

Stellar Evolution:
Course Overview,
Importance and Introduction



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Keele is Not Kiel (Germany) But Where is it?

West Midlands:



Keele area

is famous for pottery: Wedgwood, ...

and football: Stoke city fc in premier league



Plan

- Course overview
- Importance, evolution and fate of stars
- Stellar models & their physical ingredients
- EOS and partial degeneracy
- Mass domains
- Standard massive stars
- The most massive stars
- Stars at the boundary between massive and intermediate-mass stars



Lecture Plan

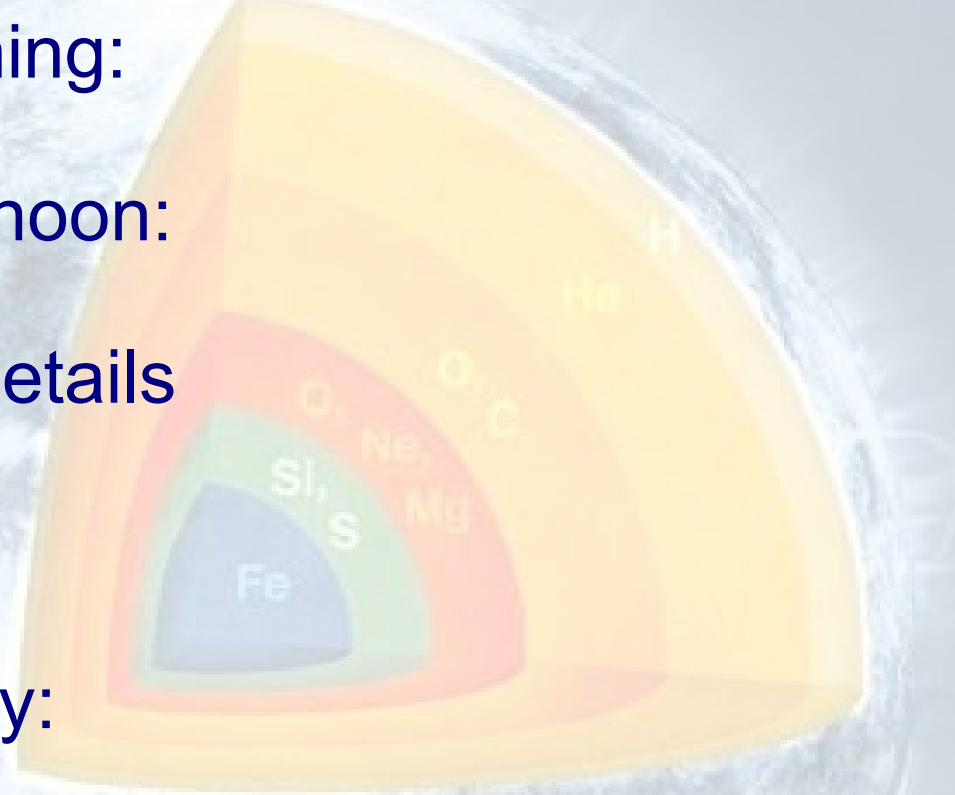
- 2 lectures every morning:
- Practicals in the afternoon:

See Google Drive for details

Questions:

Friday afternoon activity:

- 1-plot presentations by students
- Stellar yields compilation
- problem solving questions



Acknowledgements & Bibliography

- Slides in white background (with blue title) were taken from Achim Weiss' lecture slides, which you can find here: <http://www.mpa-garching.mpg.de/~weiss/lectures.html>

- A lot of content and some graphs were taken from Onno Pols' lecture notes on stellar evolution, which you can find here:

http://www.astro.ru.nl/~onnop/education/stev_utrecht_notes/

- Some slides (colourful ones) and content was taken from George Meynet's summer school slides.

- Link to slides from my lectures at the NICXIII school:

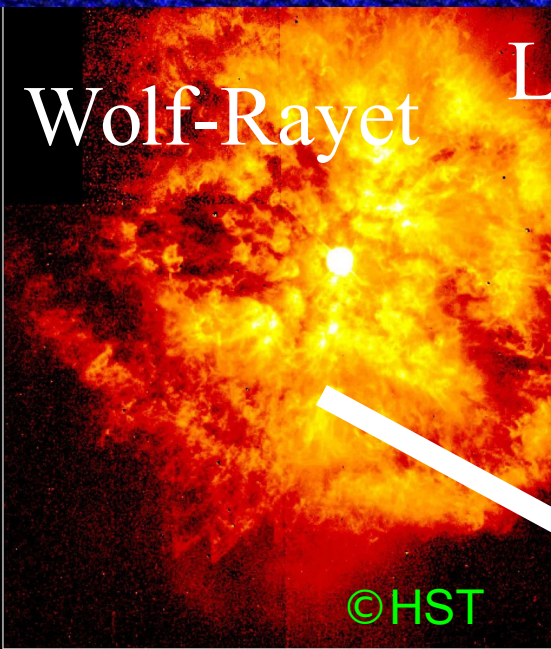
<http://www.atomki.hu/nic2014school/>

Acknowledgements & Bibliography

Recommended further reading:

- R. Kippenhahn & A. Weigert, *Stellar Structure and Evolution*, 1990, Springer-Verlag, ISBN 3-540-50211-4 (Recent update by Weiss et al.)
- A. Maeder, *Physics, Formation and Evolution of Rotating Stars*, 2009, Springer-Verlag, ISBN 978-3-540-76948-4
- D. Prialnik, *An Introduction to the Theory of Stellar Structure and Evolution*, 2000, Cambridge University Press, ISBN 0-521-65937-X
- C.J. Hansen, S.D. Kawaler & V. Trimble, *Stellar Interiors*, 2004, Springer-Verlag, ISBN 0-387-20089-4
- M. Salaris & S. Cassisi, *Evolution of Stars and Stellar Populations*, 2005, John Wiley & Sons, ISBN 0-470-09220-3

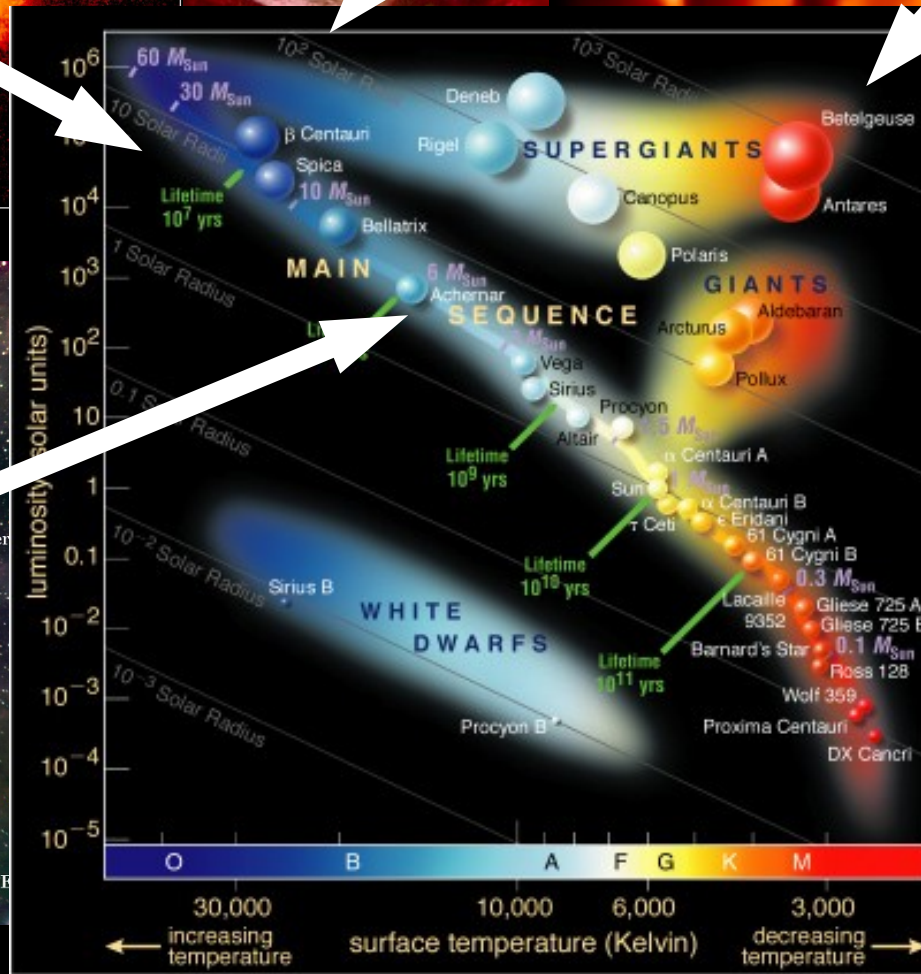
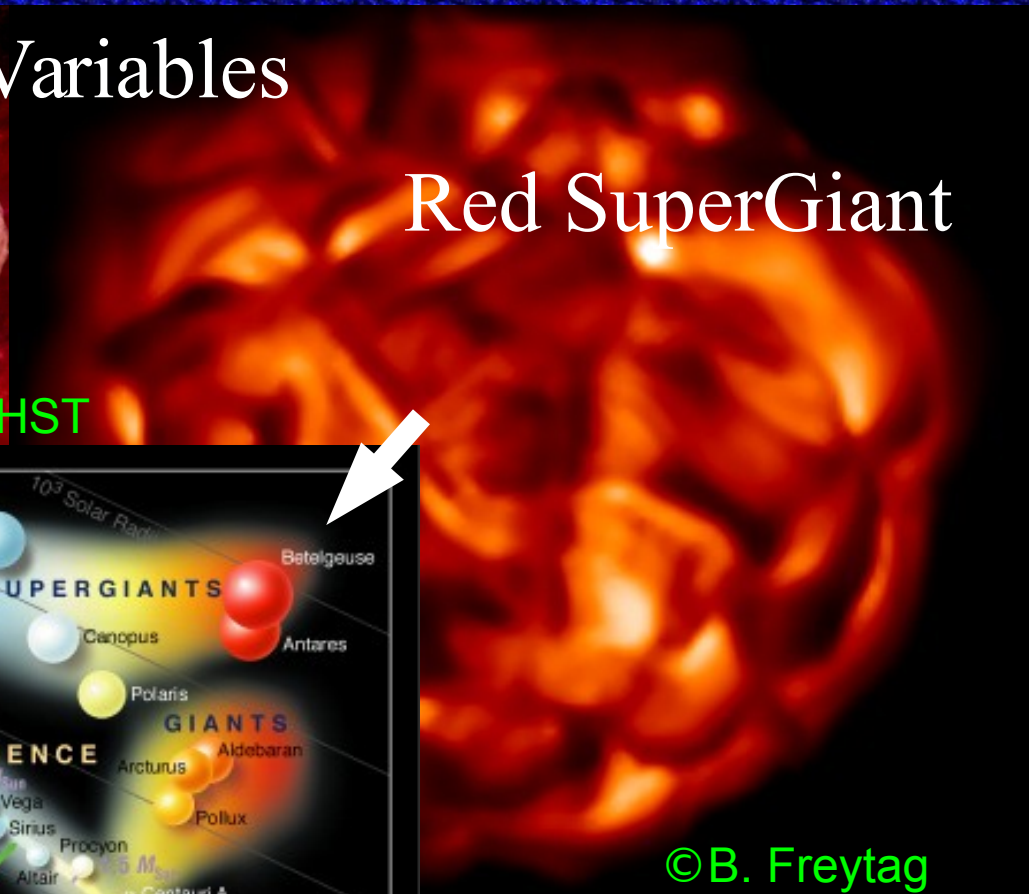
Massive Stars: Importance as *Stellar Objects*



