they lie within the pulsational instability strip in the HRD (long-dashed lines). Their equivalents are the RR Lyrae variables among HB stars (the horizontal branch is shown as a dash-dotted line), and the  $\delta$  Scuti stars ( $\delta$  Sct) among main-sequence stars. Pulsational instability is also found among luminous red giants (Mira variables), among massive main-sequence stars –  $\beta$  Cep variables and slowly pulsating B (SPB) stars, among extreme HB stars known as subdwarf B stars (sdBV) and among white dwarfs. Figure from Christensen-Dalsgaard (2004).

# 2.5 Mo: Comparison to Asteroseismology Obs.

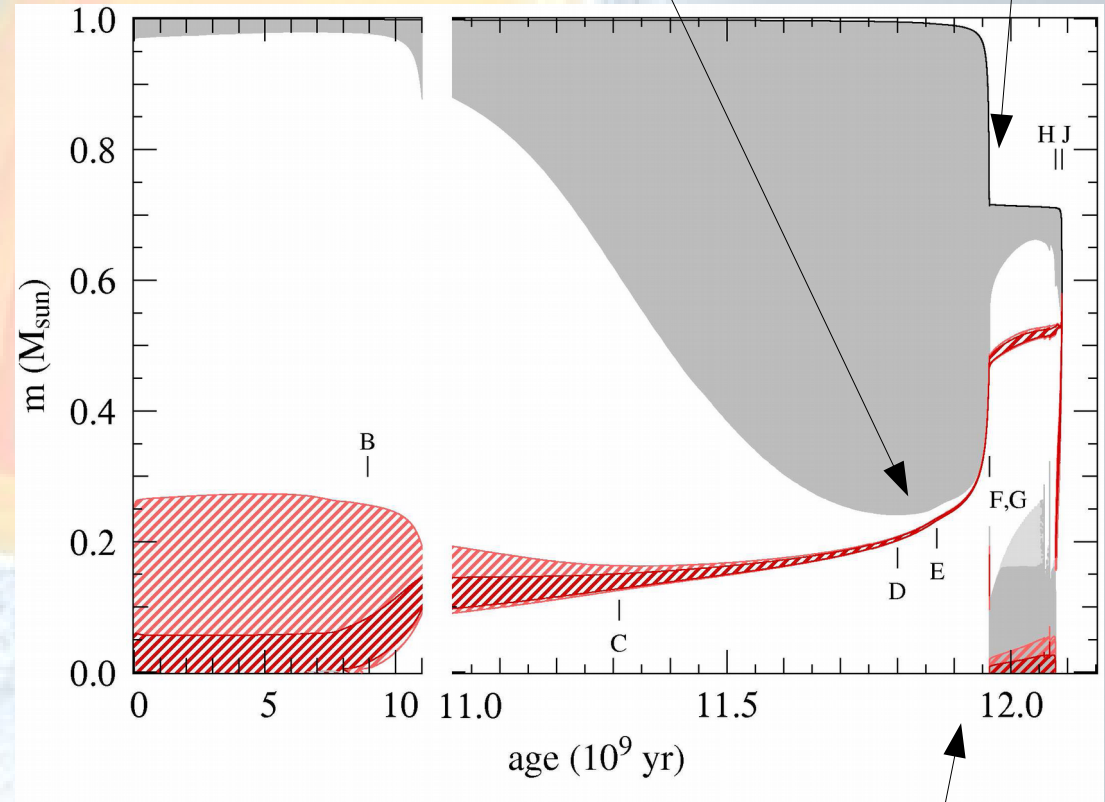


# Low-Mass Stars

1  $M_{\odot}$  star: Evolution through H- and He-burning

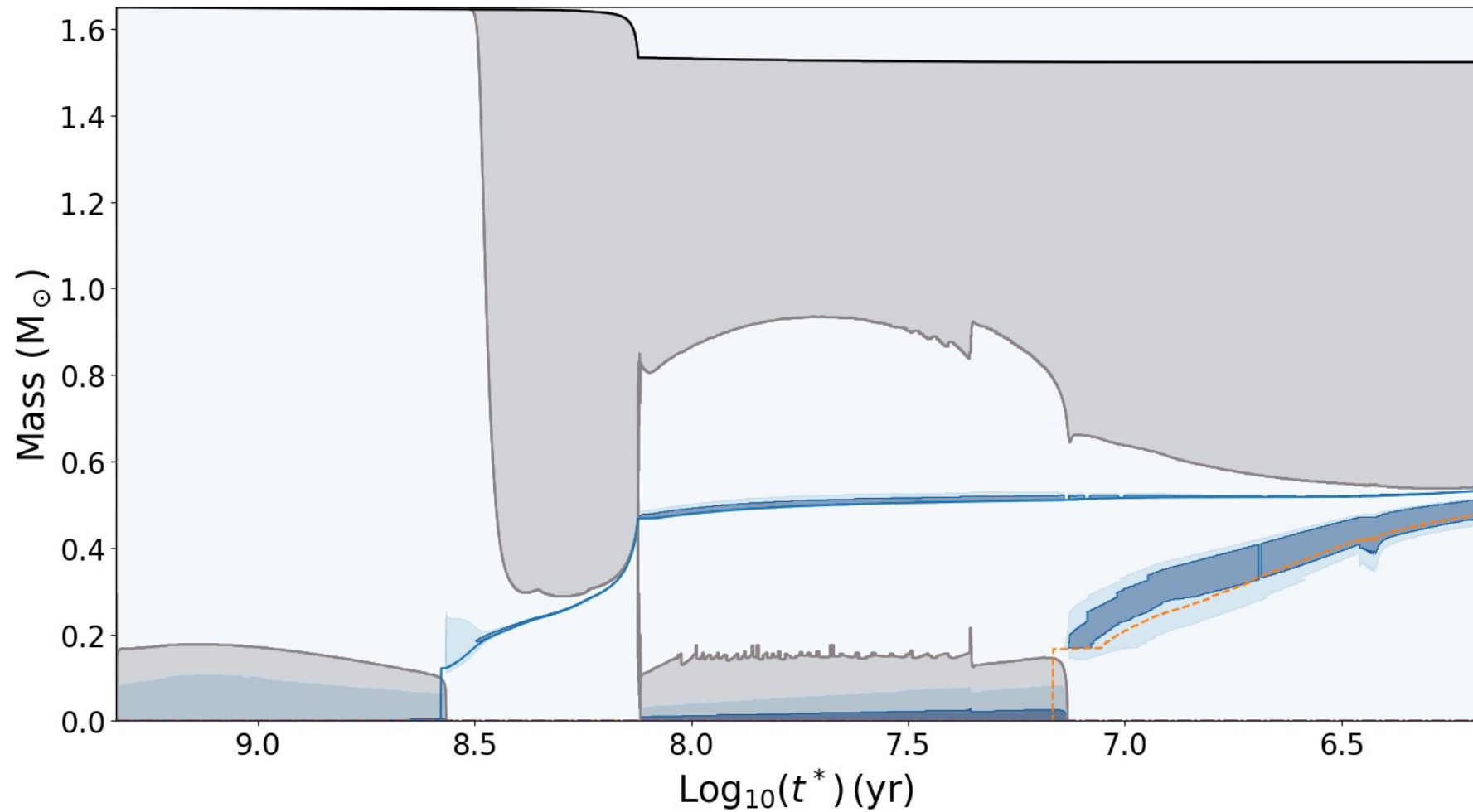


Sub-giant branch  
(no Hertzsprung gap)

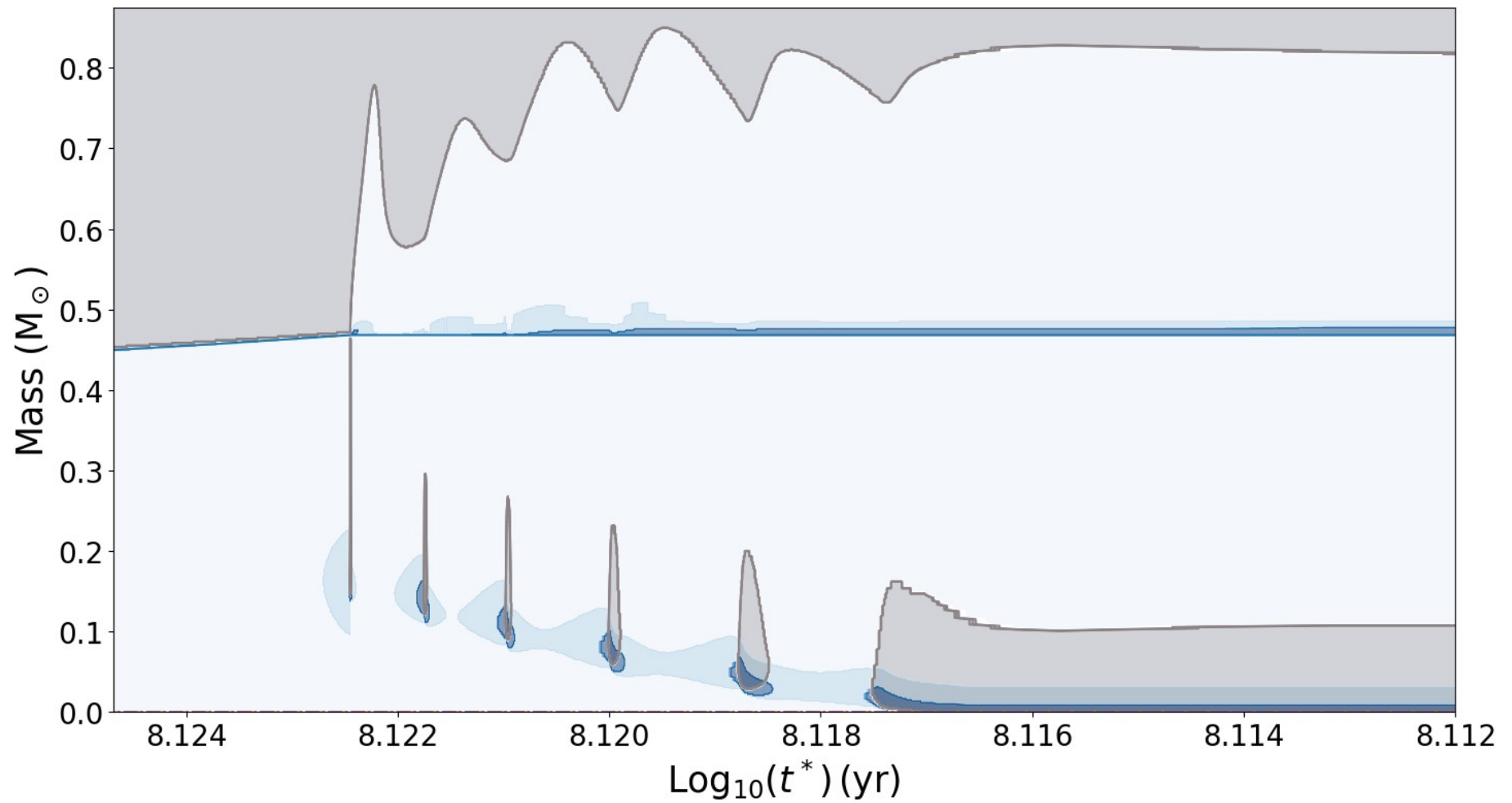


He-flash at point F  $\rightarrow$  G

# 1.65 $M_{\odot}$ MESA model



# 1.65 $M_{\odot}$ MESA model

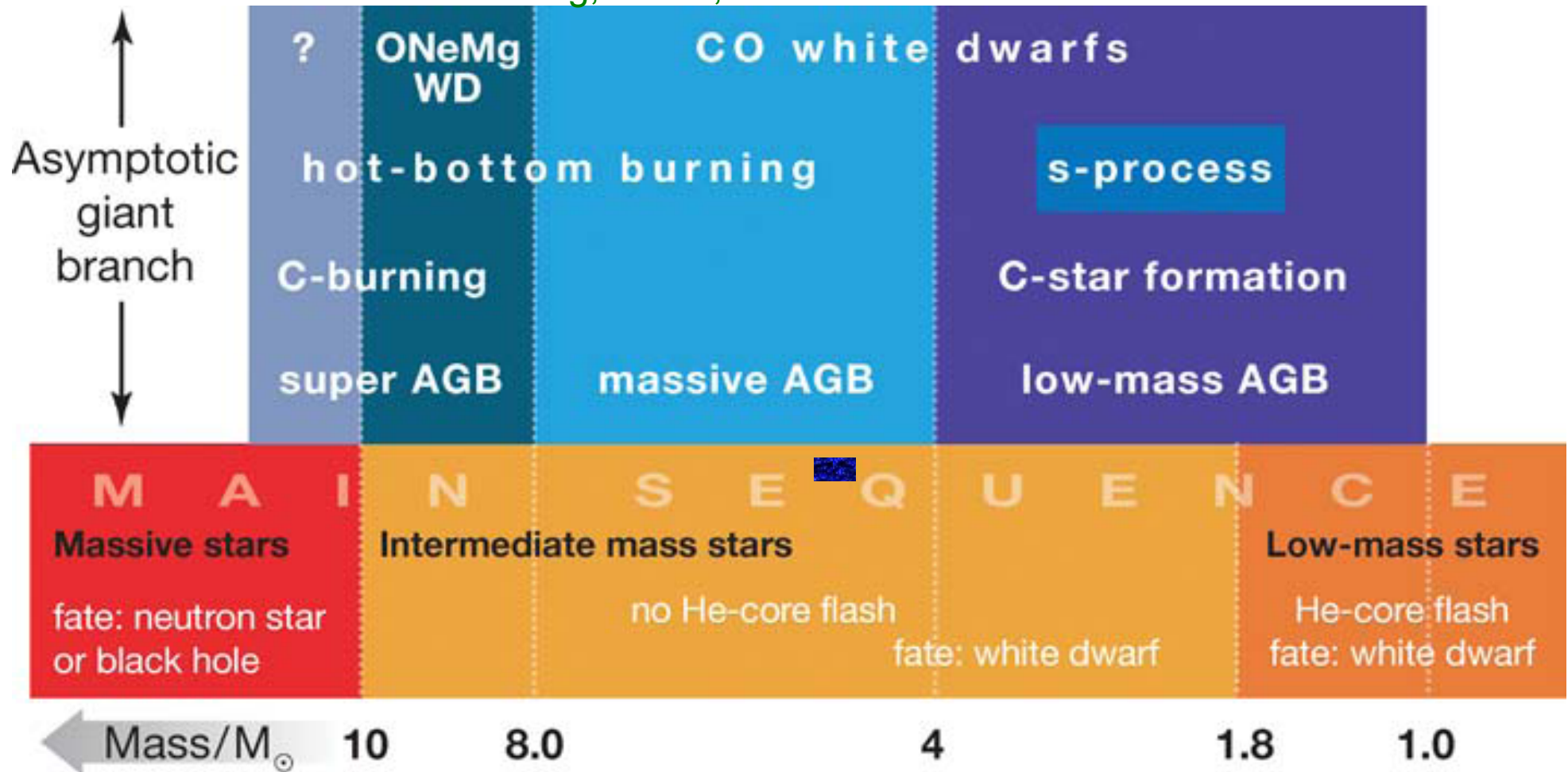


Den Hartogh et al (in prep)



# Intermediate & Low-Mass Stars: Late Phases

Herwig, ARAA, 2005



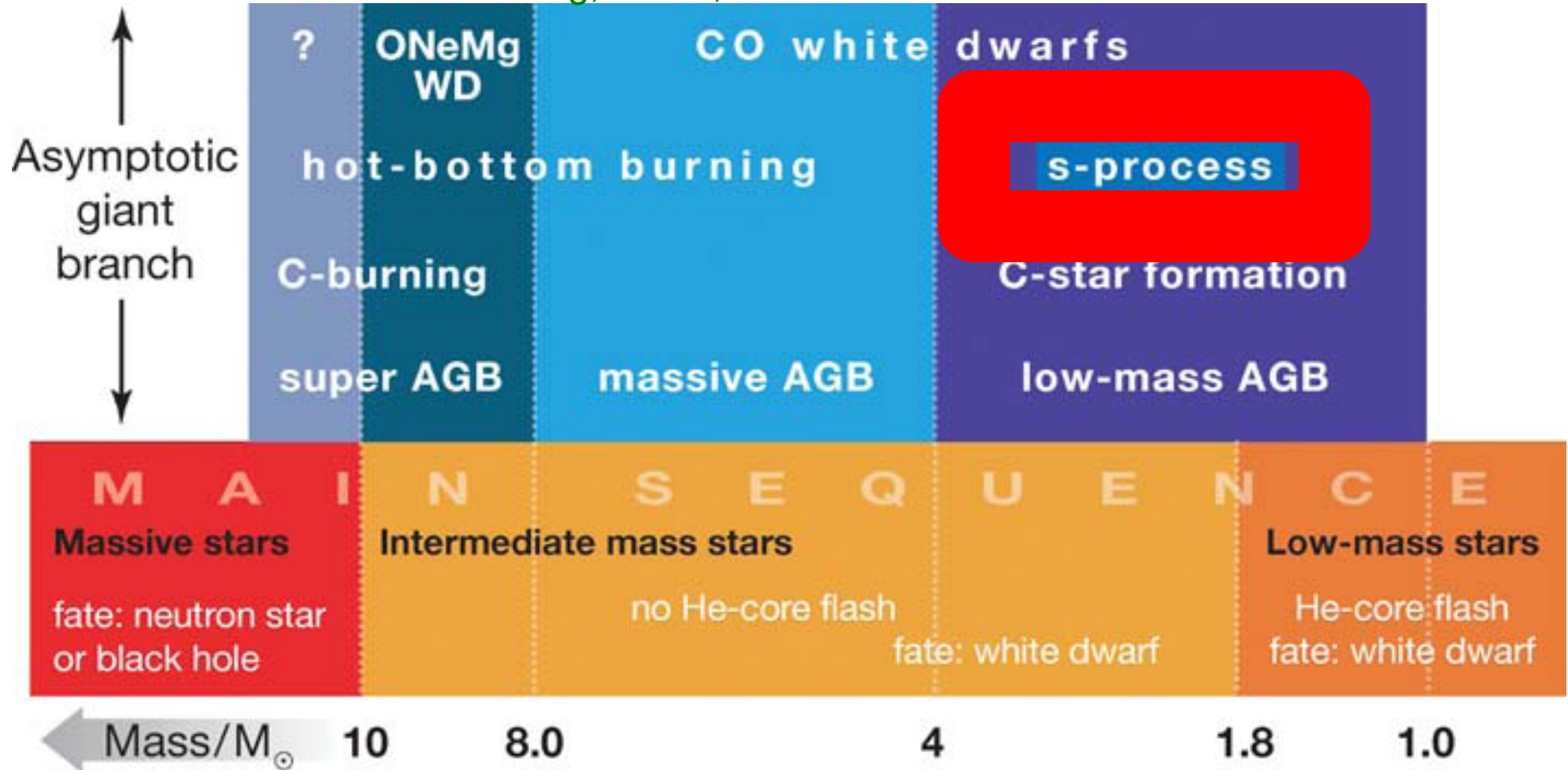
**Intermediate-mass stars:** 1.8 - 9  $M_{\odot}$  do not ignite C-burning in centre

(C-flash for SAGB stars, see later)

**Low-mass stars:** 0.5-1.8 $M_{\odot}$  do not ignite He-burning in centre (He-flash)

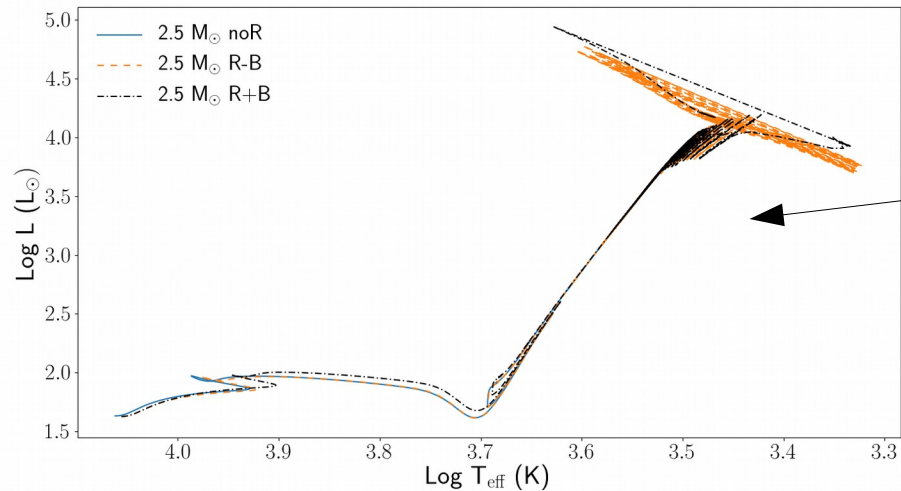
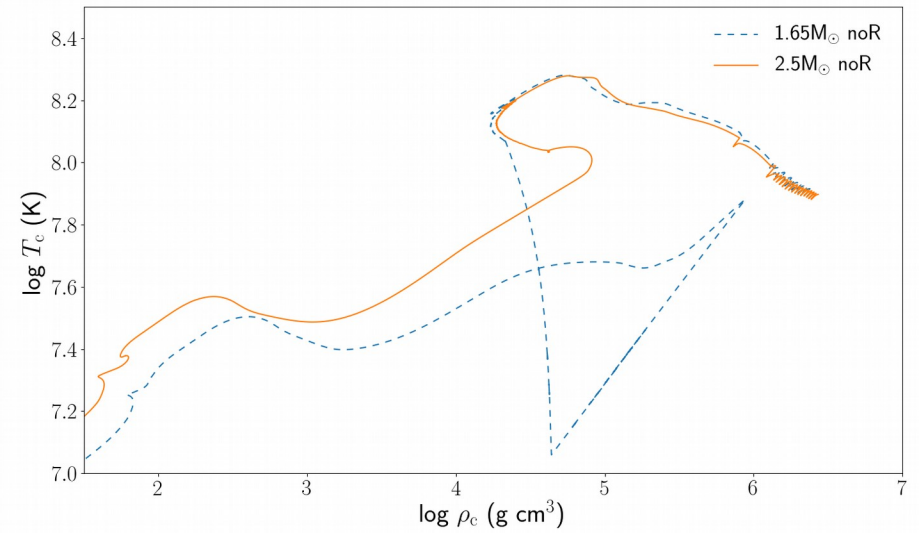
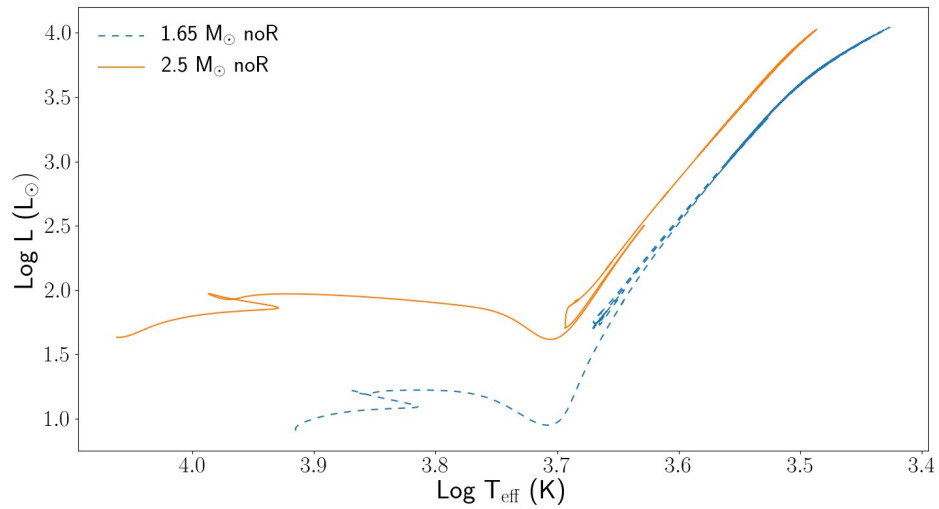
# Intermediate & Low-Mass Stars

Herwig, ARAA, 2005



AGB phase & s process in both intermediate-mass stars and low-mass stars!

# 1.65 & 2.5 Mo MESA models up to AGB phase

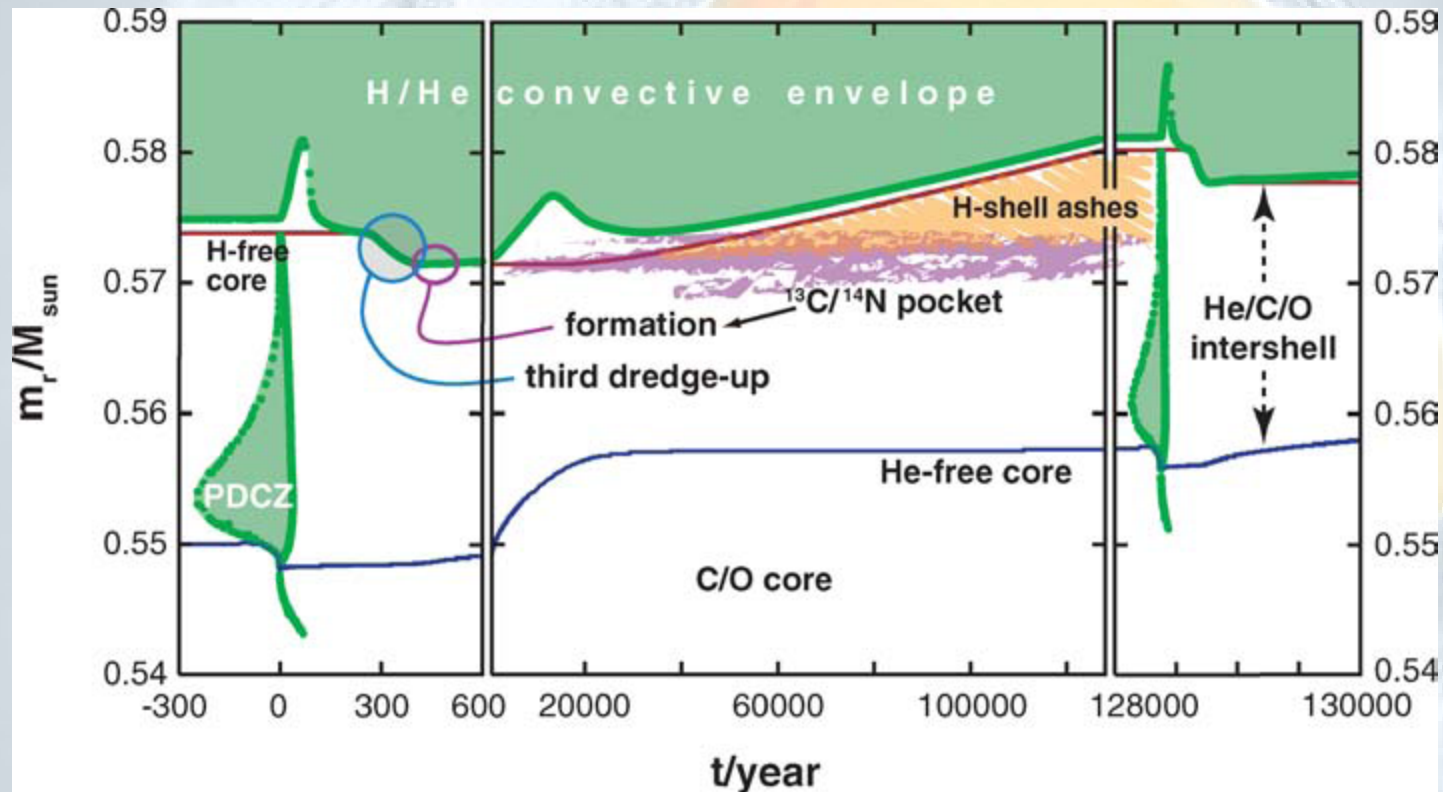


Models with rotation  
& rotation + B-fields

Den Hartogh et al (in prep)

# Intermediate & Low-Mass Stars

The plot you usually see at conferences for AGB stars:



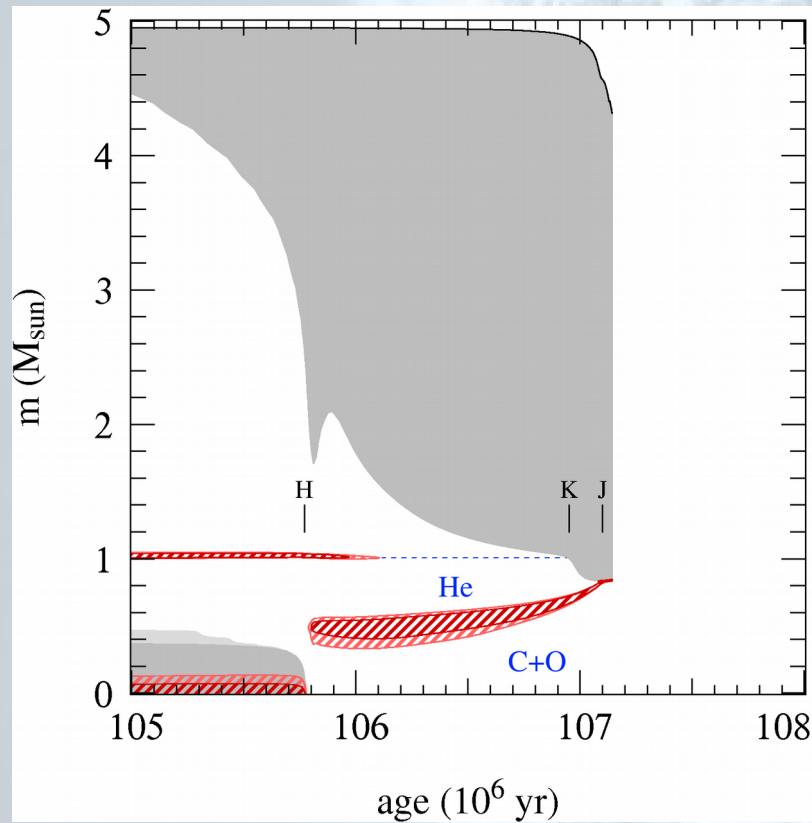
Herwig, ARAA, 2005

Where does it fit in the star's evolution?