Luminous Blue Variables

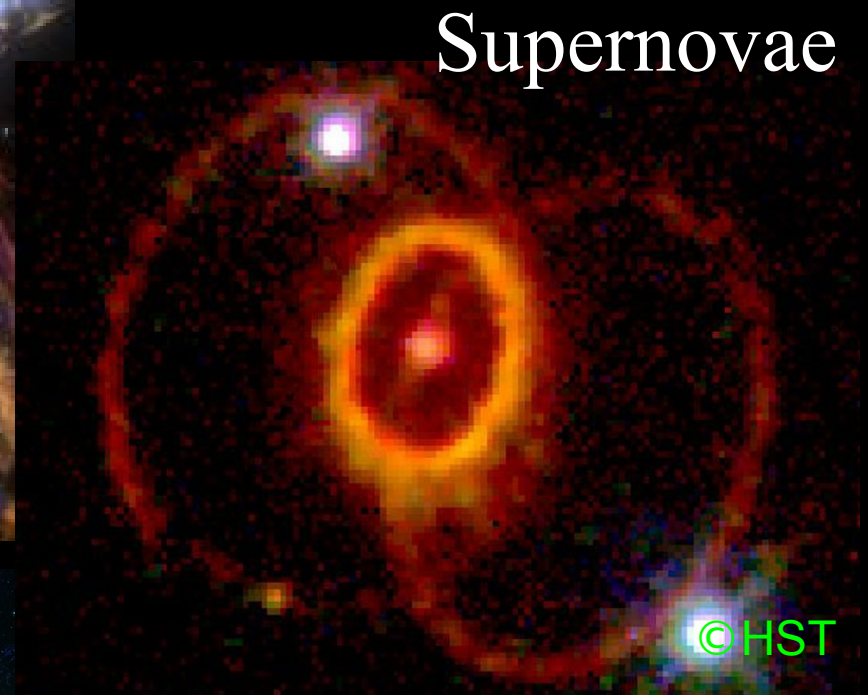


Red SuperGiant



©B. Mendez

Importance as *Progenitors*

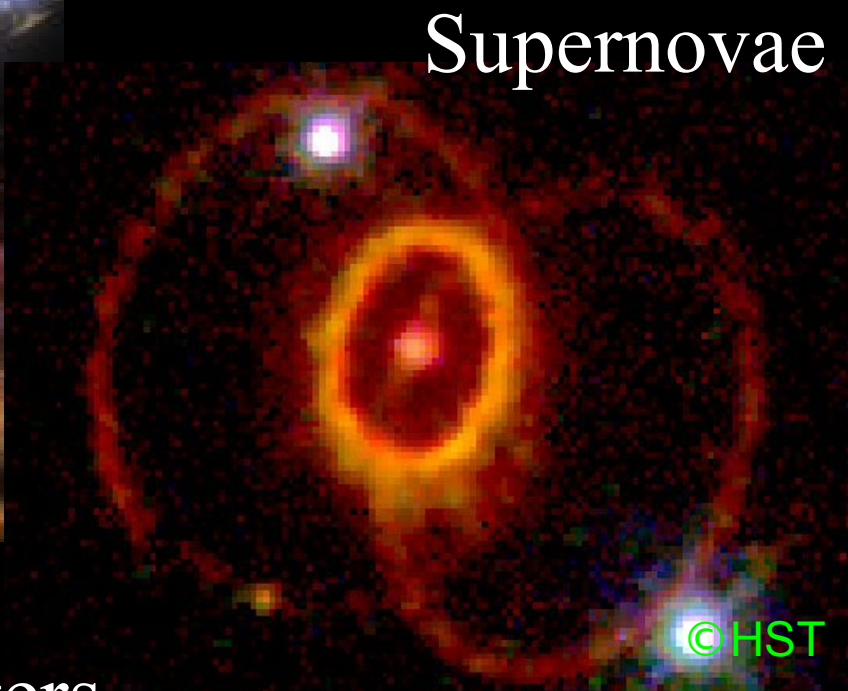


Massive Stars: Importance as Progenitors



©NASA

GRBs



Supernovae

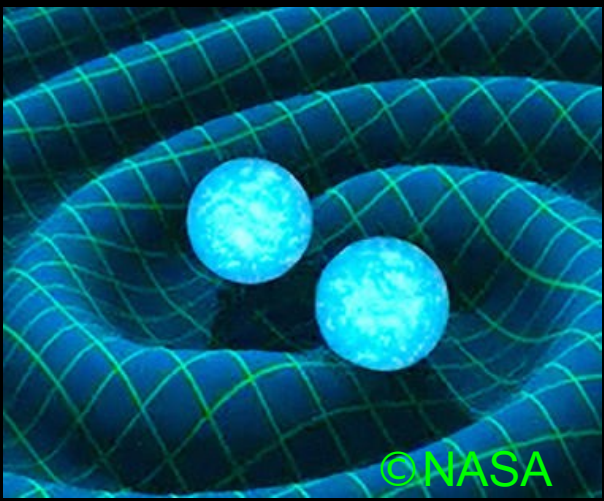
©HST

Neutron Stars



©STScI

GWs ← mergers



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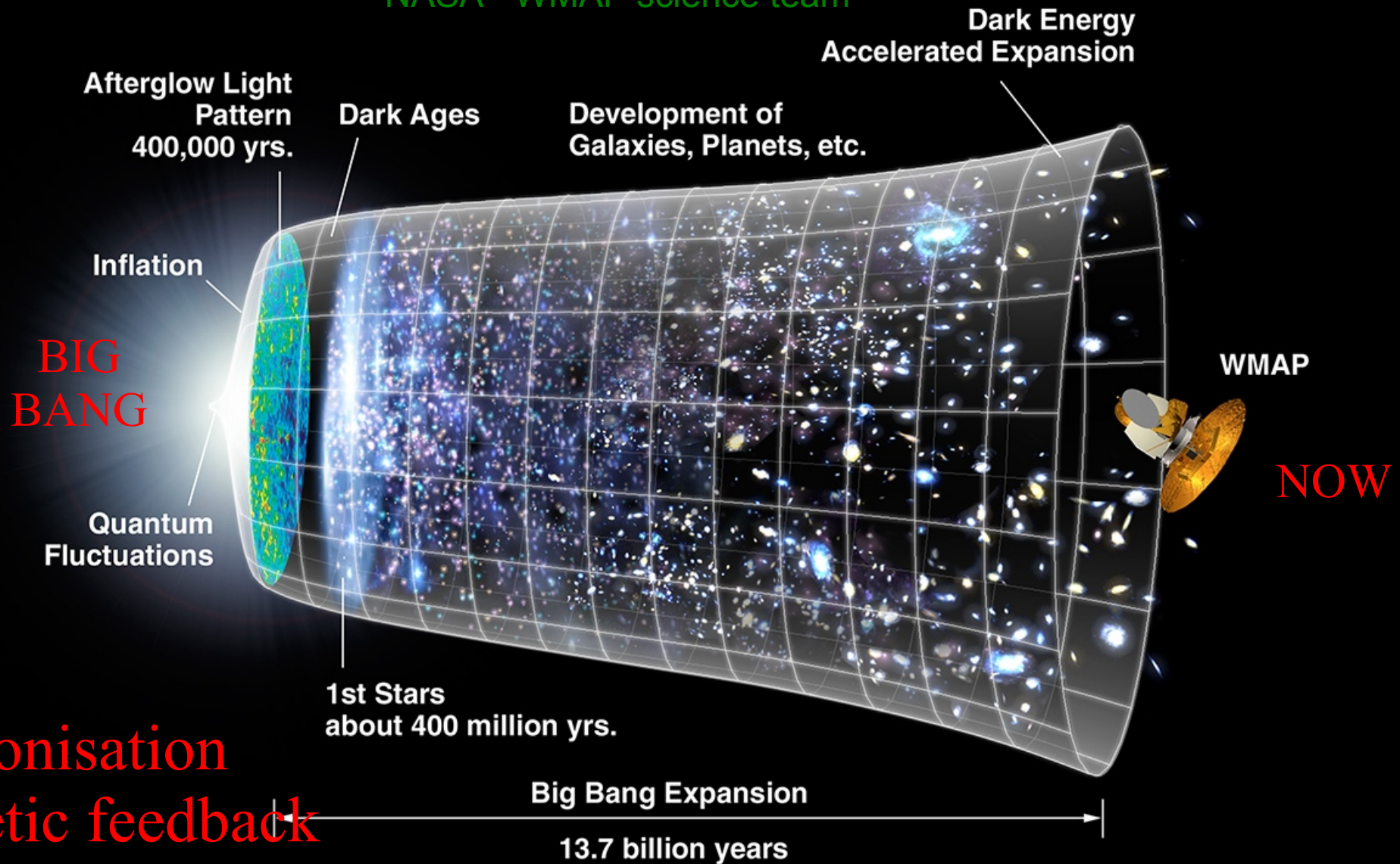
Black Holes



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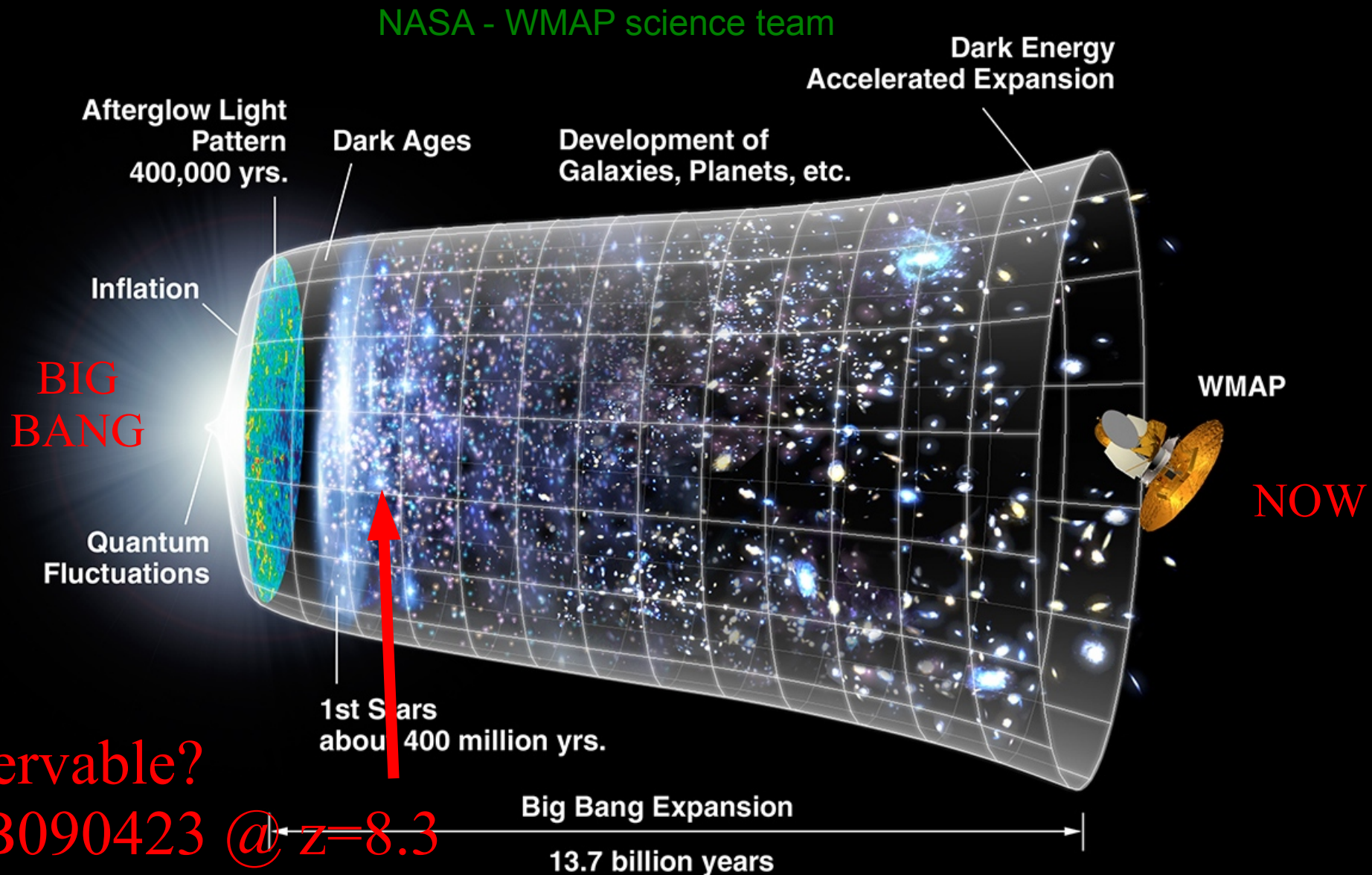
First Stellar Generations: Importance

NASA - WMAP science team



- Re-ionisation
- Kinetic feedback
- Chemical feedback observed in EMP stars

First Stellar Generations: Importance

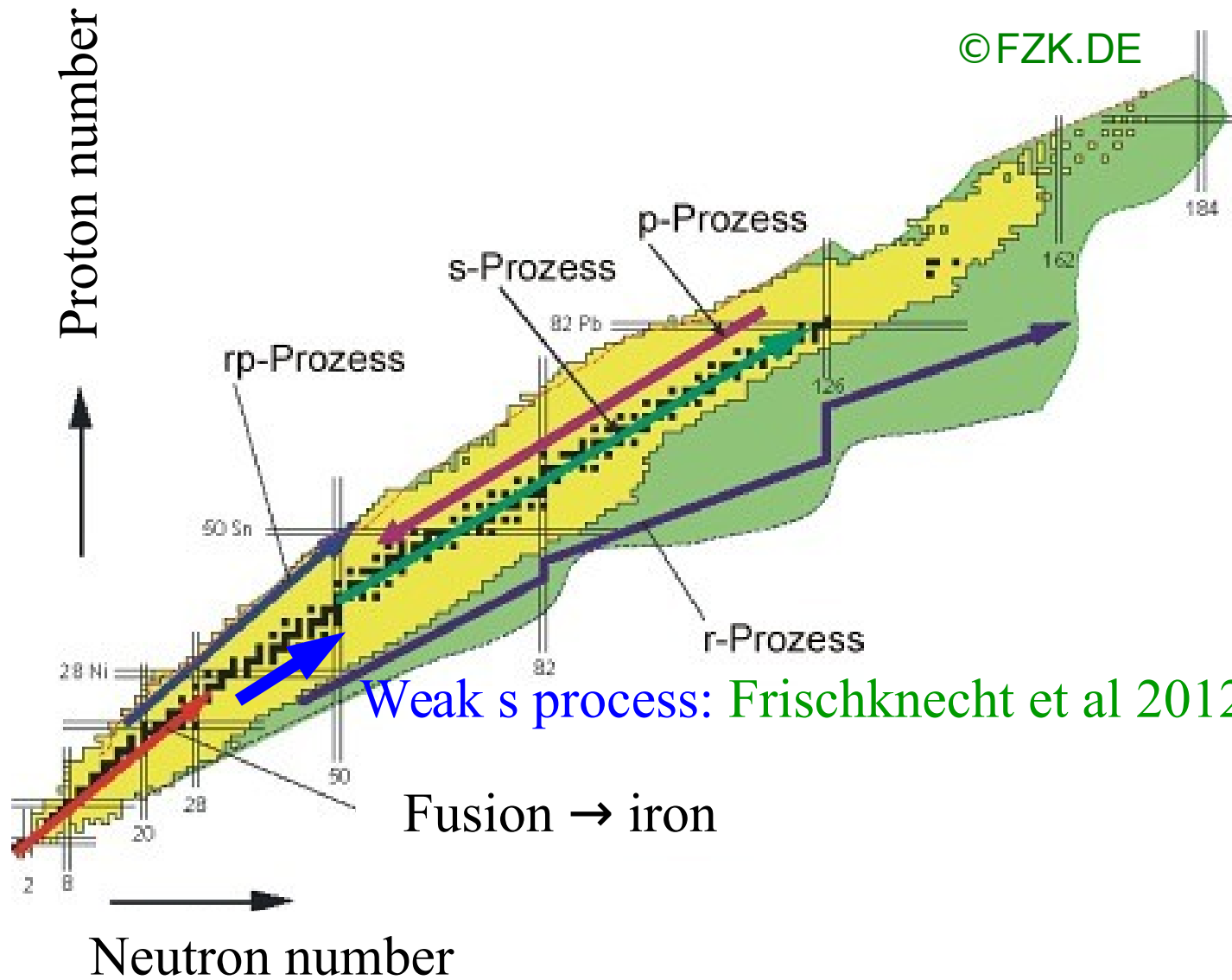


- Observable?

- GRB090423 @ $z=8.3$

Universe age ~ 600 Myr (Tanvir et al 09 Nature: arXiv:0906.1577)

Stars: Importance for *Nucleosynthesis*

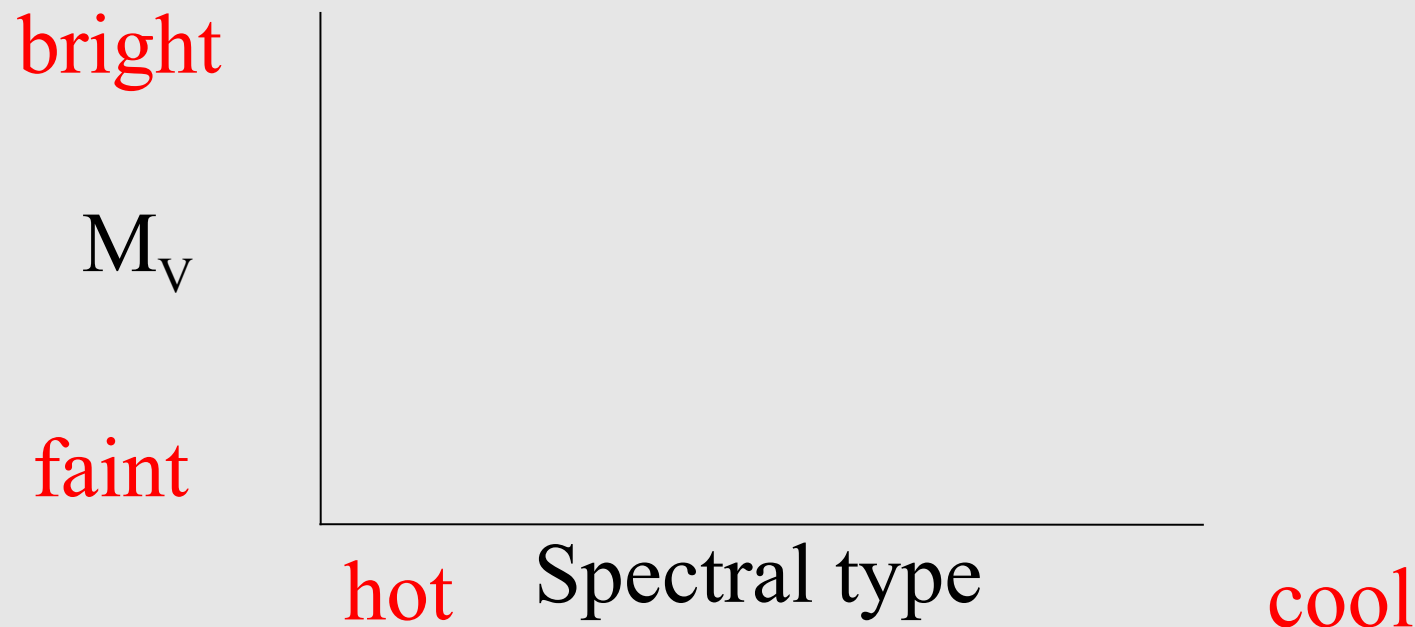


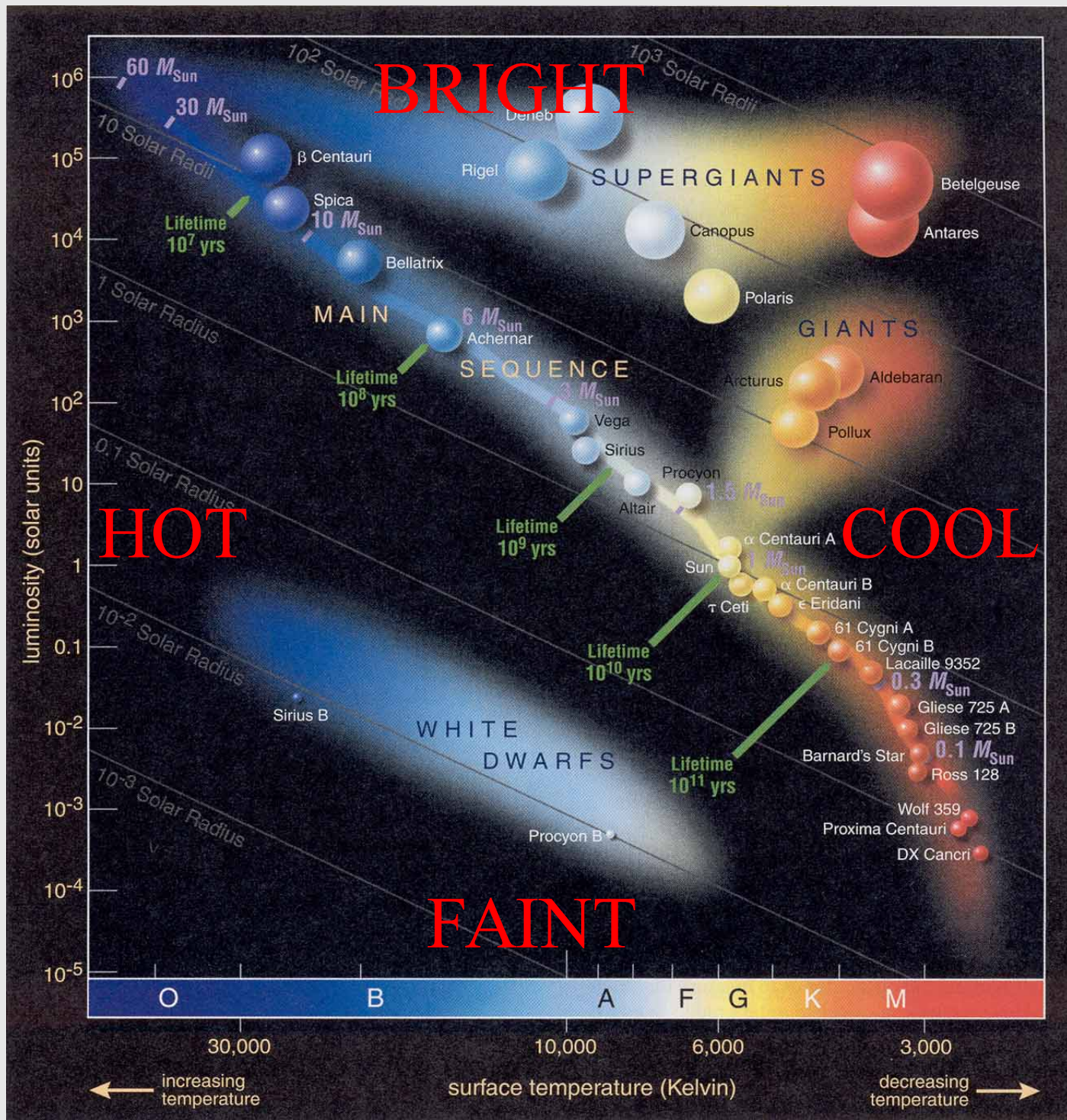
Information about Stars from Observations

- Photometry → apparent brightness
- astrometry (parallax) → distances
- Spectroscopy → many surface properties:
temperature, gravity, chemical composition, rotation, winds
- Orbit+eclipses of binary stars → masses, radii
- Interferometry → angular diameter → radius
- Asteroseismology → speed of sound → internal structure
- Neutrinos / gravitational waves → core properties

The Hertzsprung-Russell Diagram

- A very useful diagram for understanding stars
- We plot two major properties of stars:
 - Temperature (x) vs. Luminosity (y)
 - Spectral Type (x) vs. Absolute Magnitude, M_V (y)



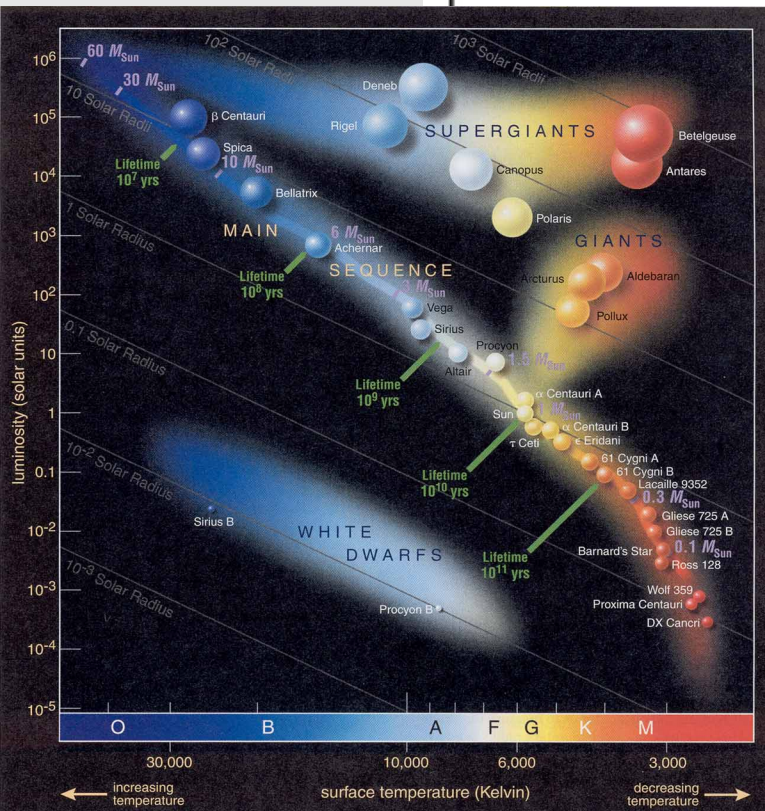


Stellar Luminosity

How can two stars have the same temperature, but vastly different luminosities?