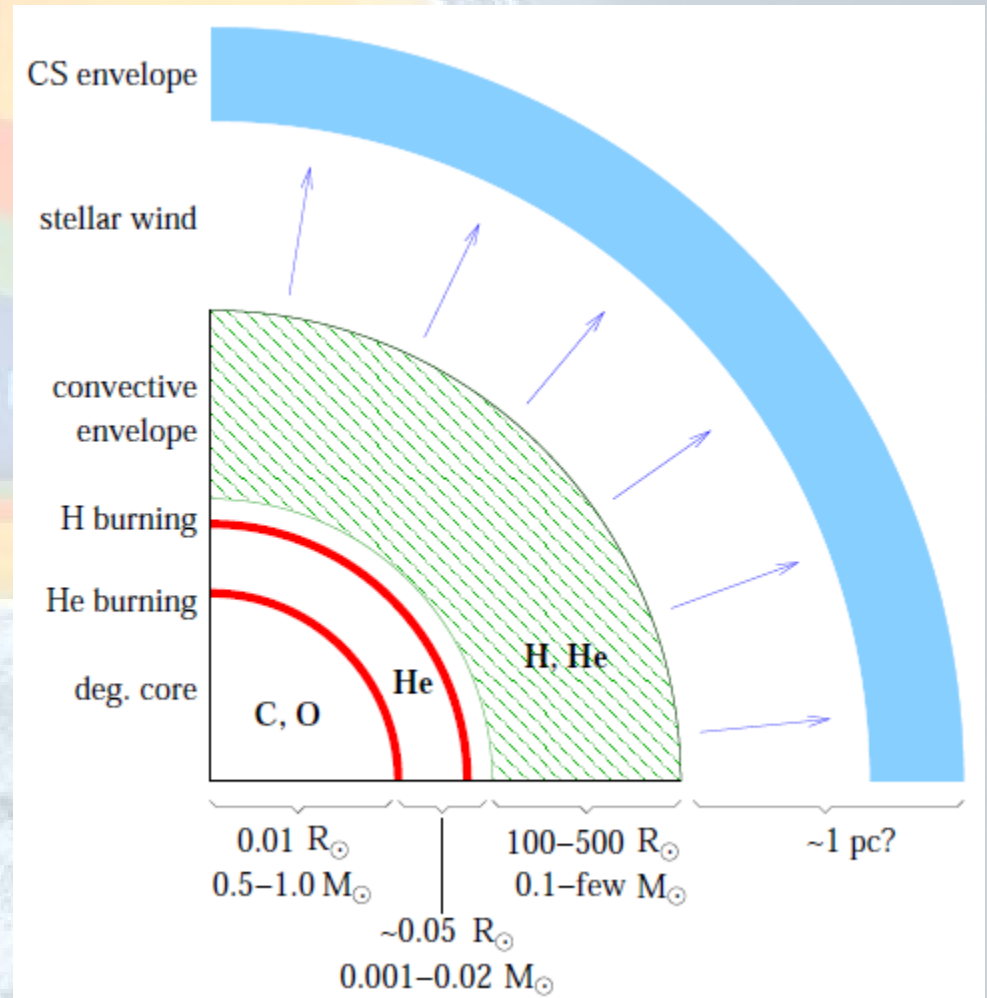


# Intermediate & Low-Mass Stars

5  $M_{\odot}$  star: early-AGB phase

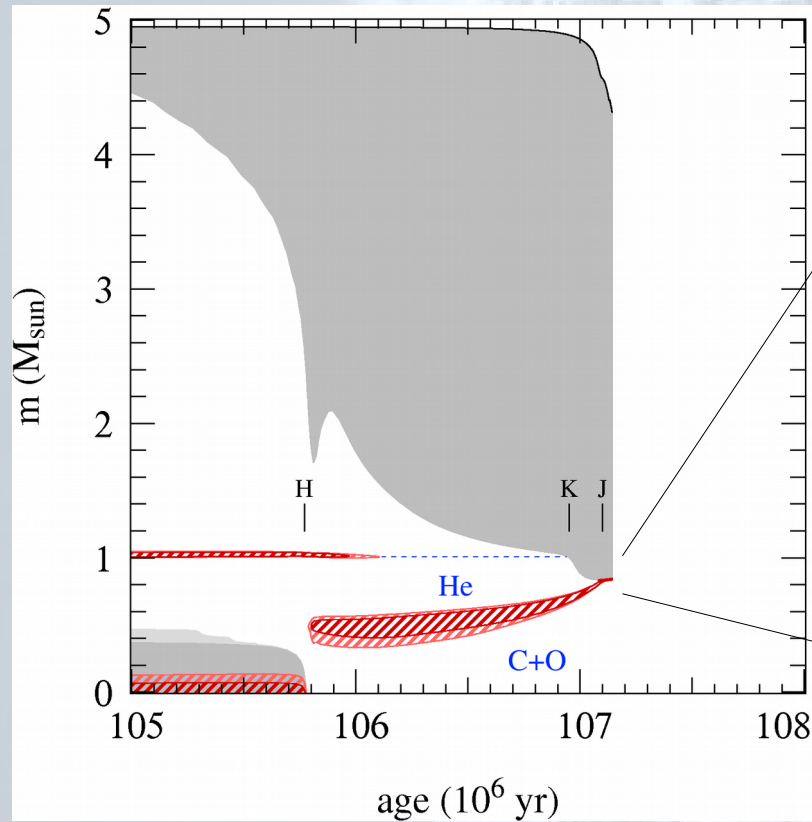


Structure in AGB phase

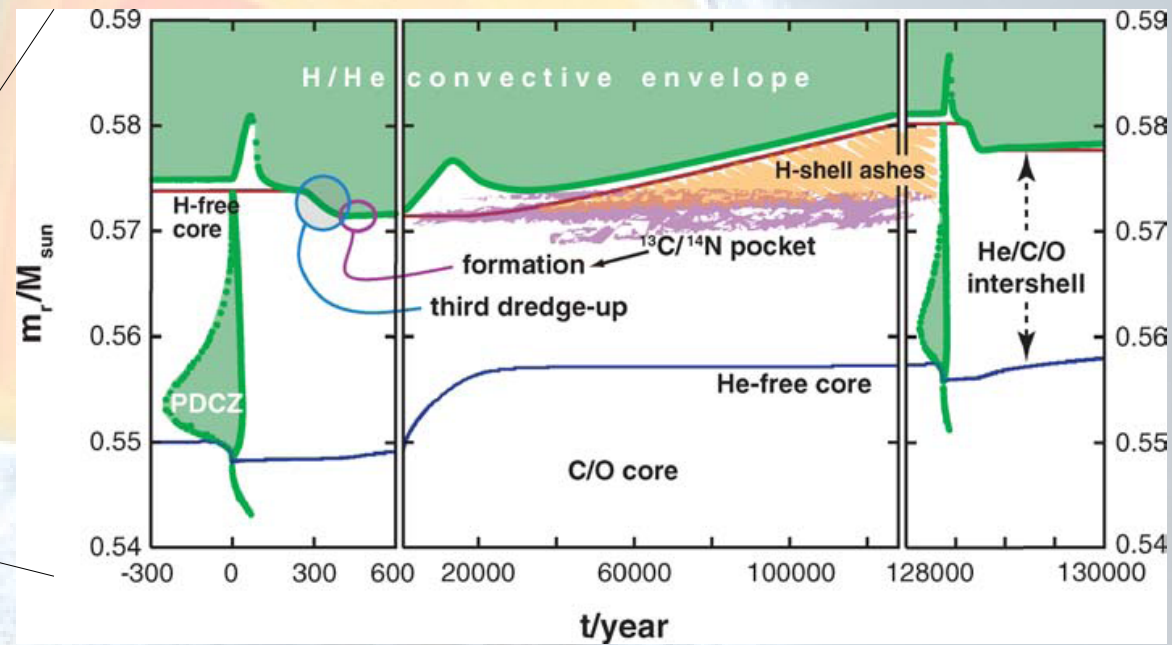


# Intermediate & Low-Mass Stars

5  $M_{\odot}$  star: AGB phase



Structure in AGB phase



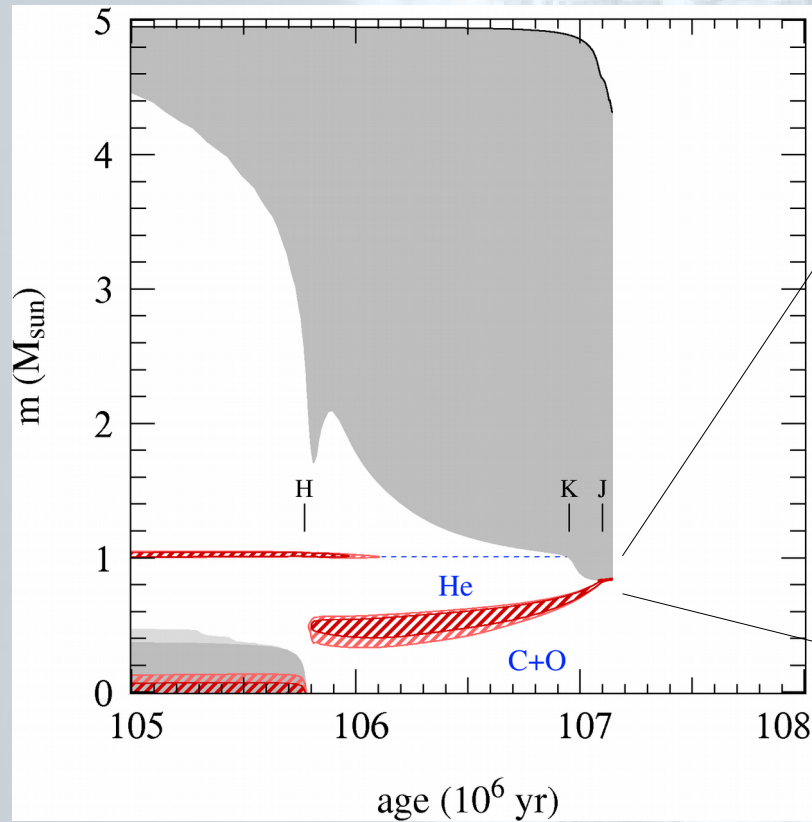
Herwig, ARAA, 2005

From SE notes, O. Pols (2009)

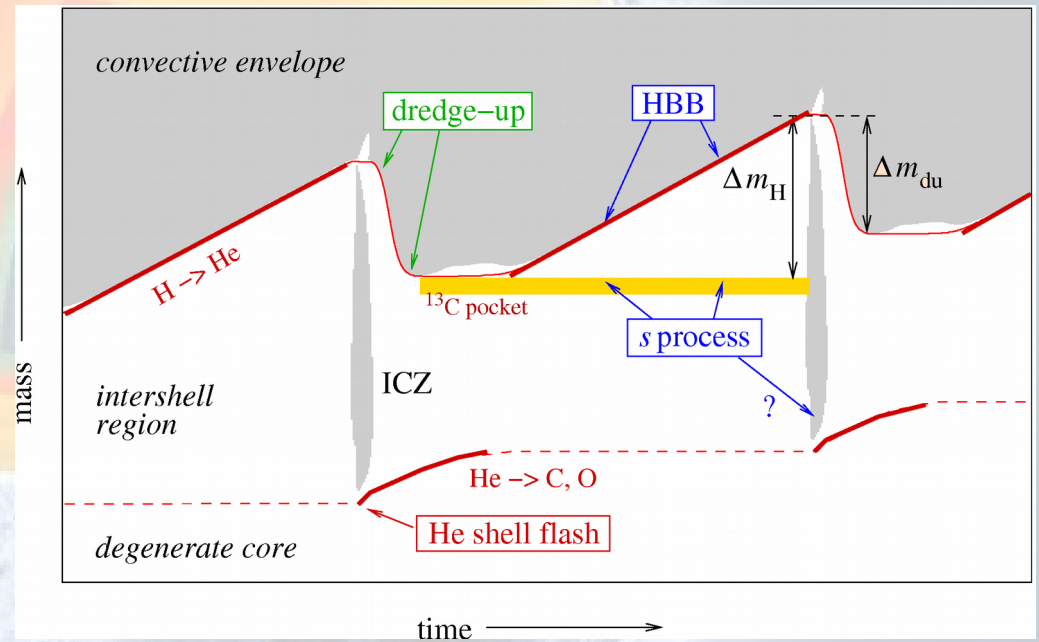


# Intermediate & Low-Mass Stars

5  $M_{\odot}$  star: AGB phase

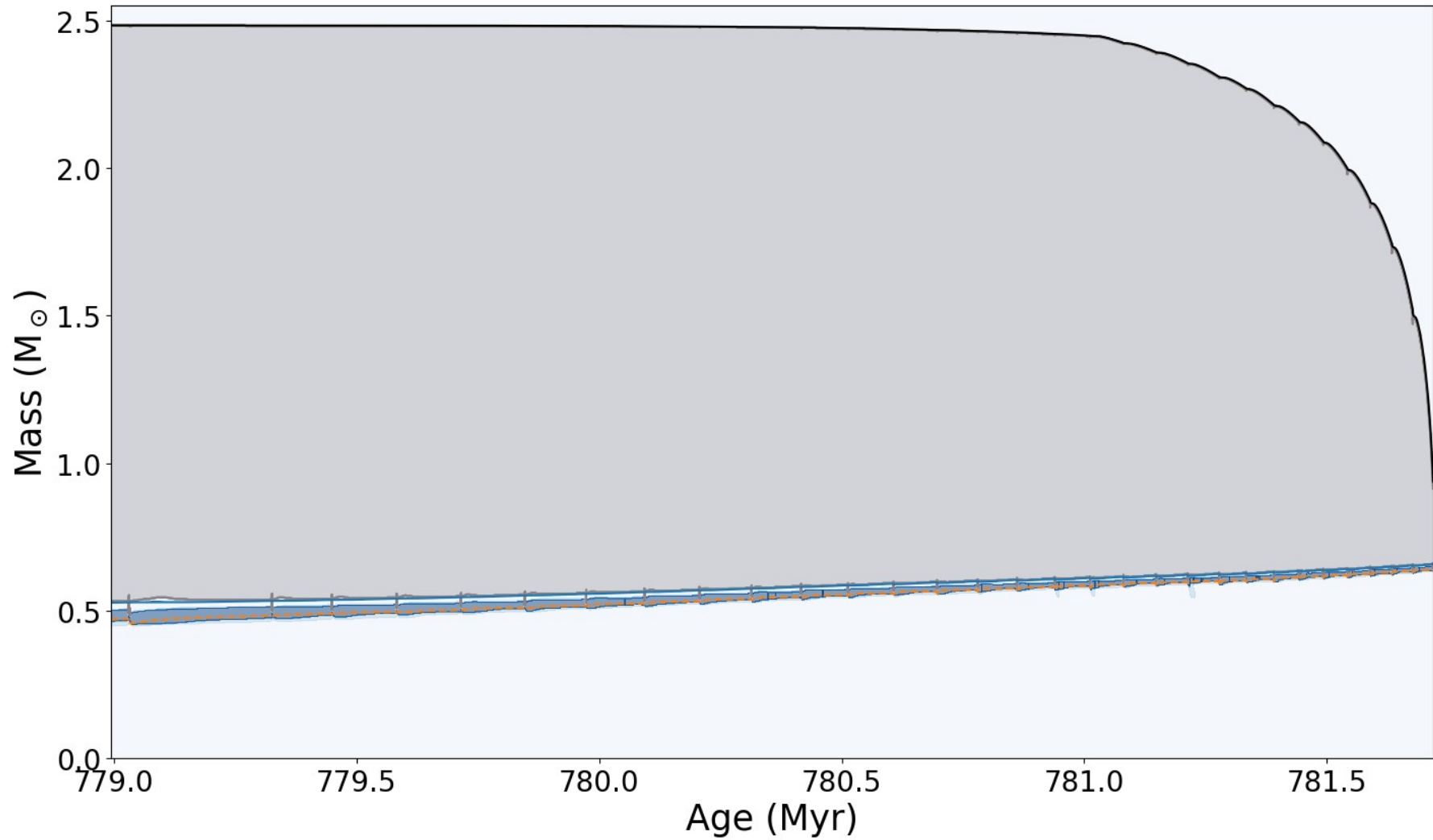


Structure in AGB phase

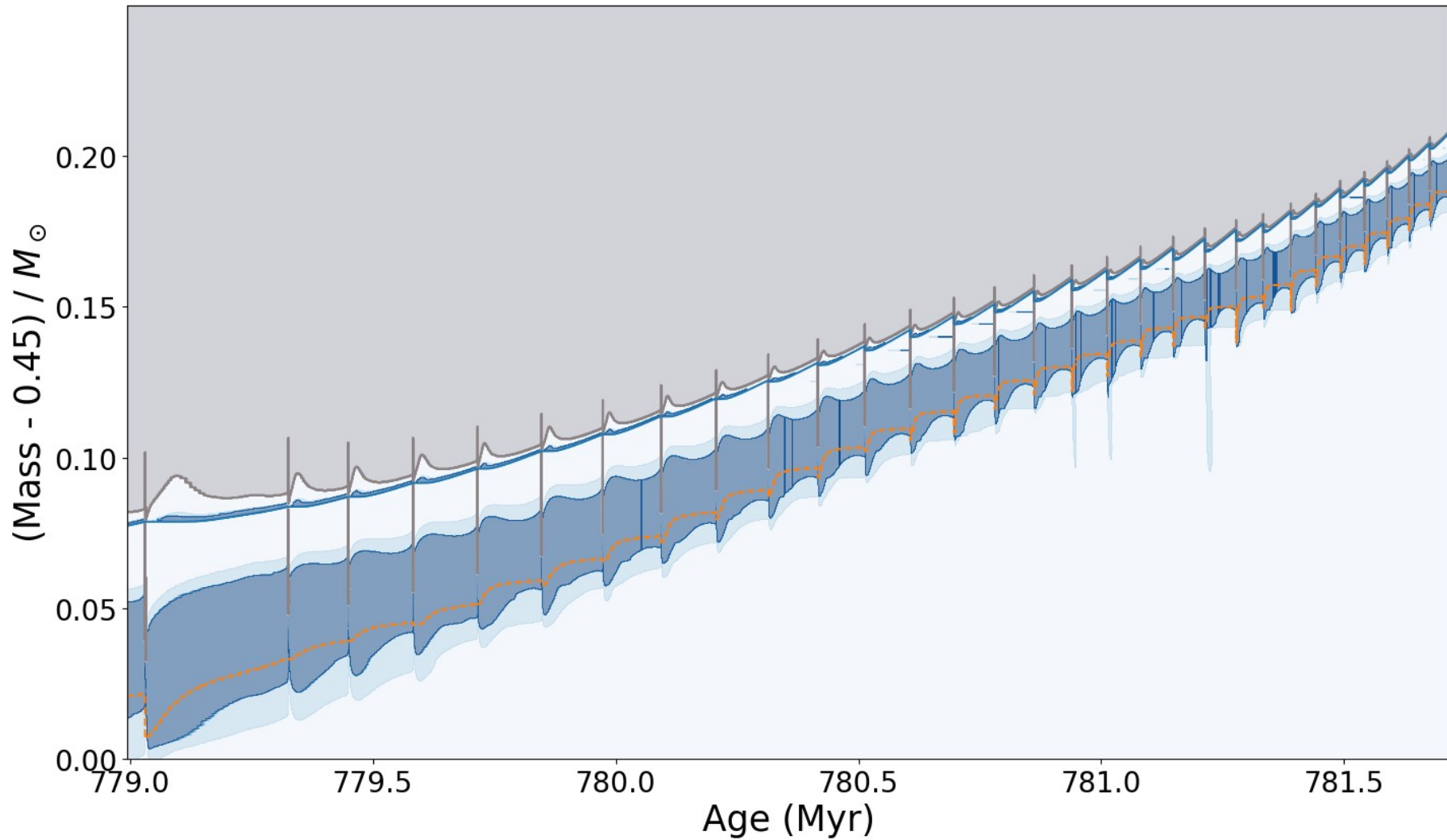


From SE notes, O. Pols (2009)

# *2.5 Mo MESA model: AGB phase*

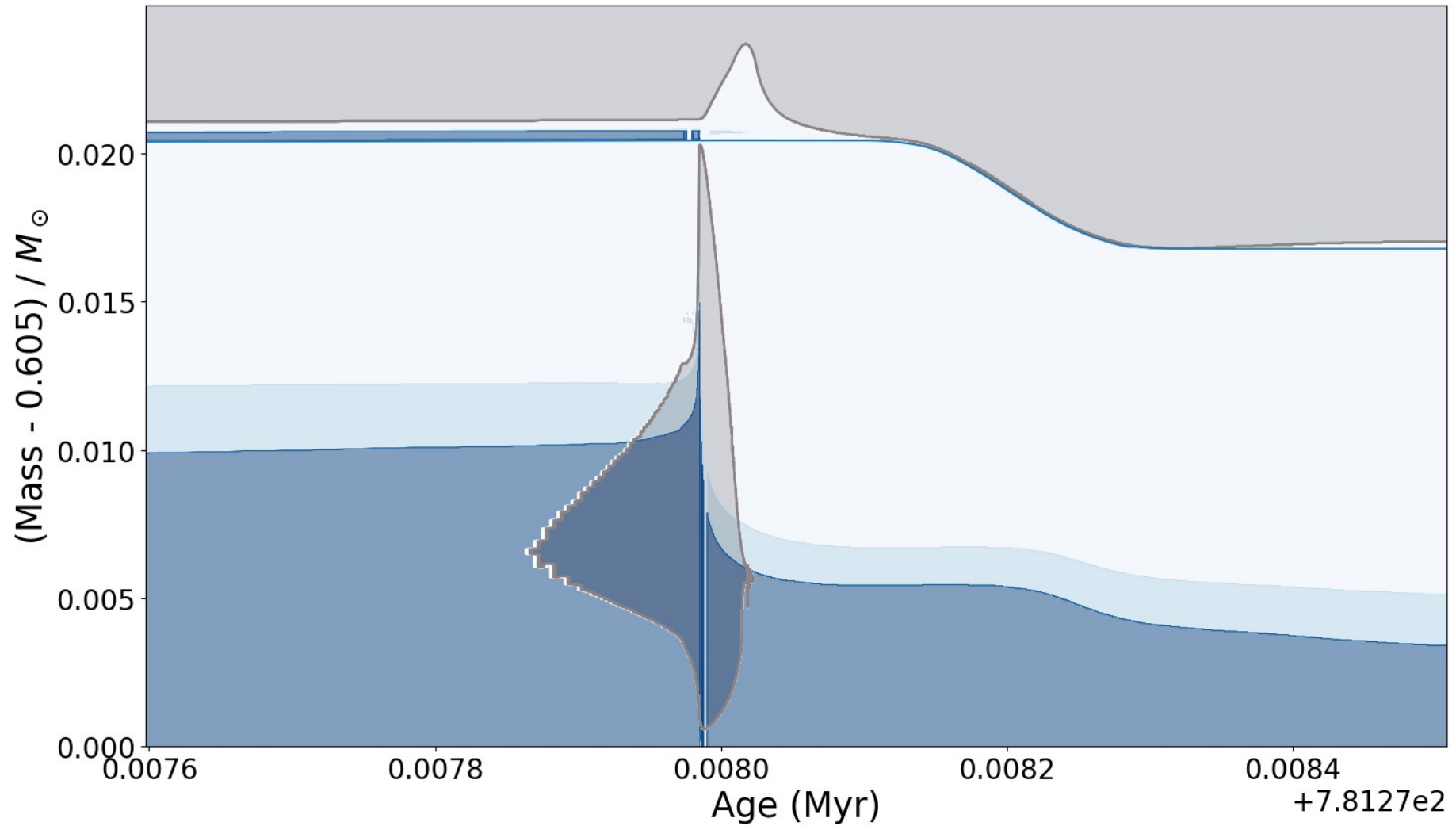


# 2.5 $M_{\odot}$ MESA model: AGB phase

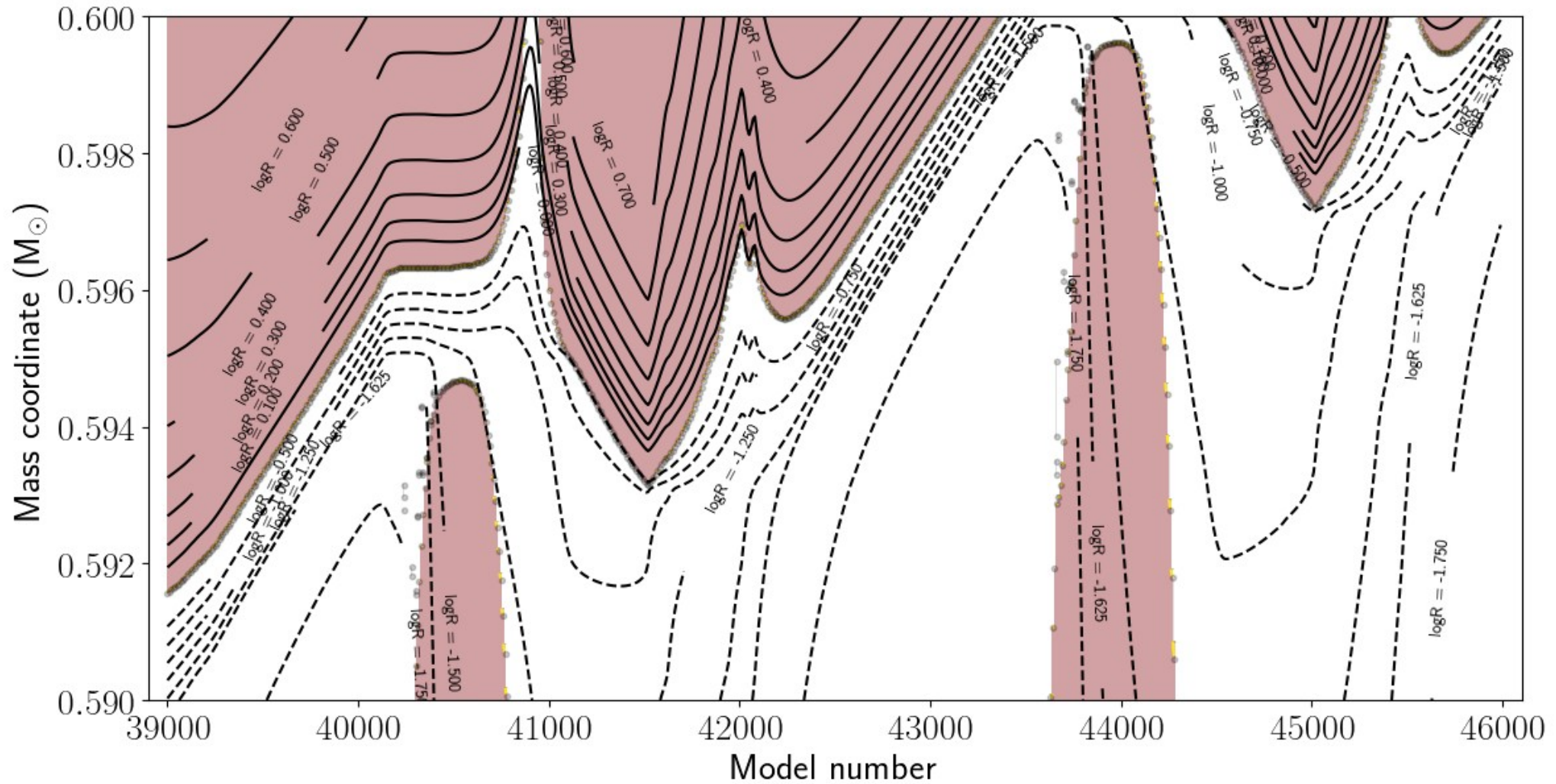


Den Hartogh et al (in prep)