Stellar Luminosity Classes

Class	Description
I	Supergiants
II	Bright giants
III	Giants
IV	Subgiants
V	Main sequence



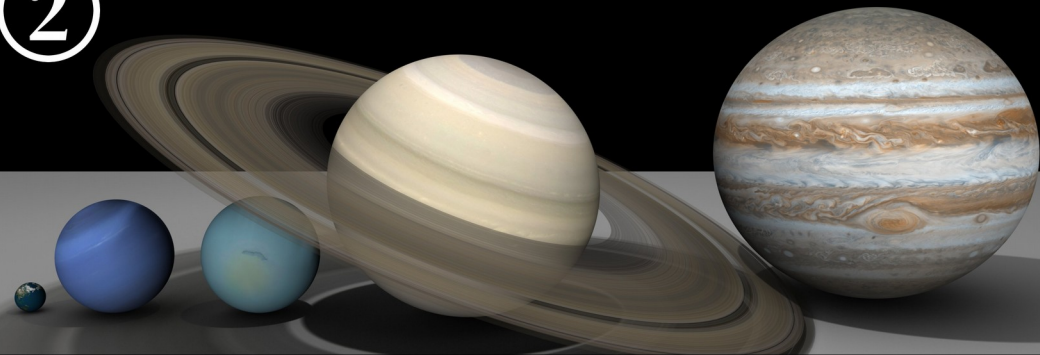
Radius of largest stars is larger than 1 AU!

The Most Voluminous Stars

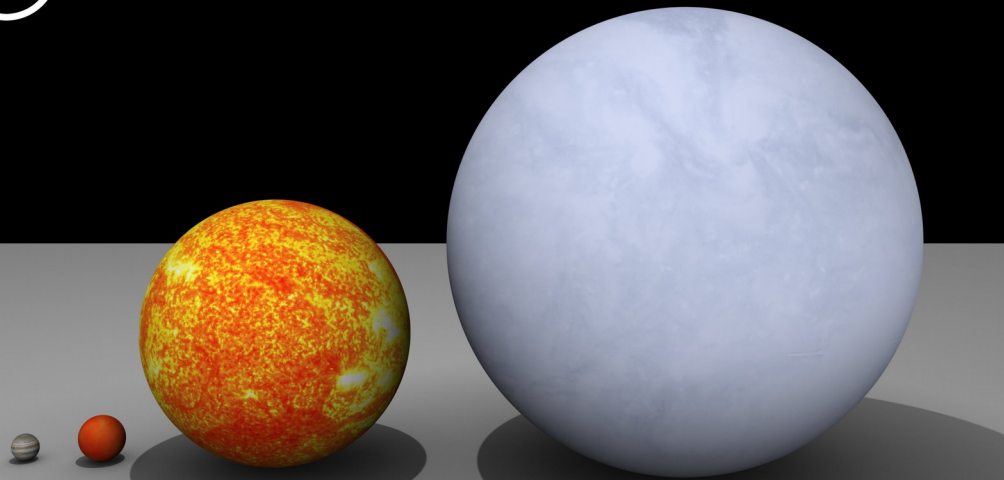
① Mercury < Mars < Venus < Earth



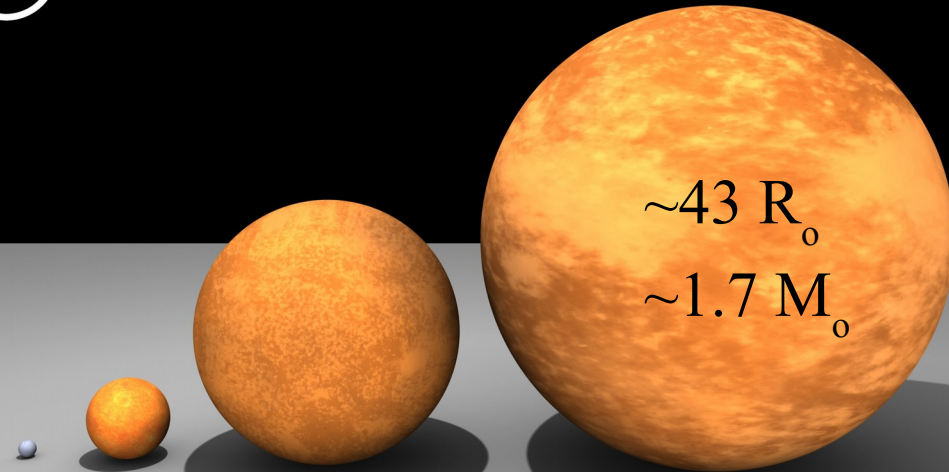
② Earth < Neptune < Uranus < Saturn < Jupiter



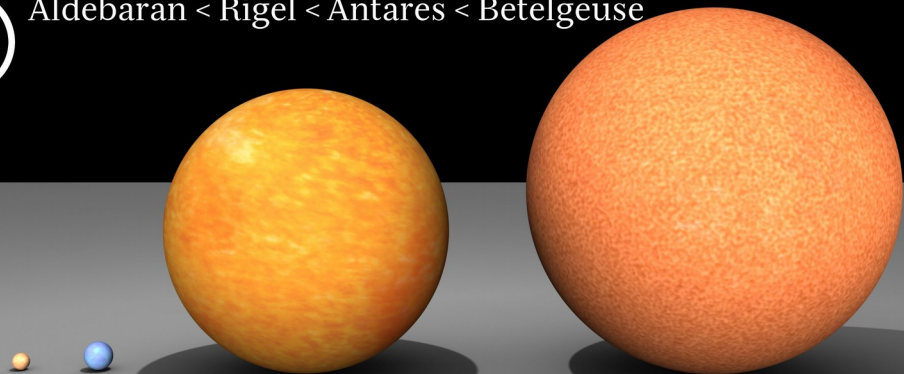
③ Jupiter < Wolf 359 < Sun < Sirius



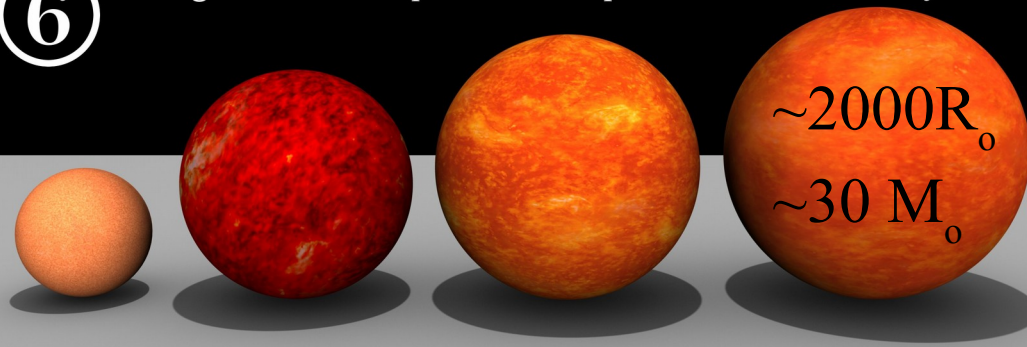
④ Sirius < Pollux < Arcturus < Aldebaran



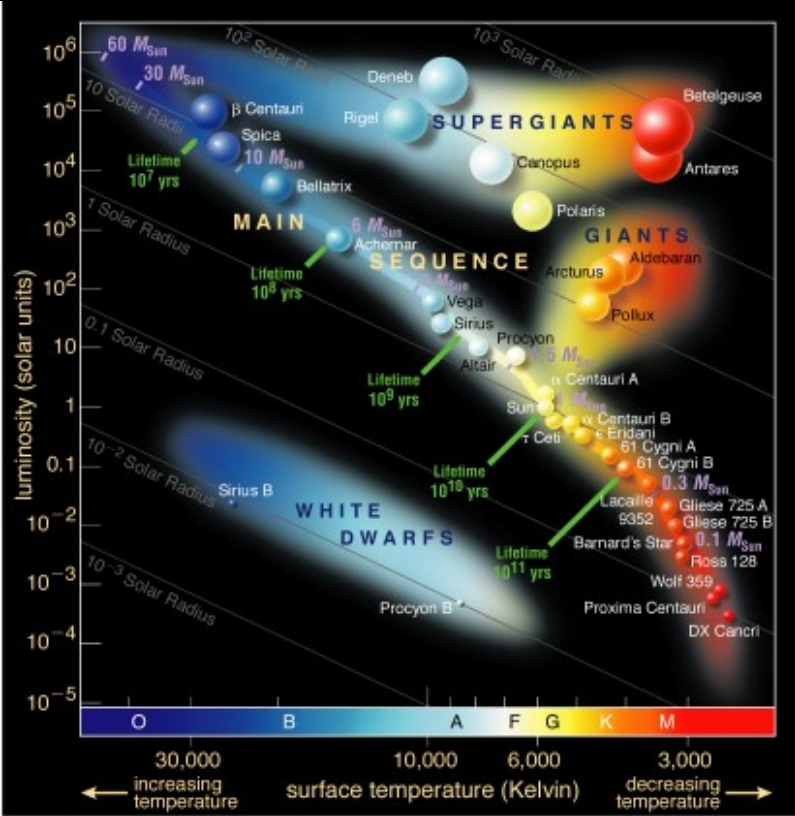
⑤ Aldebaran < Rigel < Antares < Betelgeuse



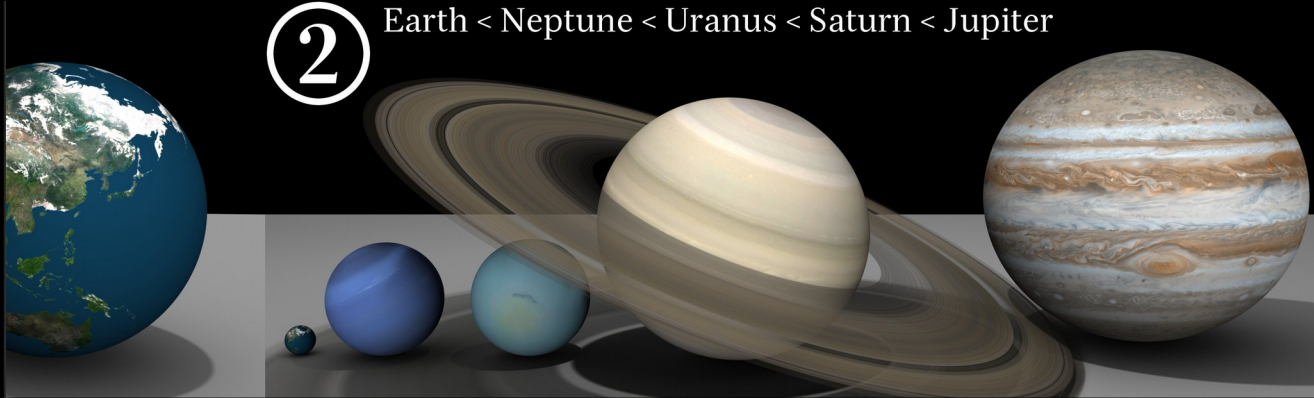
⑥ Betelgeuse < Mu Cephei < VV Cephei A < VY Canis Majoris