# 2.5 $M_{\odot}$ MESA model: AGB phase

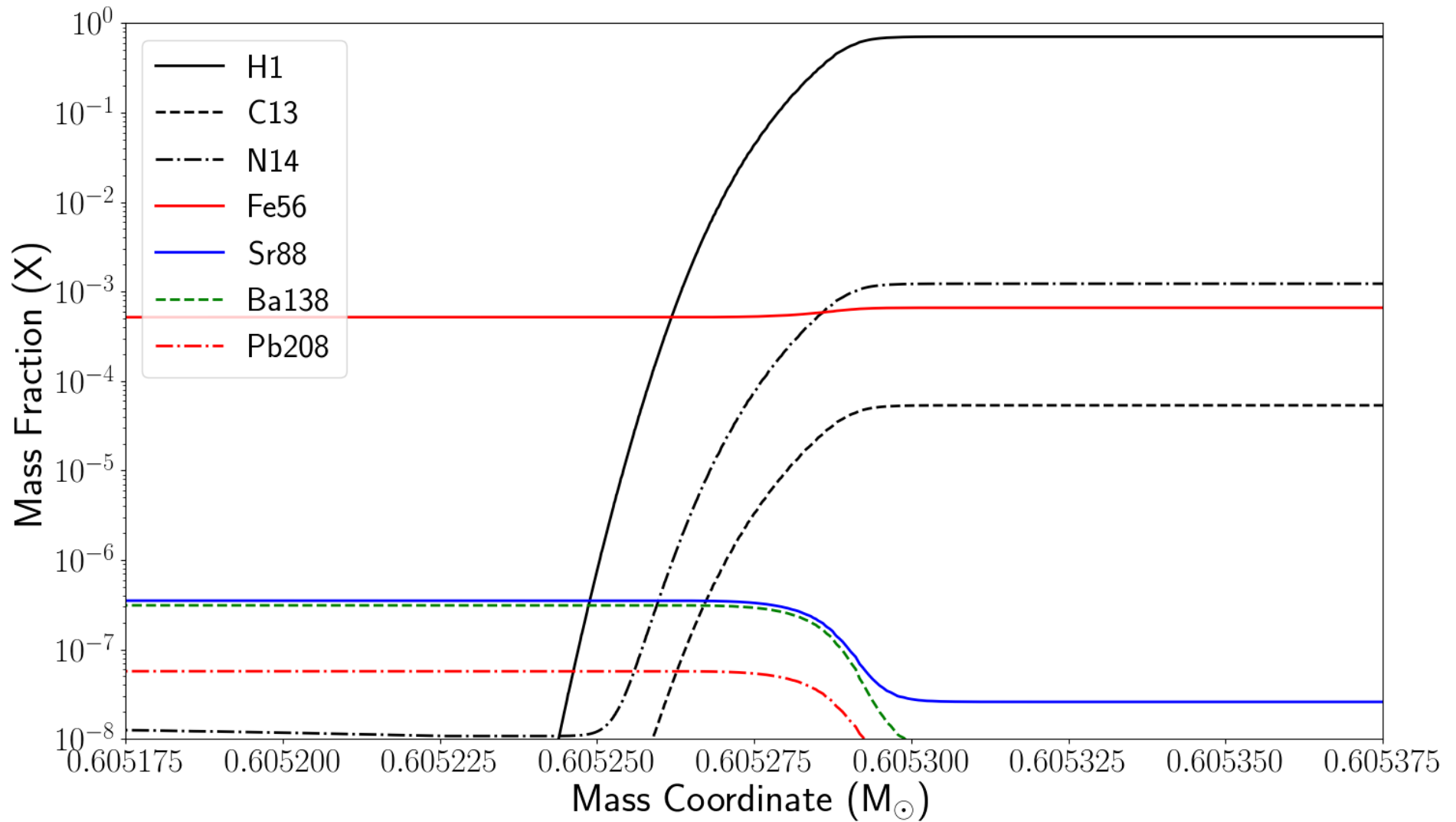


# 2.5 $M_{\odot}$ MESA model: AGB phase



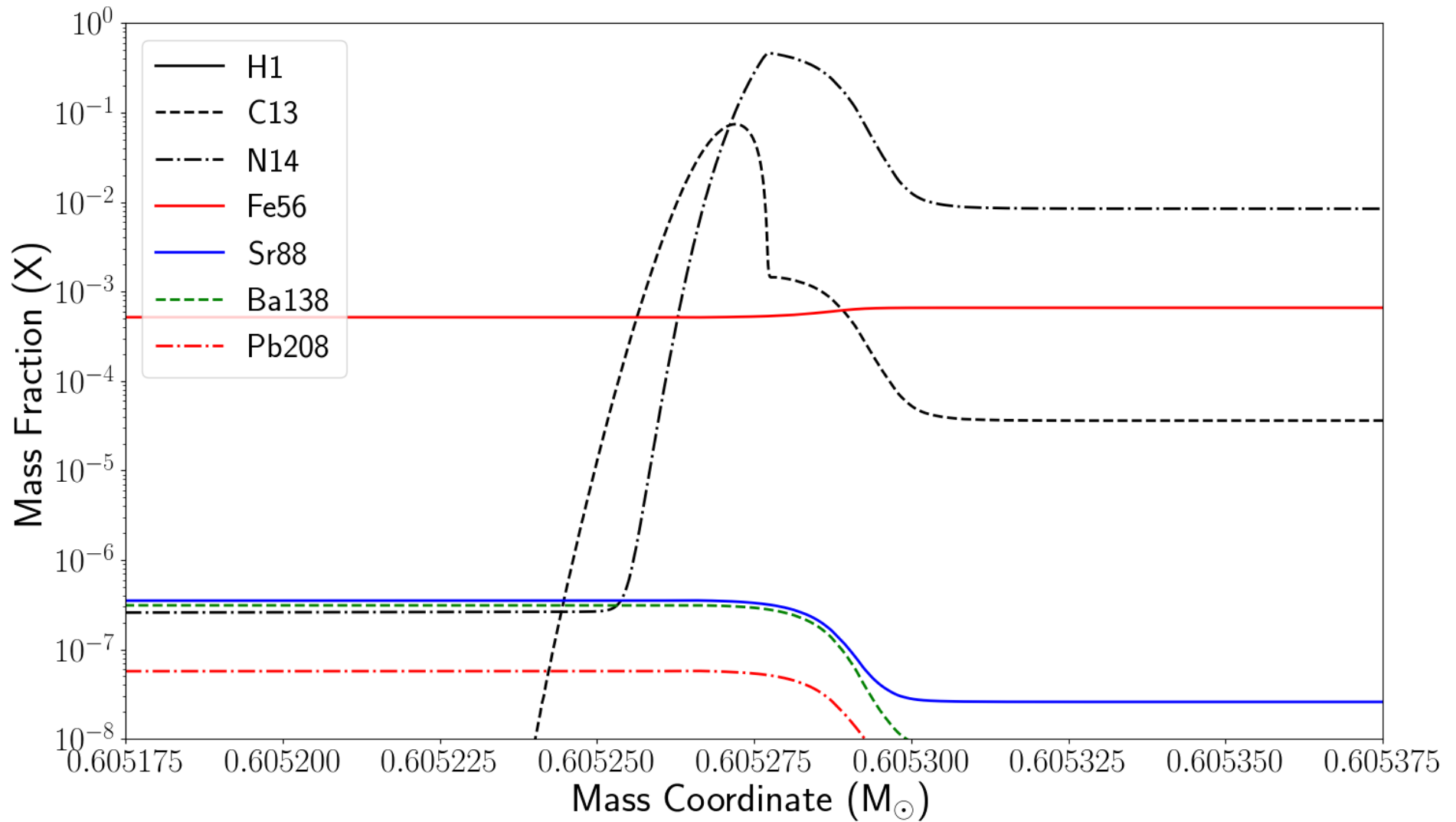


# *C-13 pocket formation*

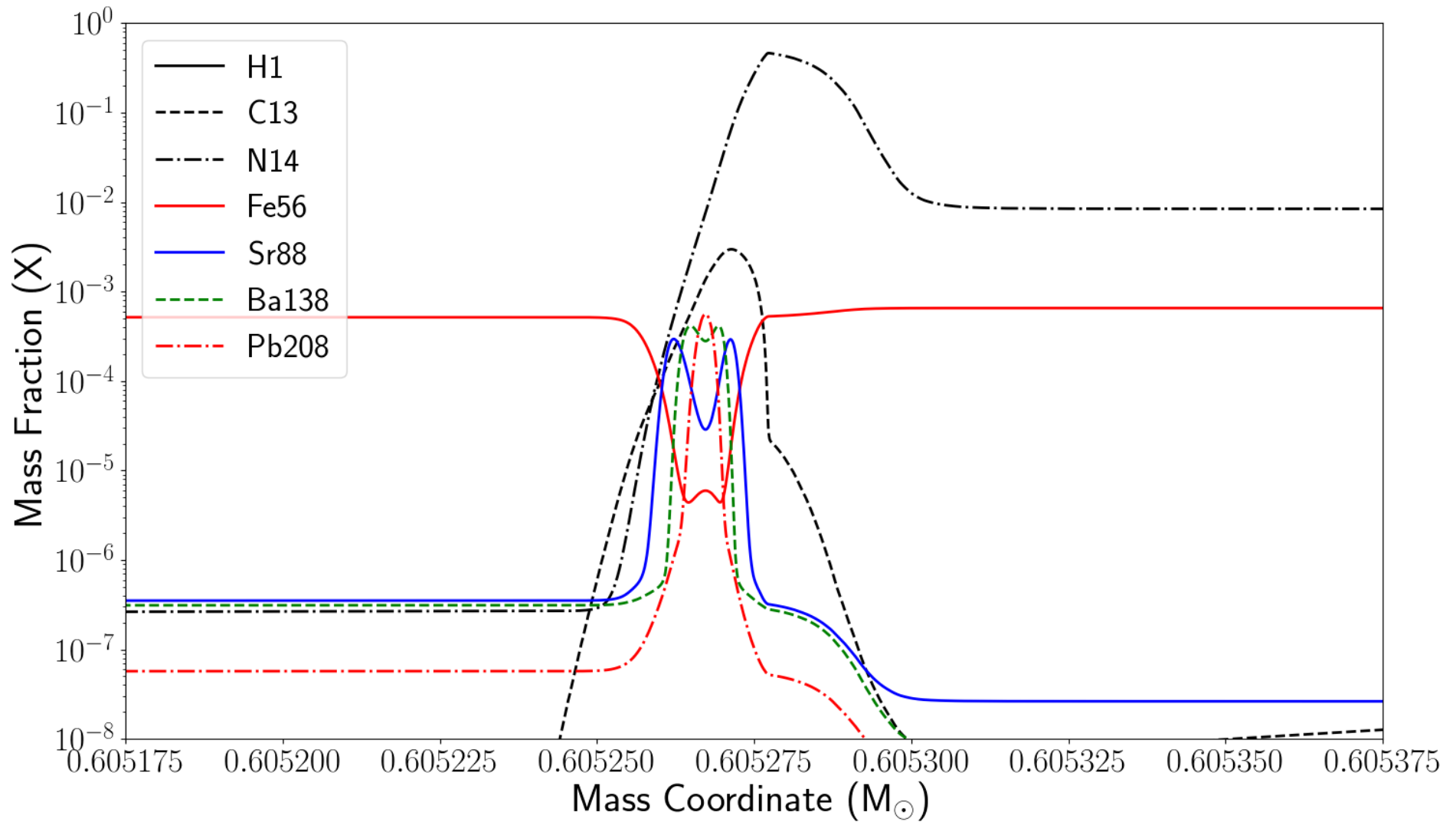




# *C-13 pocket formation*

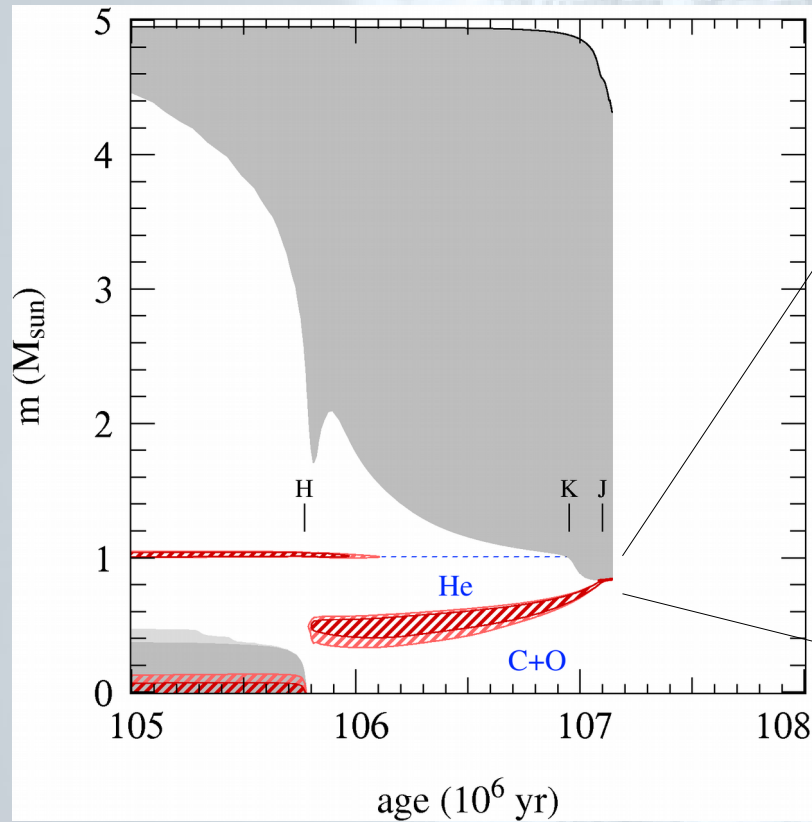


# *C-13 pocket formation*

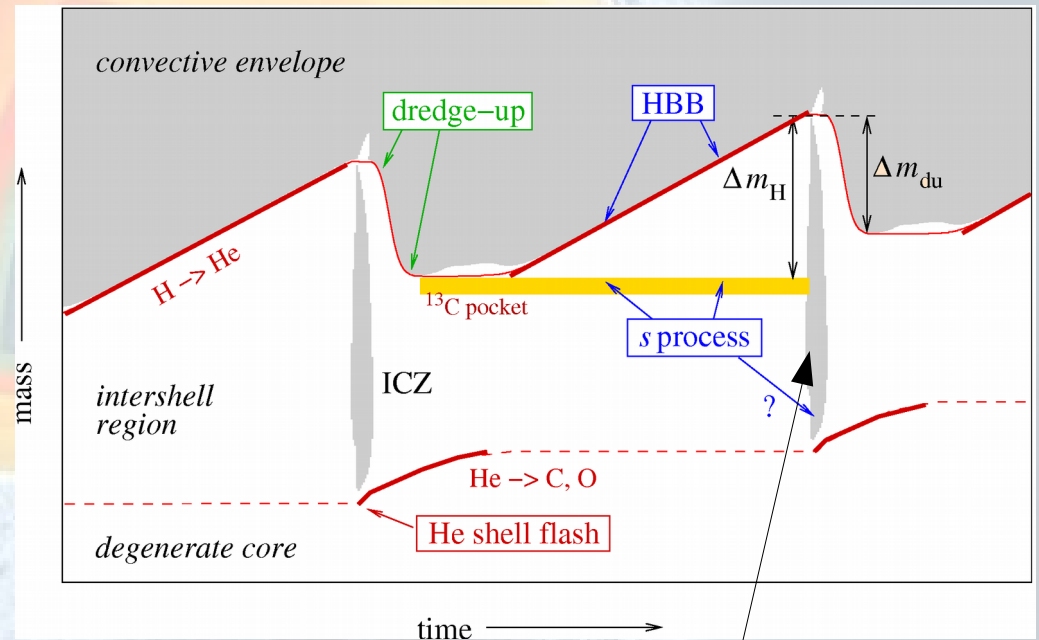


# Intermediate & Low-Mass Stars

5  $M_{\odot}$  star: AGB phase

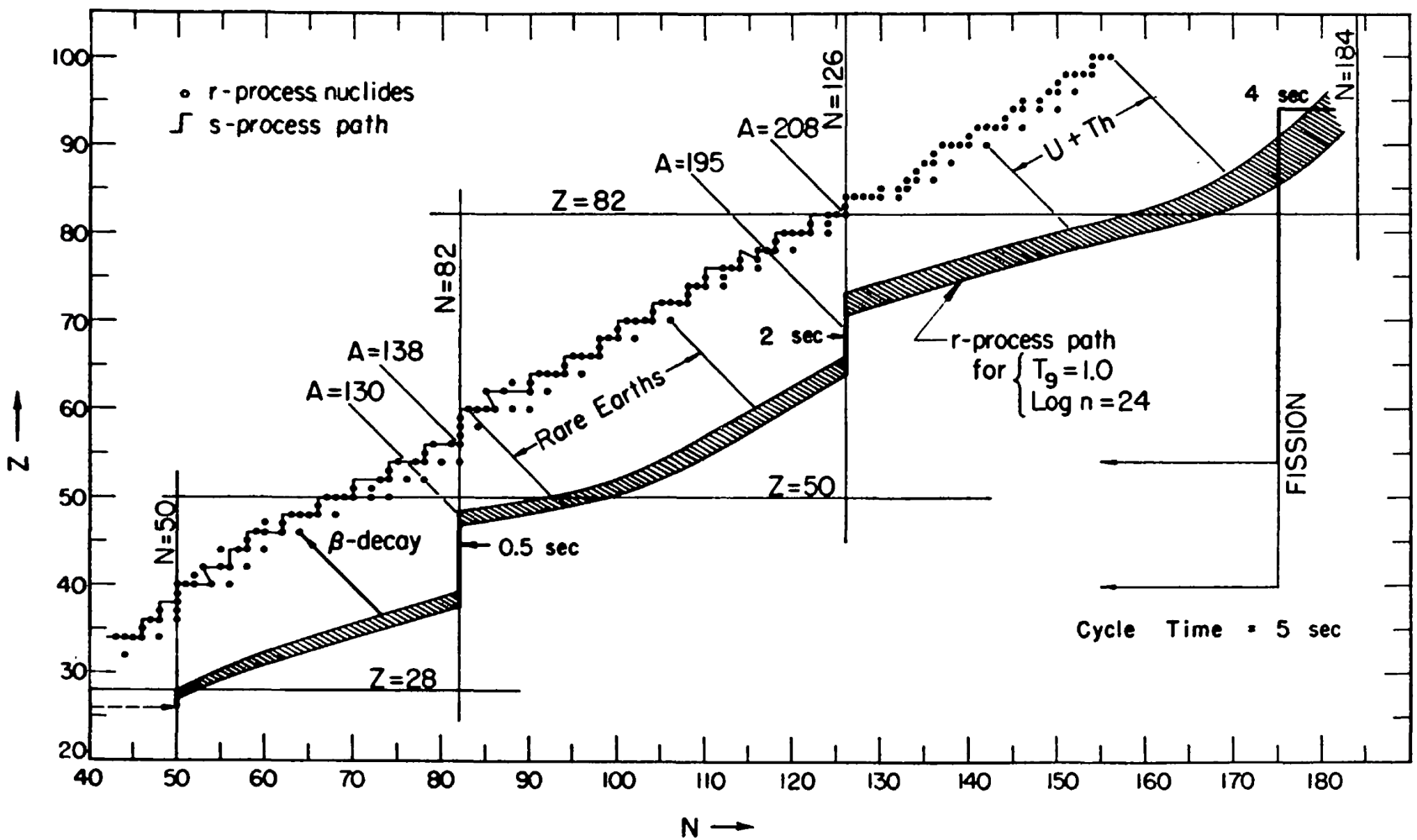


Structure in AGB phase



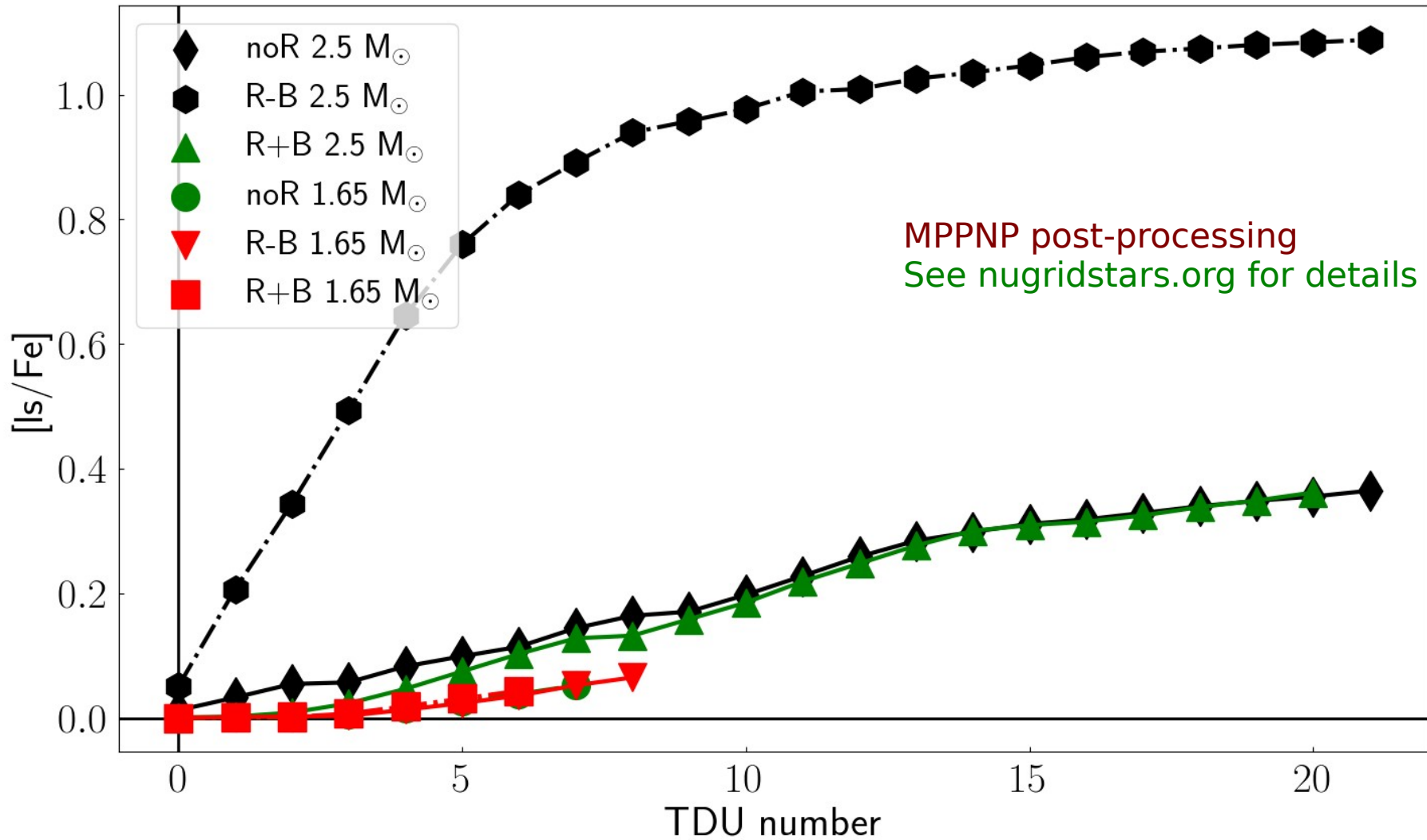
$^{22}\text{Ne}(a,n)$  contribution in TP

# S-process Production

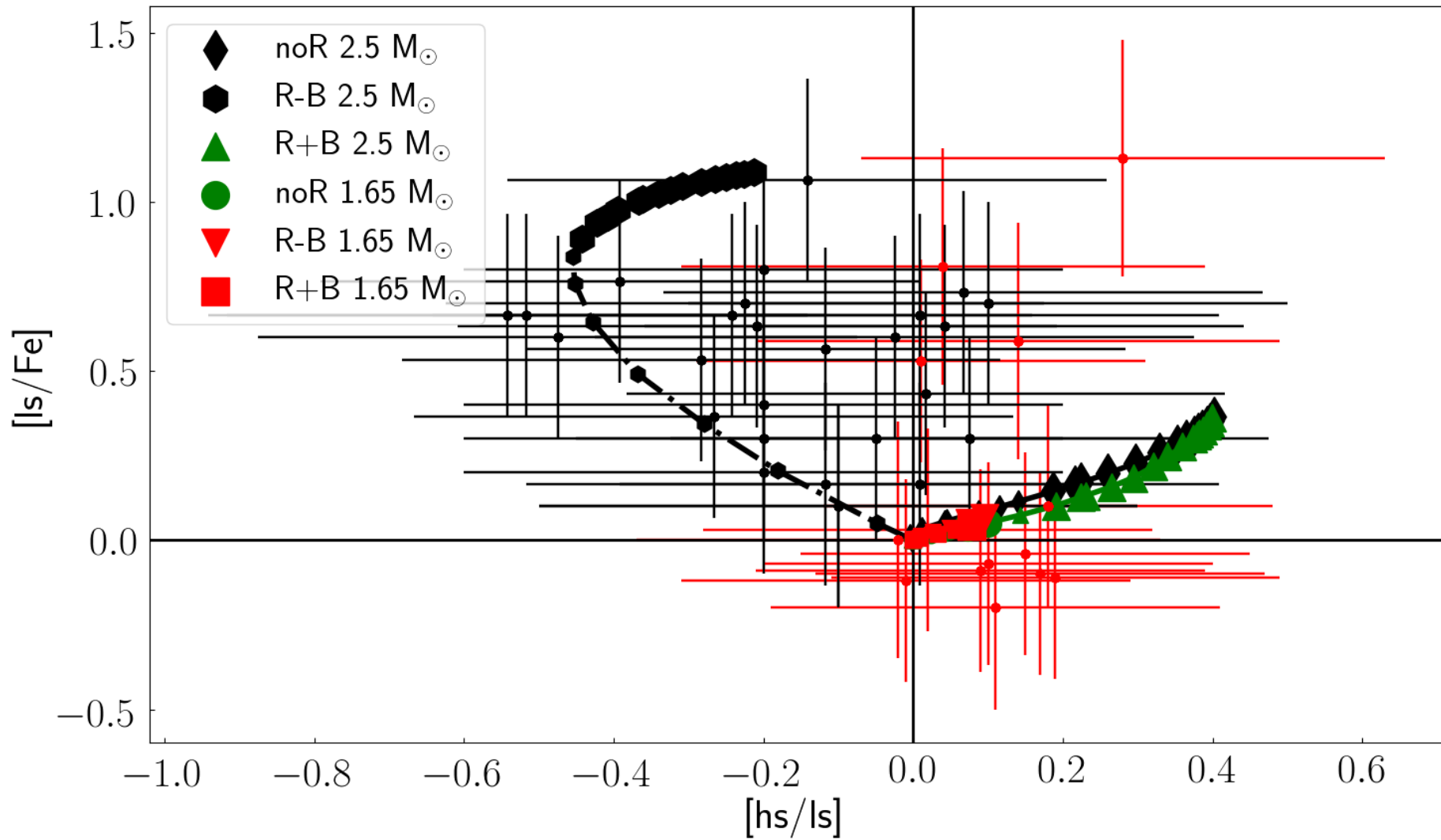


Seeger, Fowler & Clayton (1965)

# *S*-process Production



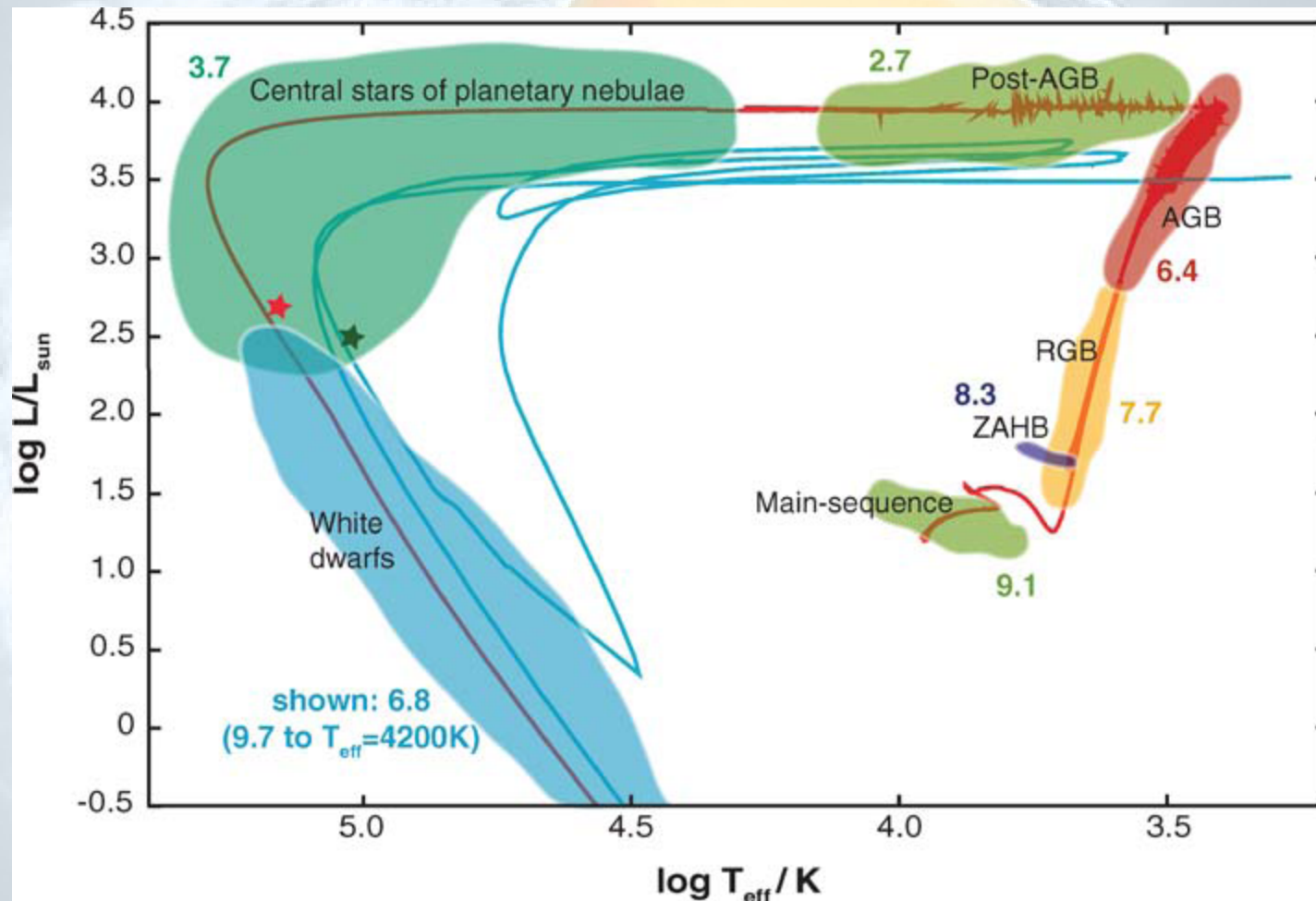
# *S*-process Production





# Intermediate & Low-Mass Stars

2  $M_{\odot}$  star: post-AGB phase



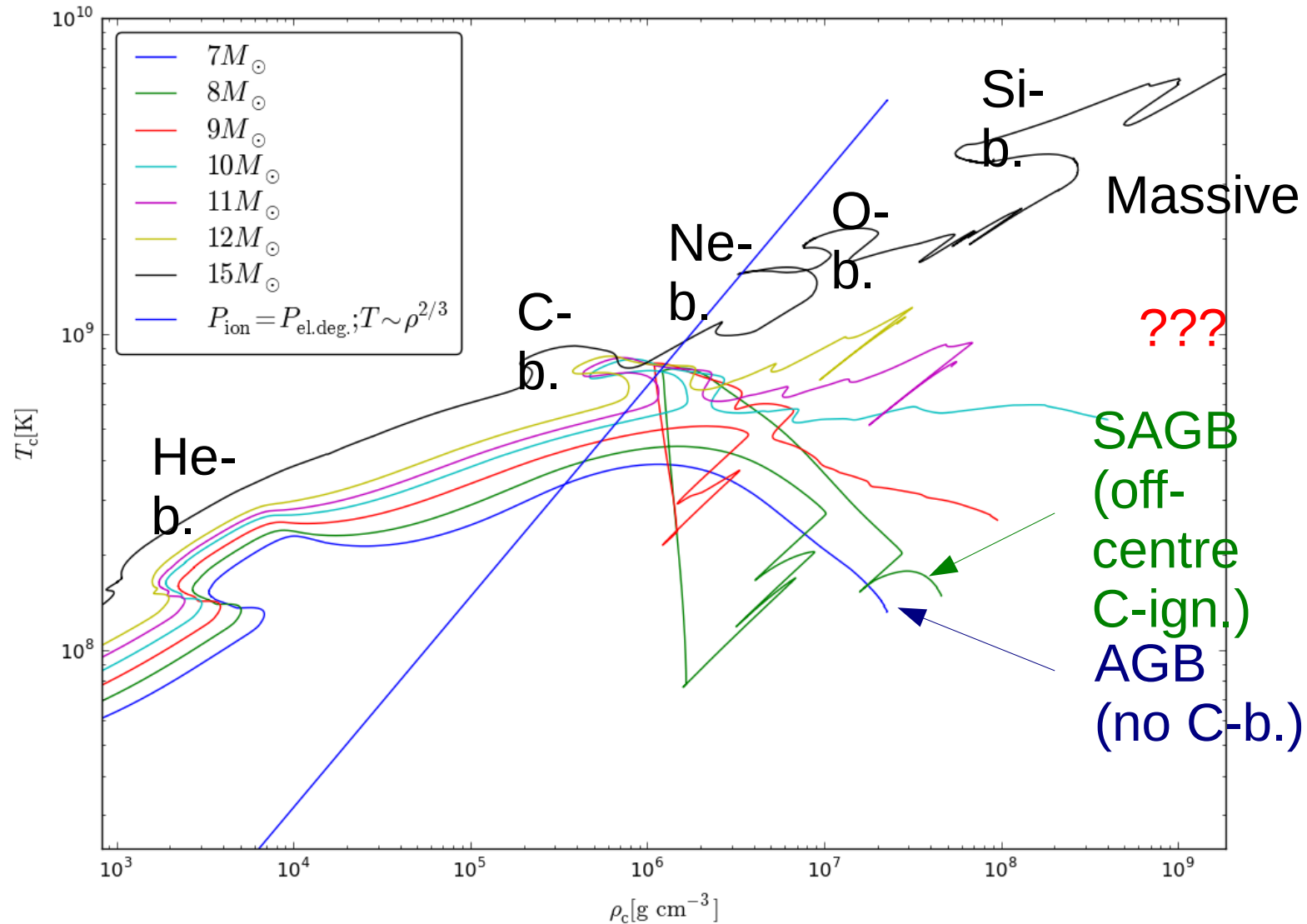
Herwig, ARAA, 2005

# Massive/AGB Stars Transition

7-15  $M_{\odot}$  models ← MESA stellar evolution code:

<http://mesa.sourceforge.net/>

Paxton et al 10



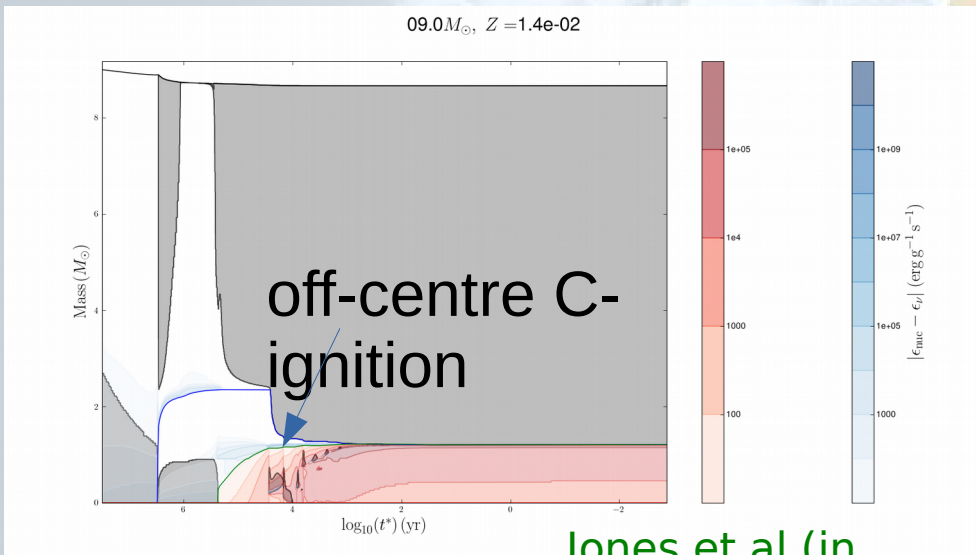
Jones et al 2013; see also Mueller et al 12, Umeda et al 12