The Most Voluminous Stars

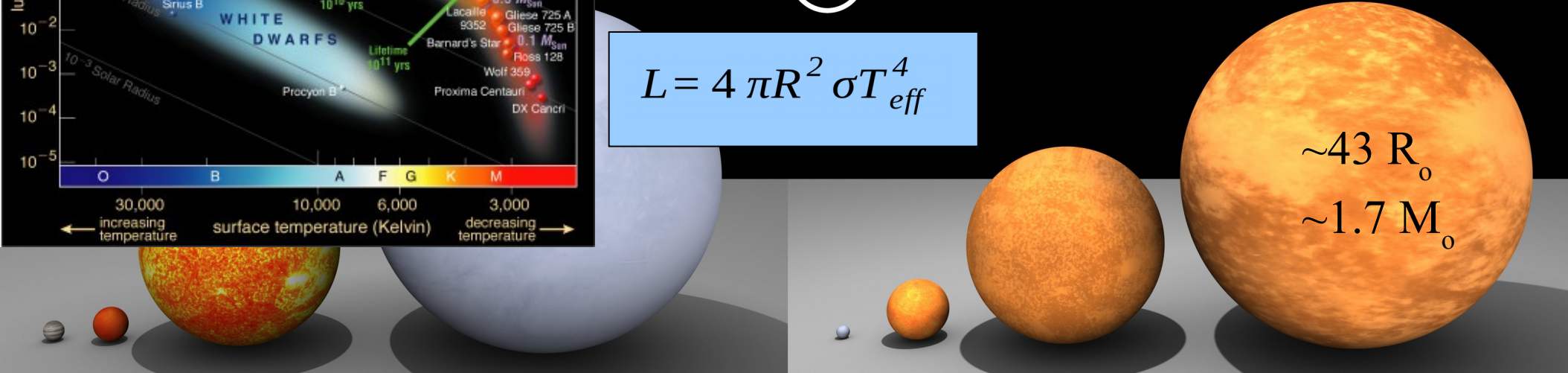


② Earth < Neptune < Uranus < Saturn < Jupiter

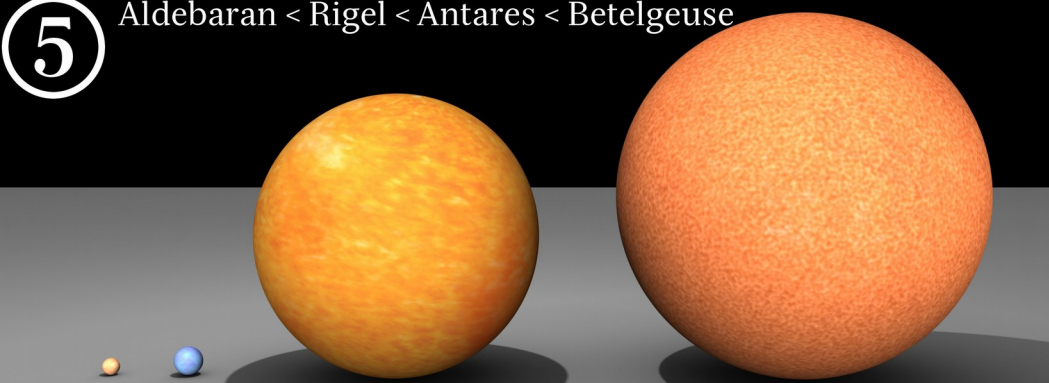


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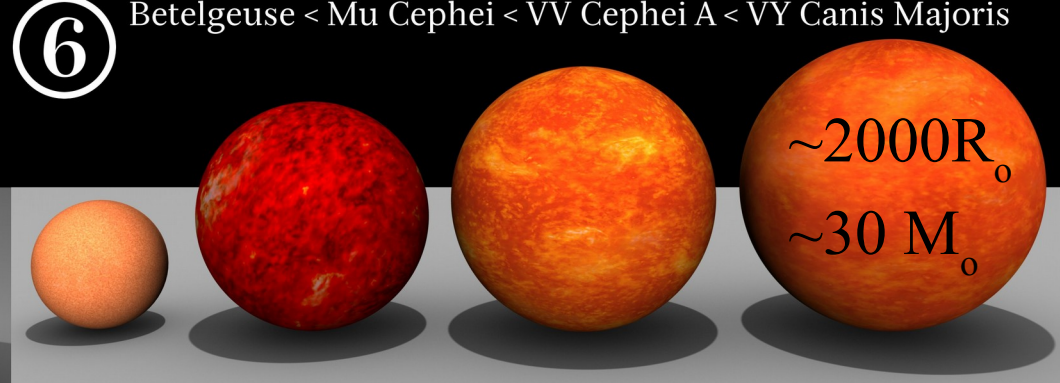
$$L = 4 \pi R^2 \sigma T_{eff}^4$$



⑤ Aldebaran < Rigel < Antares < Betelgeuse



⑥ Betelgeuse < Mu Cephei < VV Cephei A < VY Canis Majoris



Goals of Stellar Evolution Theory

- Explain observed properties of stars and stellar populations using known laws of physics
- Explain and predict evolution and fate of stars
- Explain and predict radiative, chemical and mechanical impact of stars on environment (e.g. galaxies)
- Study physics under extreme conditions not found in the laboratory (plasma/nuclear physics)
- Study early Universe (e.g. EMP stars, GRBs)

Stellar Structure Equations

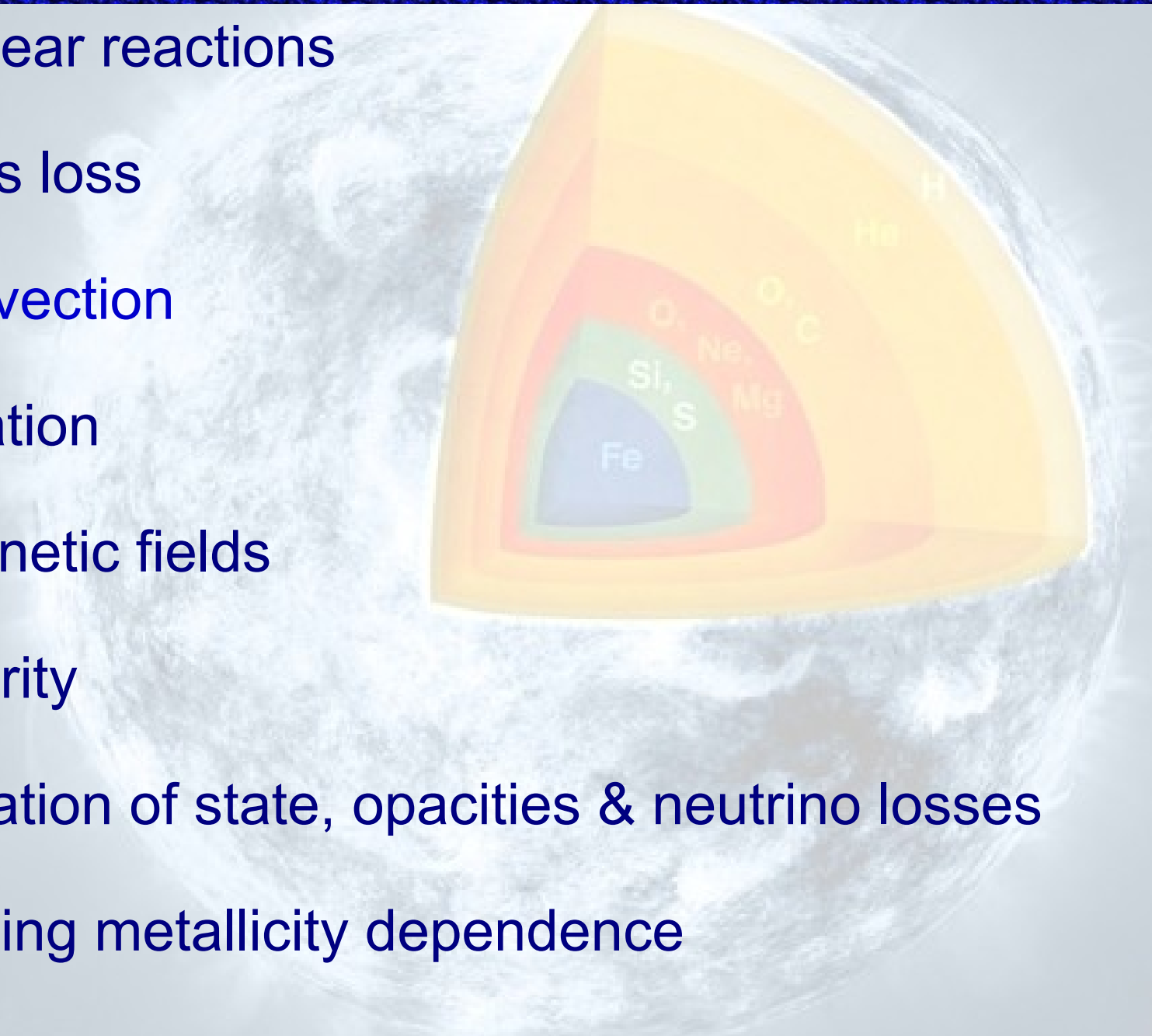
The four structure equations to be solved are:

$$\begin{aligned}\frac{\partial r}{\partial m} &= \frac{1}{4\pi r^2 \rho} \\ \frac{\partial P}{\partial m} &= -\frac{Gm}{4\pi r^4} - \frac{1}{4\pi r^2} \frac{\partial^2 r}{\partial t^2} \\ \frac{\partial L_r}{\partial m} &= \epsilon_n - \epsilon_\nu - c_P \frac{\partial T}{\partial t} + \frac{\delta}{\rho} \frac{\partial P}{\partial t} \\ \frac{\partial T}{\partial m} &= -\frac{GmT}{4\pi r^4 P} \nabla\end{aligned}$$

(Assuming spherical symmetry: one-dimensional model)

Physical Ingredients

- Nuclear reactions
- Mass loss
- Convection
- Rotation
- Magnetic fields
- Binararity
- Equation of state, opacities & neutrino losses
including metallicity dependence



Geneva Stellar Evolution Code

1.5D hydrostatic code (Eggenberger et al 2008)

Rotation: (Maeder & Meynet 2008)

Centrifugal force: **KEY FOR GRB prog.**

Mass loss: enhanced and anisotropic

Mixing: meridional circ. & shear

Mass loss dep. on Z & Ω

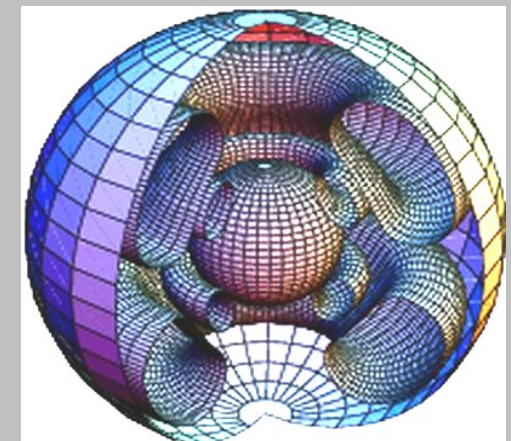
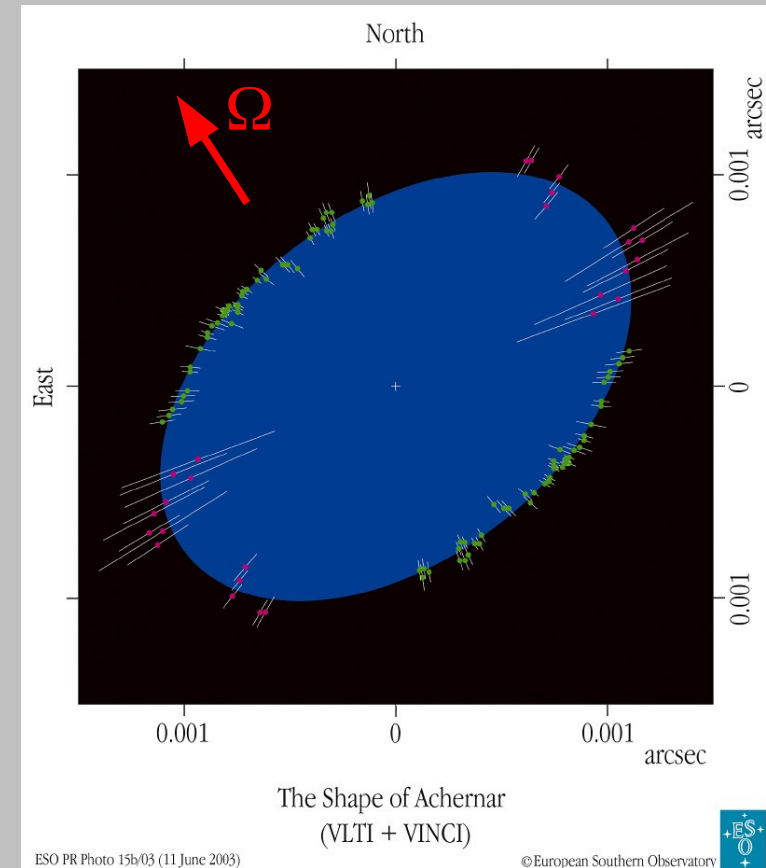
Convection: Schwarzschild + $0.1 H_p$

Large nuclear reaction network: rates from NACRE/reaclib \rightarrow s process (600-700 isotopes)!