# SAGB & ECSN progenitors

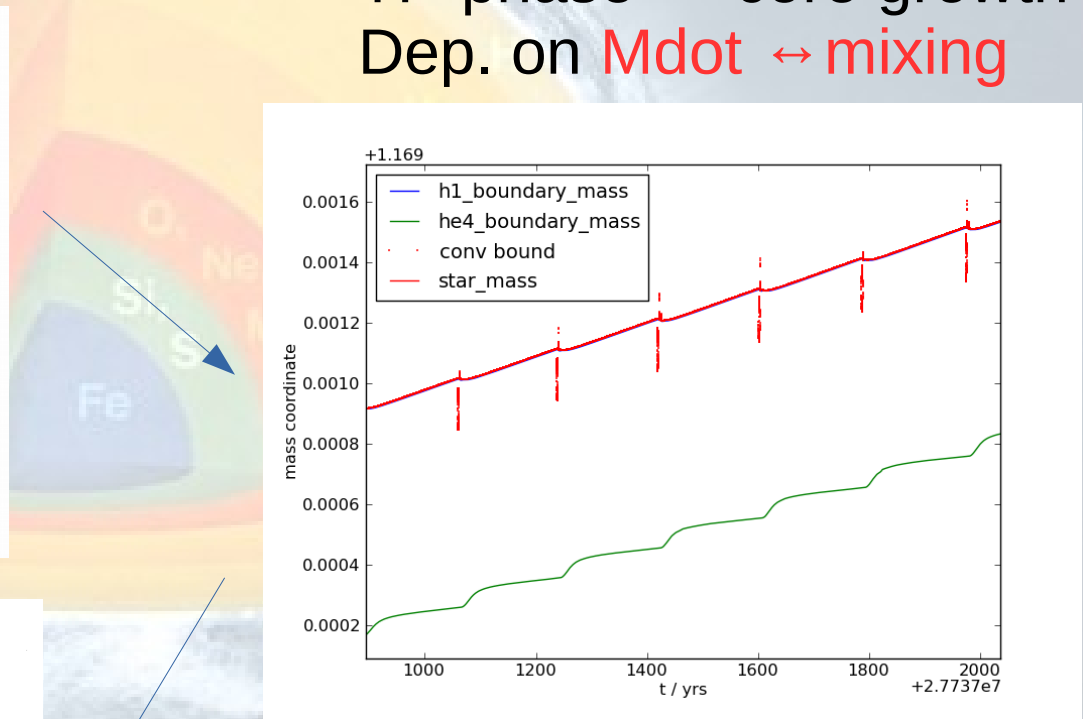
$M_{up} \leq M \leq M_{mas}$ ;  $M_{up} \approx 8M_{sun}$ ,  $M_{mas} \approx 10M_{sun}$  (TRANSITION MASSES)

Early evolution like AGBs;

TP-phase → core growth  
Dep. on  $\dot{M}$  ↔ mixing



Jones et al (in prep)



Jones et al (subm.)

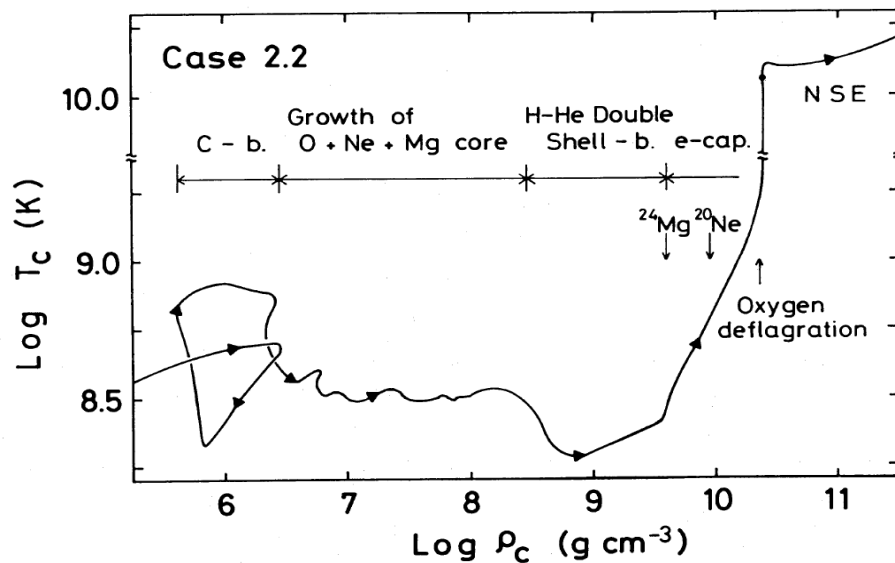
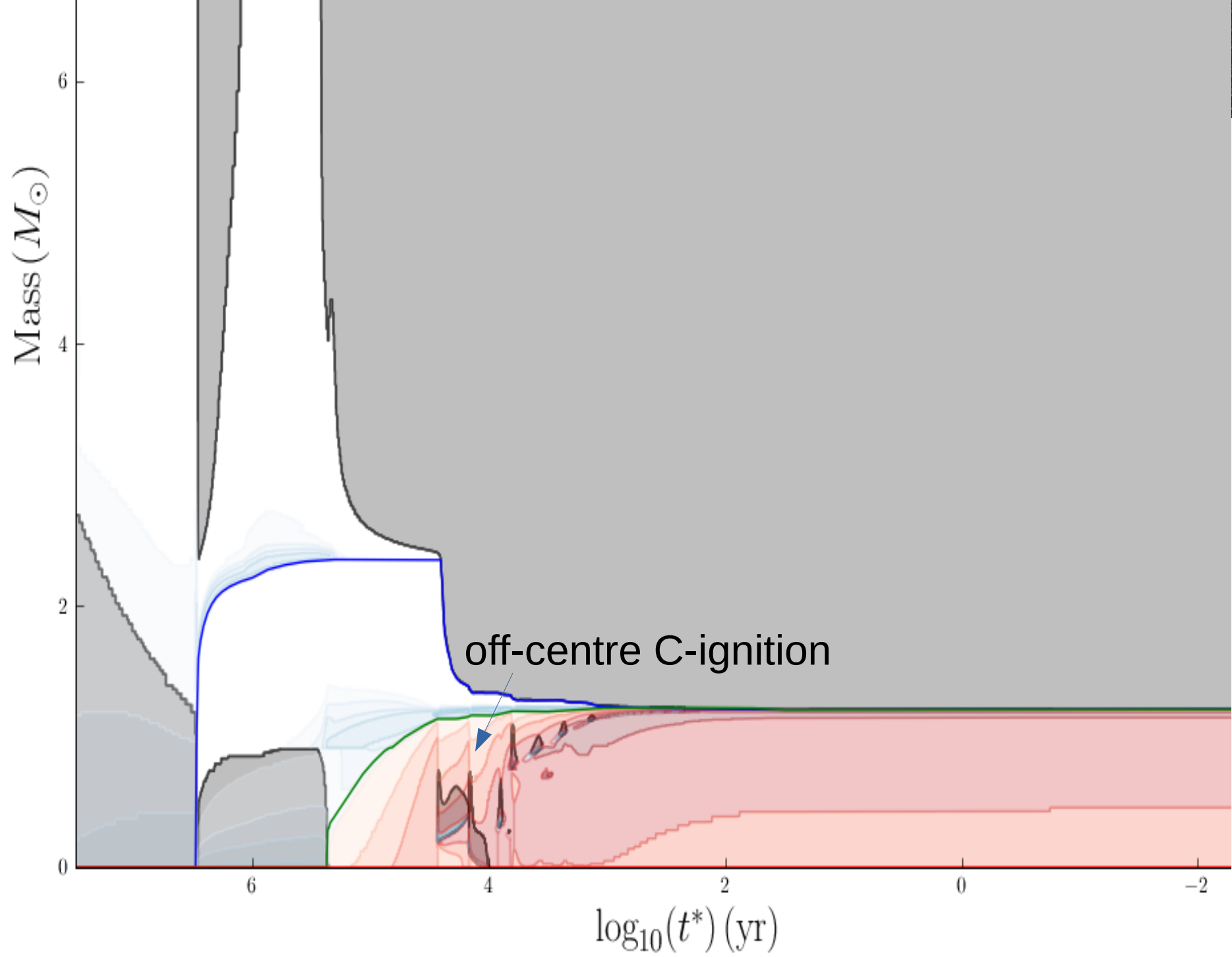


FIG. 4.—Evolutionary track in the central density and temperature diagram

Critical ONeMg core mass =  $M_{crit} = 1.375$

(Miyaji et al. 1980; Nomoto 1984)

See also: Miyaji (1980); Nomoto(1984, 1987); Miyaji & Nomoto (1987); Garcia-Berro, Ritossa and Iben (1990s); Eldridge & Tout (2004); L. Siess (2006, 2007, 2009, 2010), Poelarends (2008); Doherty et al. (2010) ...

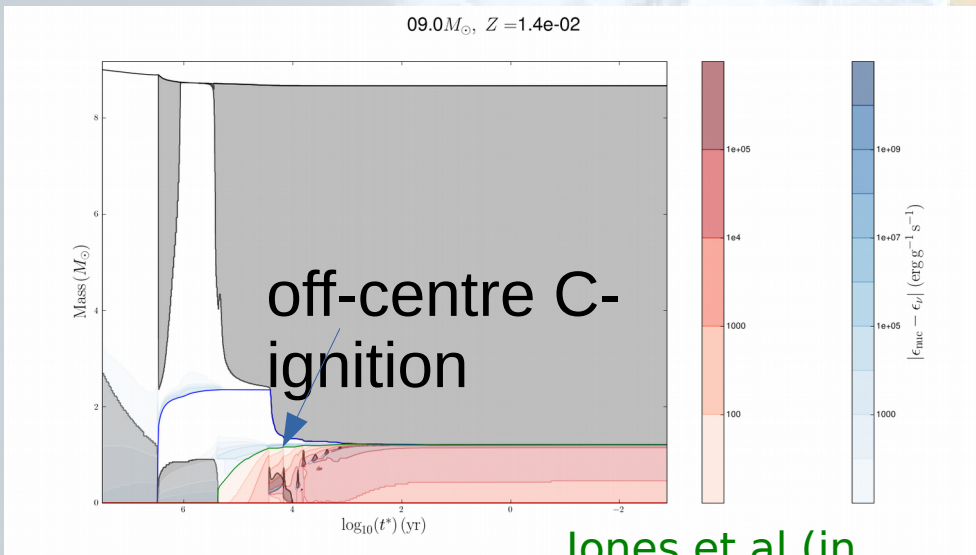


# SAGB & ECSN progenitors

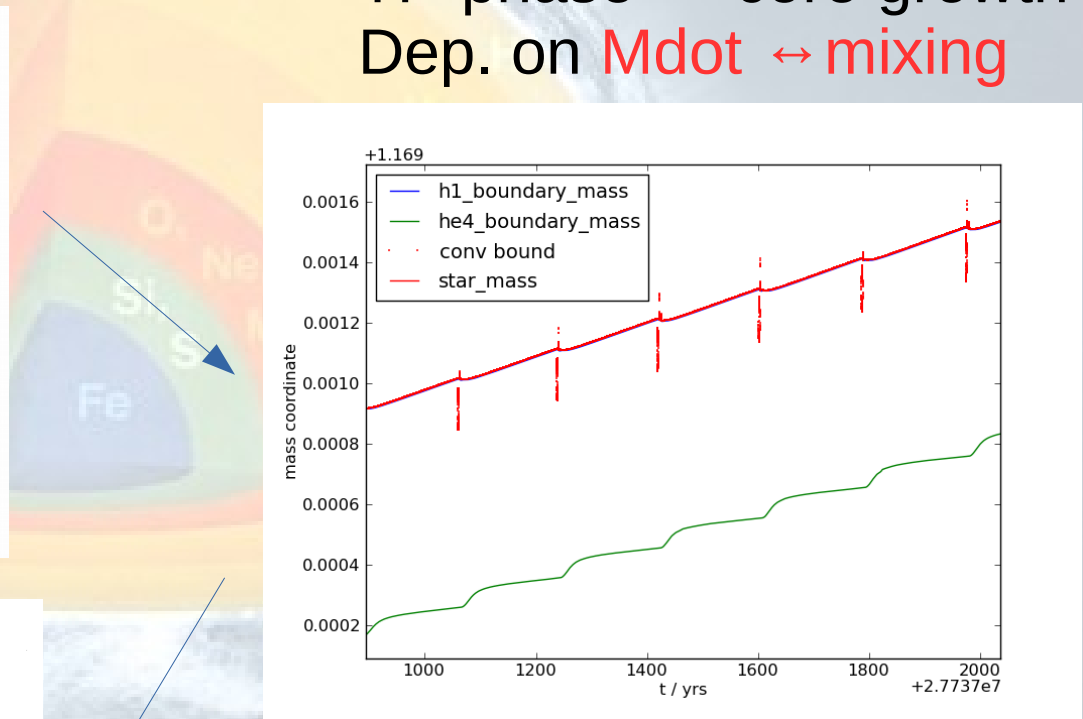
$M_{up} \leq M \leq M_{mas}$ ;  $M_{up} \approx 8M_{sun}$ ,  $M_{mas} \approx 10M_{sun}$  (TRANSITION MASSES)

Early evolution like AGBs;

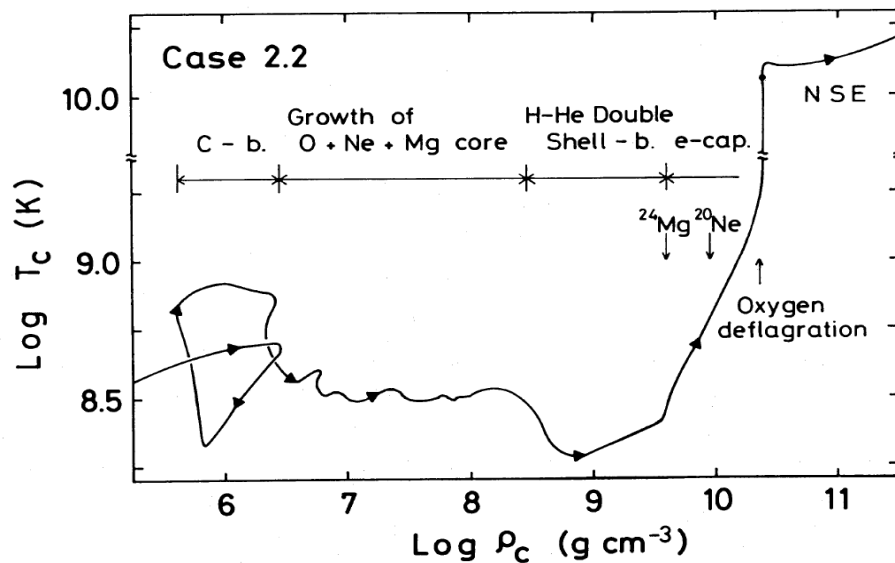
TP-phase → core growth  
Dep. on  $\dot{M}$  ↔ mixing



Jones et al (in prep)



Jones et al (subm.)