B-fields (Spruit 02, Maeder 05),

see also α - Ω dyn. models by Potter et al 2012

Models ZAMS until Silicon burning



Meynet & Maeder 2000

Evolution of Surface Properties

Main sequence:

hydrogen burning

After Main Sequence:

Helium burning

Low and intermediate-mass stars:

MS \rightarrow RG \rightarrow HB/RC \rightarrow AGB \rightarrow WD

Massive stars:

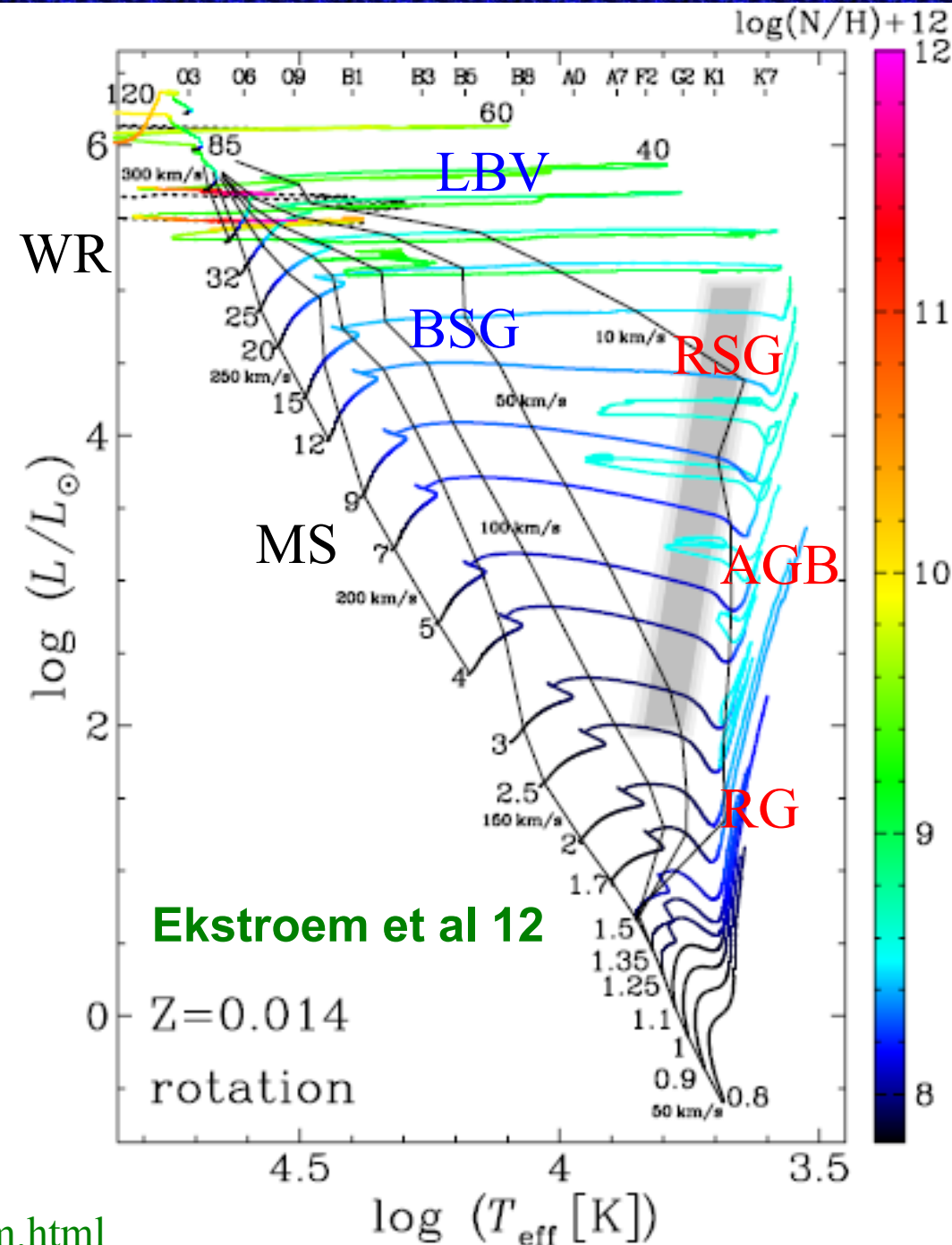
Supergiant stage (red or blue)

Wolf-Rayet (WR): $M > 20\text{-}25 M_{\odot}$

WR without RSG: $M > 40 M_{\odot}$

Advanced stages: C, Ne, O, Si

\rightarrow iron core \rightarrow SN/NS/BH



Evolution of Surface Properties

Main sequence:

hydrogen burning

After Main Sequence:

Helium burning

Low and intermediate-mass stars:

Animations

MS → RG → HB/RC → AGB → WD

Massive stars:

Supergiant stage (red or blue)

Wolf-Rayet (WR): $M > 20-25 M_{\odot}$

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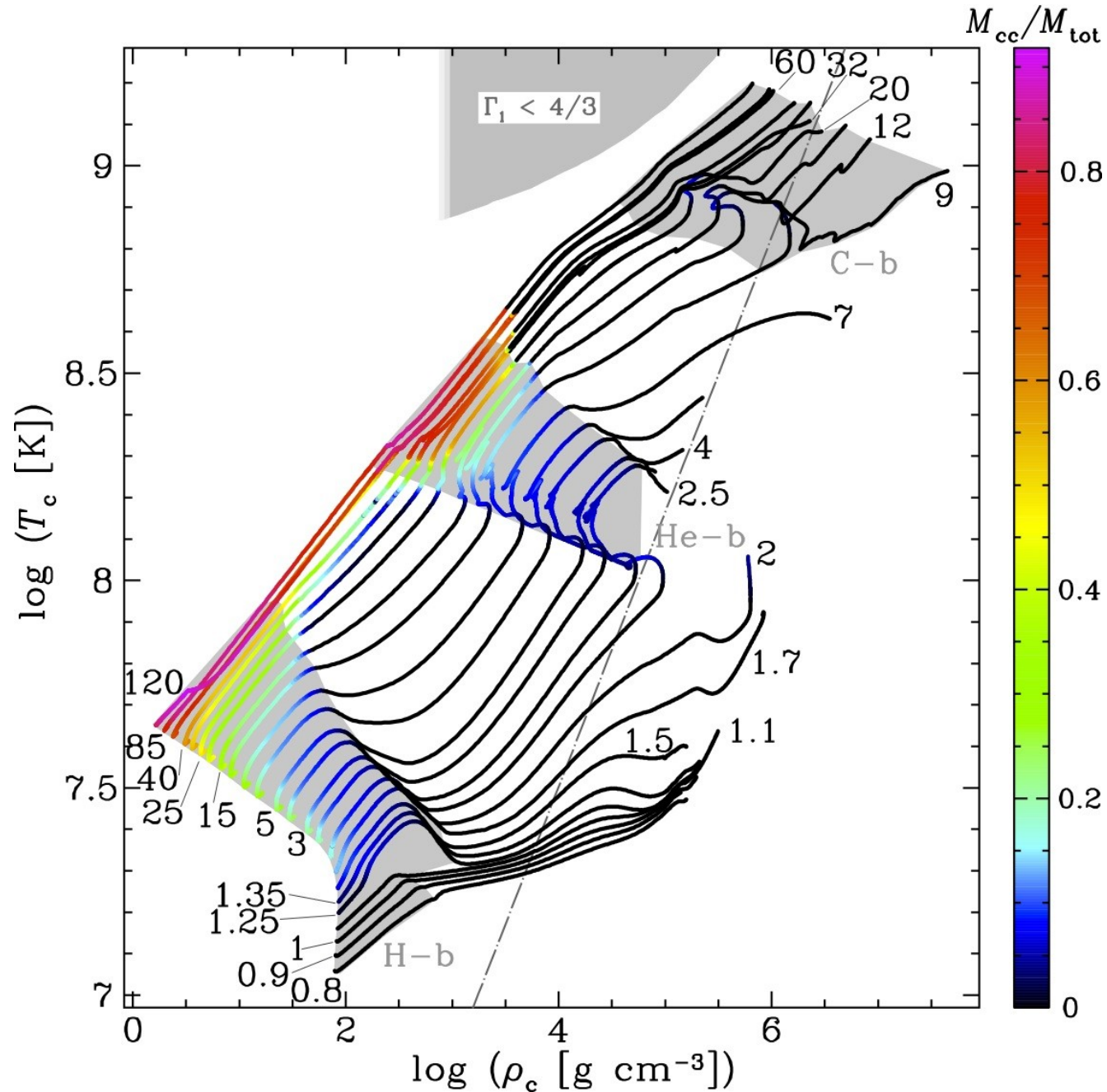
→ iron core → SN/NS/BH

<http://www.astro.keele.ac.uk/~hirschi/animation/anim.html>

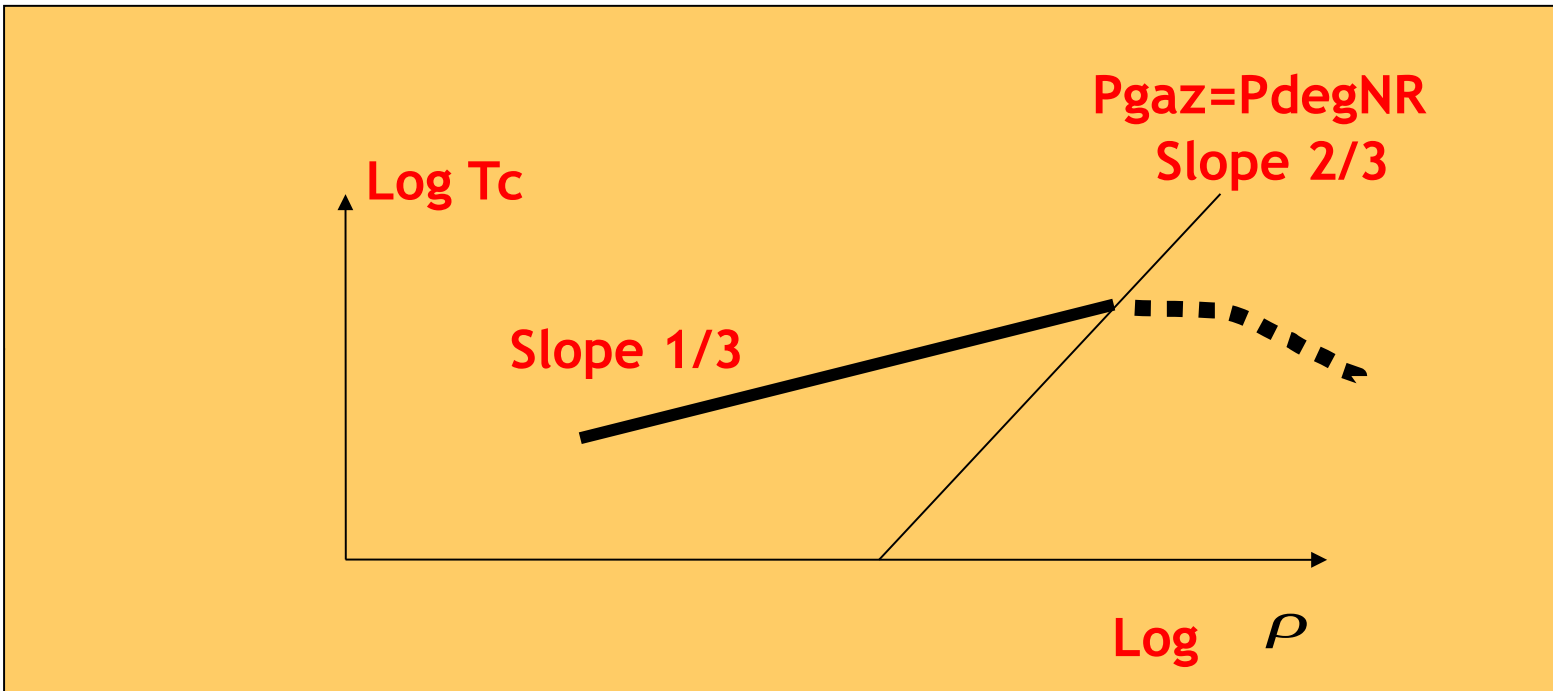
Central Temperature vs Central Density Diagram

Evolution of central properties

What is the slope of the evolutionary tracks?