Critical ONeMg core mass =  $M_{crit} = 1.375$

(Miyaji et al. 1980; Nomoto 1984)

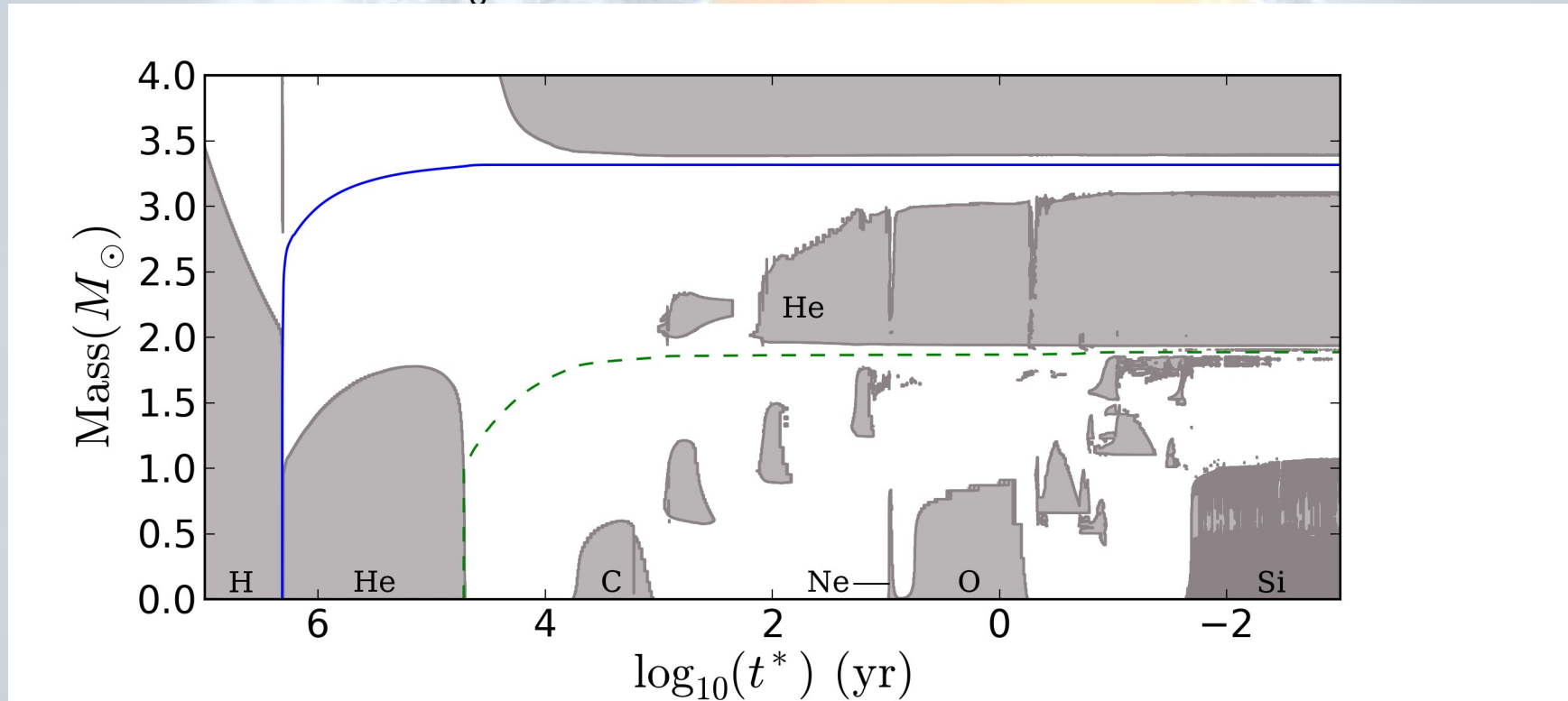
See also: Miyaji (1980); Nomoto(1984, 1987); Miyaji & Nomoto (1987); Garcia-Berro, Ritossa and Iben (1990s); Eldridge & Tout (2004); L. Siess (2006, 2007, 2009, 2010), Poelarends (2008); Doherty et al. (2010) ...

FIG. 4.—Evolutionary track in the central density and temperature diagram

# Can Massive Stars produce ECSN?

7-15  $M_{\odot}$  models ← MESA stellar evolution code **Paxton et al 10,12**

12  $M_{\odot}$  is a typical massive star:



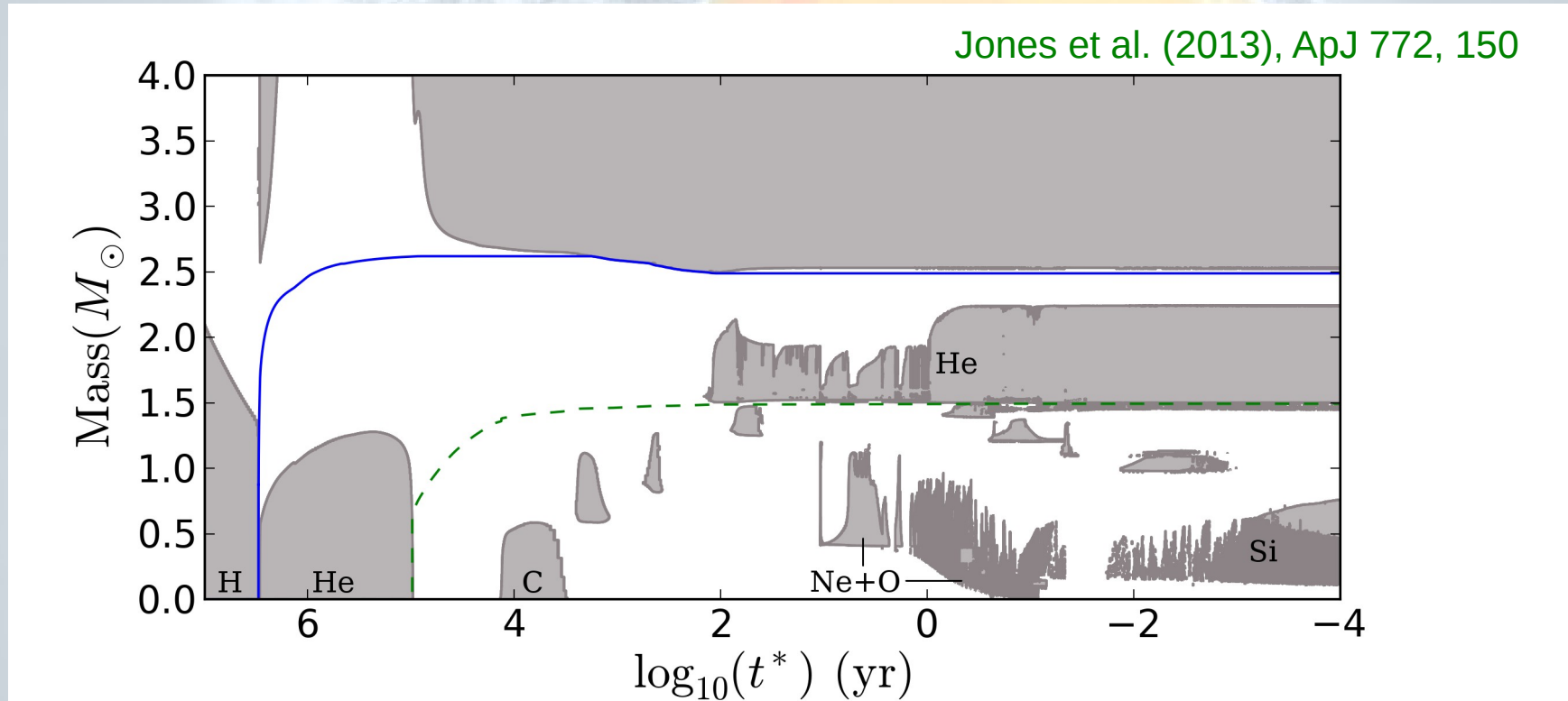
All burning stages ignited centrally. Fate: Fe-CCSN

**Jones et al. (2013), ApJ 772, 150;**  
**see also Mueller et al 12, Umeda et al 12, Takahashi et al 13**



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9.5  $M_{\odot}$  still a massive star:



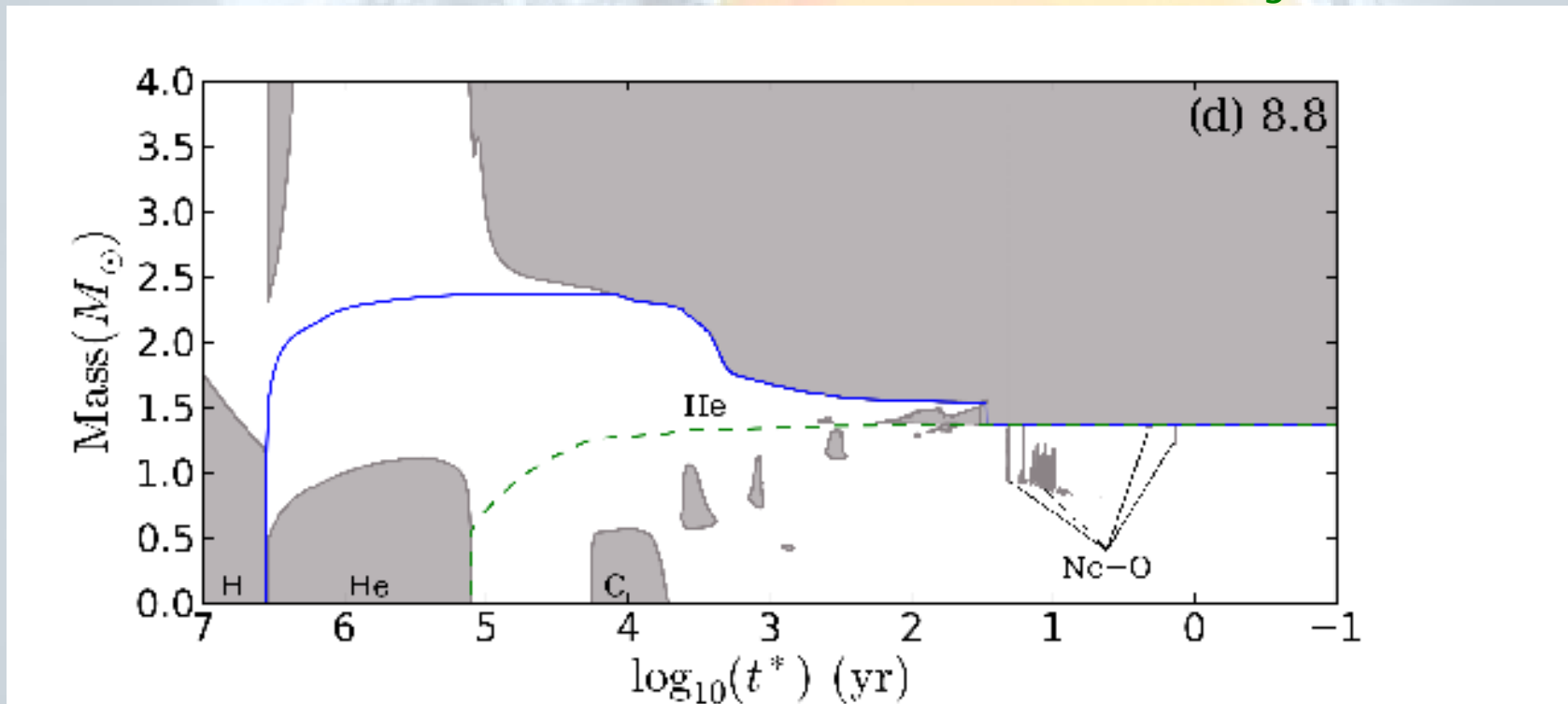
Ne-Si burning stages ignited off-centre. Fate: still Fe-CCSN

Simulations include 114-isotope network!

# Can Massive Stars produce ECSN?

Jones et al. (2013,...),  
ApJ 772, 150  
See also Nomoto 84: case 2.6  
Timmes et al 92,94  
Eldridge & Tout 04

8.8  $M_{\odot}$  failed massive star:



Ne-b. starts off-centre but does not reach the centre.

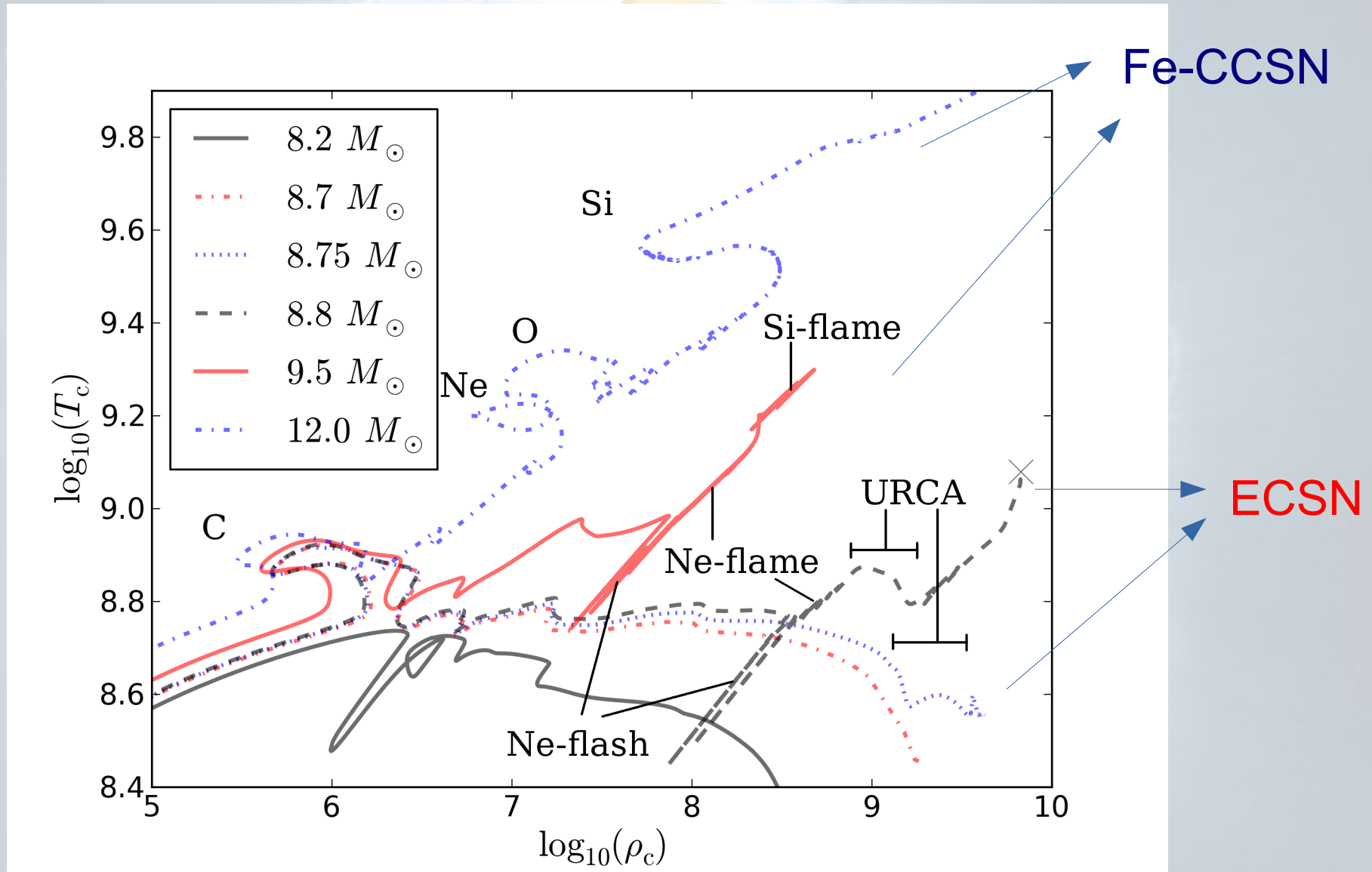
MESA → Oxygen deflagration

Agile-Bolztran for collapse + explosion (Jones et al 2016)

Fate: ECSN

Key uncertainties: convective boundary mixing, mass loss

# Fate of Least-Massive MS: ECSN/Fe-CCSN?



Jones et al. (2013), ApJ 772, 150

Both SAGB and failed massive stars may produce ECSN