Evolution of the temperature and density at the centre

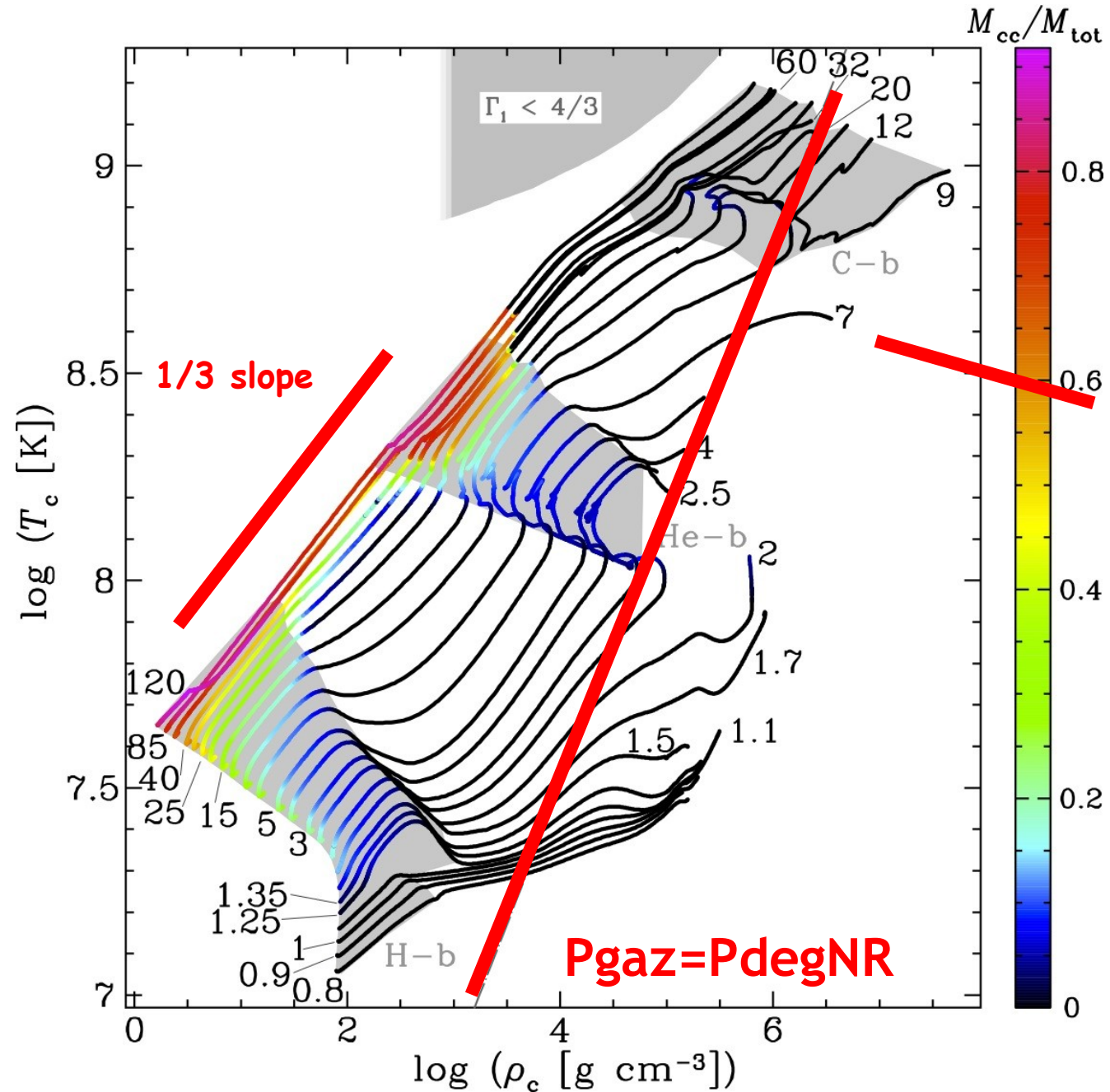


$P_{\text{gaz}} = P_{\text{degNR}}$

$$\frac{k}{\mu m_H} \rho T = K_1 \left(\frac{\rho}{\mu e} \right)^{5/3} \rightarrow T = K_1 \frac{\mu m_H}{k} \frac{1}{\mu_e^{5/3}} \rho^{2/3}$$

Non → Degenerate Conditions

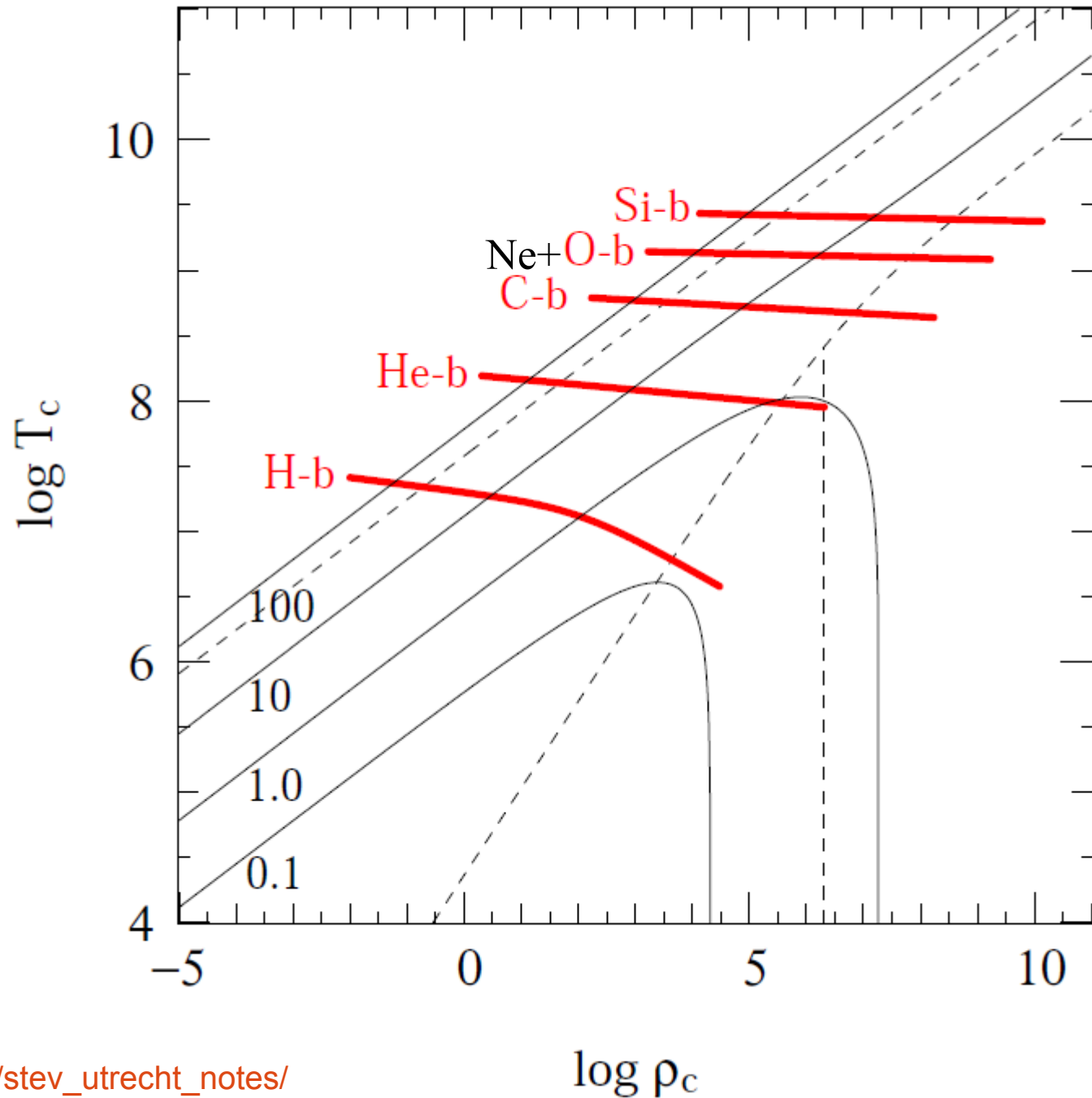
Evolution of central
properties



Ekström et al. (2012)
A&A, 537, A146

Mass Domains

$$\epsilon_{\text{nuc}} = \epsilon_0 \rho^\lambda T^\nu$$



Mass Domains

Stars: radiate energy produced internally & are bound by their own gravity

- $0.08 M_{\text{sun}}$ inferior mass limit for core H-burning : **Brown Dwarfs**
- $0.08 M_{\text{sun}} - 0.5M_{\text{sun}}$: H burning OK, degenerate before core He-burning (lifetime $>$ Hubble time \rightarrow no He white dwarf from single stars)
- $0.5-7M_{\text{sun}}$: core H OK, core He OK (He-flash below $1.8 M_{\text{sun}}$), degenerate CO white dwarf
- $7-9 M_{\text{sun}}$: Core C burning OK \rightarrow WD(?) or Complete destruction (?) or collapse through electron captures (?)
- $9 - 150 M_{\text{sun}}$: core H, He, C, Ne, O, Si \rightarrow Fe cores
- $150-250 M_{\text{sun}}$: Pair Creation/instability Supernovae

Massive Stars: Evolution of the chemical composition

Burning stages (lifetime [yr]):

Hydrogen (10^{6-7}): ${}^1\text{H} \rightarrow {}^4\text{He}$

& ${}^{12}\text{C}, {}^{16}\text{O} \rightarrow {}^{14}\text{N}$

Helium (10^{5-6}): ${}^4\text{He} \rightarrow {}^{12}\text{C}, {}^{16}\text{O}$

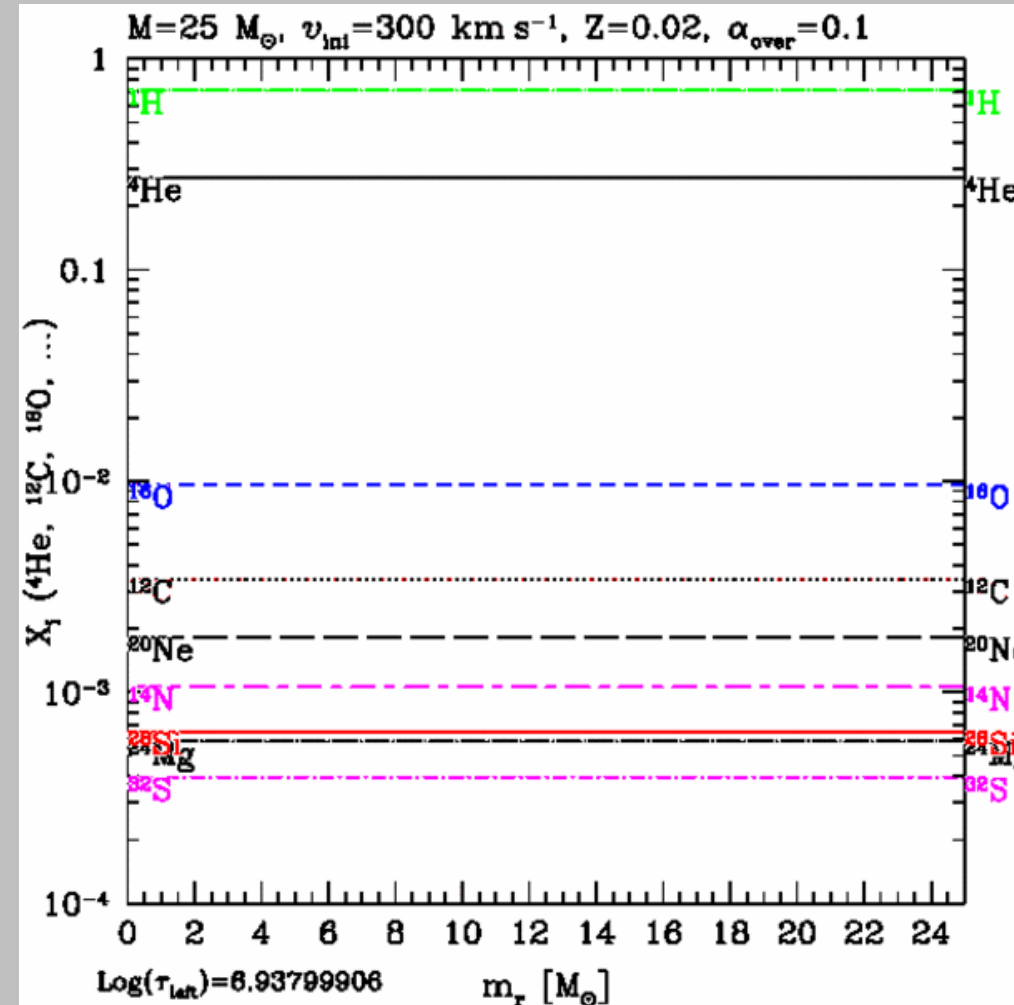
& ${}^{14}\text{N} \rightarrow {}^{18}\text{O} \rightarrow {}^{22}\text{Ne}$

Carbon (10^{2-3}): ${}^{12}\text{C} \rightarrow {}^{20}\text{Ne}, {}^{24}\text{Mg}$

Neon (0.1-1): ${}^{20}\text{Ne} \rightarrow {}^{16}\text{O}, {}^{24}\text{Mg}$

Oxygen (0.1-1): ${}^{16}\text{O} \rightarrow {}^{28}\text{Si}, {}^{32}\text{S}$

Silicon (10^{-3}): ${}^{28}\text{Si}, {}^{32}\text{S} \rightarrow {}^{56}\text{Ni}$

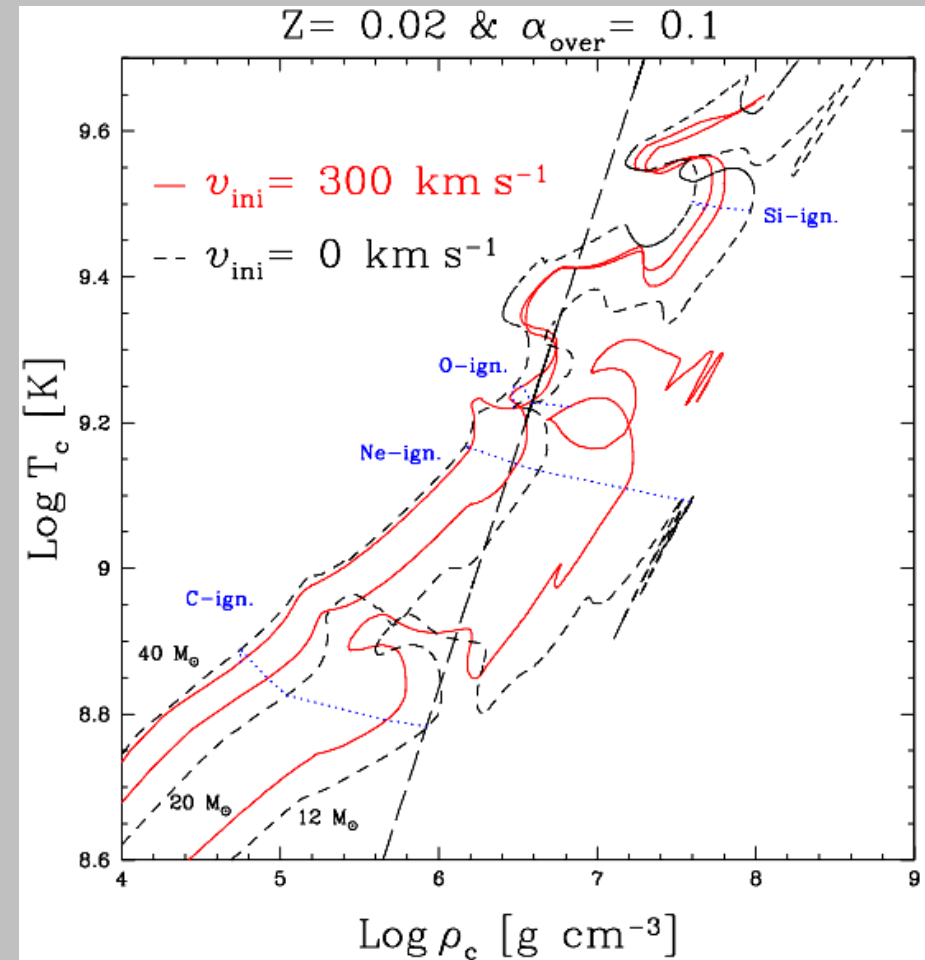
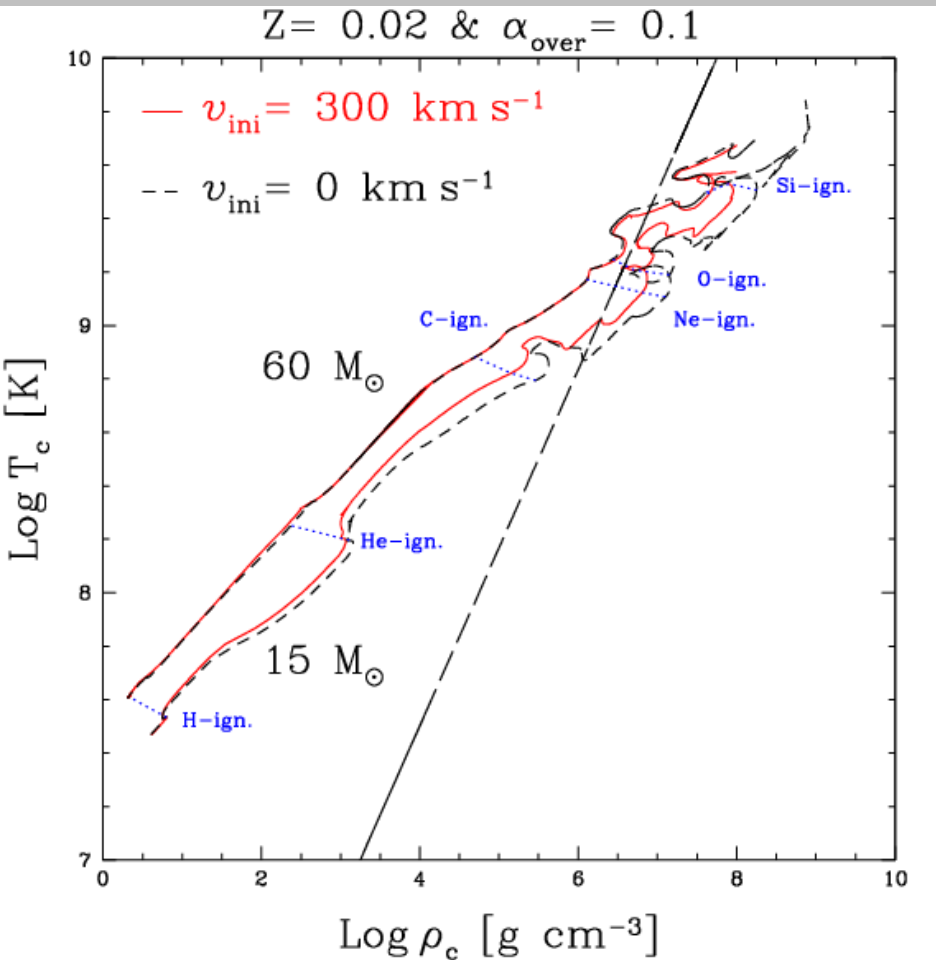


<http://www.astro.keele.ac.uk/~hirschi/animation/anim.html>

Massive Stars

$M < \sim 20 M_{\odot}$: Rotational **mixing** dominates \rightarrow bigger cores

$M > \sim 30 M_{\odot}$: **mass loss** dominates \rightarrow \sim or smaller cores



CO-core mass & C/O ratio: key parameters that determine evolution during late stages

How massive can stars be?

Do very massive stars (VMS: $M > 100 M_{\odot}$) exist?

Very Massive Stars in the Local Universe, 2014, Springer, Ed. Jorick S. Vink

- Star formation: already difficulties with $30 M_{\odot}$ stars but 2/3D simulations are promising (Kuiper et al 11, Krumholz 2014)
- Stellar evolution: possible up to $\sim 1,000 M_{\odot}$ (BUT mass loss/rad.) (Baraffe et al 01)

Can we see them?

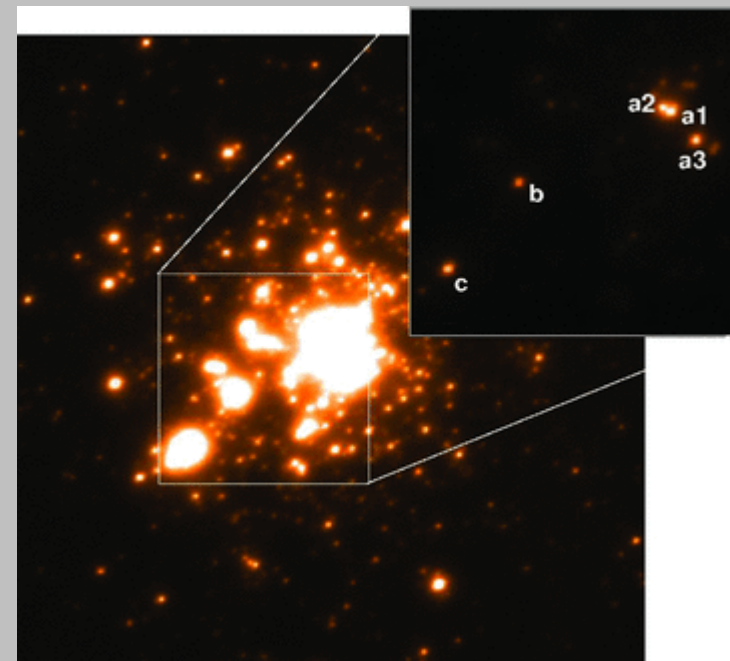
- Rare and short-lived
- Need to look at youngest and most massive clusters:

- Arches: $M < \sim 150 M_{\odot}$

(Figer 05, Martins et al 08)

- NGC 3603 & R136: new $M_{\max} = 320 M_{\odot}!$

(Crowther et al 10, MNRAS)



R136 cluster

Mass Loss: Types, Driving & Recipes

Mass loss driving mechanism and prescriptions for different stages:

- O-type & “LBV” stars (bi-stab.): line-driven Vink et al 2000, 2001
- WR stars (clumping effect): line-driven Nugis & Lamers 2000, Gräfener & Hamann (2008)
- RSG: Pulsation/dust? de Jager et al 1988
- RG: Pulsation/dust? Reimers 1975,78, with $\eta \sim 0.5$
- AGB: Super winds? Dust Bloeker et al 1995, with $\eta \sim 0.05$
- LBV eruptions: continuous driven winds? Owocki et al
- ...

What changes at low Z?

- Stars are **more compact**: $R \sim R(Z_0)/4$ (lower opacities) at $Z=10^{-8}$
- Rotation at low Z: stronger shear, weaker mer. circ.
- Mass loss weaker at low Z: \rightarrow faster rotation

$$\dot{M}(Z) = \dot{M}(Z_0) \left(Z/Z_0 \right)^\alpha$$

- $\alpha = 0.5-0.6$ (Kudritzki & Puls 00, Ku02)

(Nugis & Lamers, Evans et al 05)

- $\alpha = 0.7-0.86$ (Vink et al 00,01,05)

$$Z(\text{LMC}) \sim Z_0/2.3 \Rightarrow \dot{M}/1.5 - \dot{M}/2$$

$$Z(\text{SMC}) \sim Z_0/7 \Rightarrow \dot{M}/2.6 - \dot{M}/5$$

Mass loss at low Z still possible?

RSG (and LBV?): no Z-dep.; CNO? (Van Loon 05, Owocky et al)

Mechanical mass loss \leftarrow critical rotation/ Eddington limit

(e.g. Hirschi 2007, Ekstroem et al 2008, Yoon et al 2012)

The fate of VMS: PCSN/BH/CCSN?

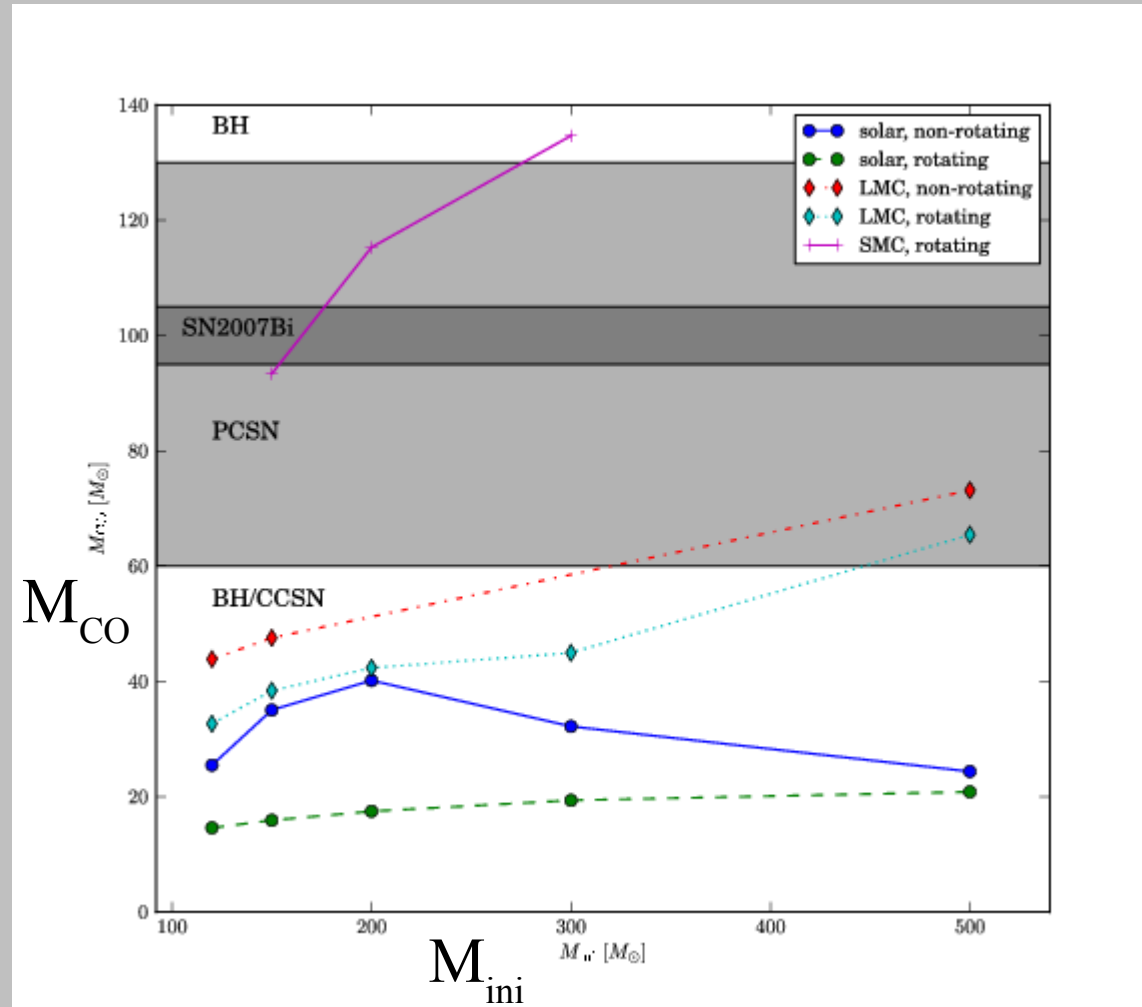
(Yusof et al 13 MNRAS, aph1305.2099)

Z_{solar} : no PCSN

(Rotating) models with $Z < Z(\text{LMC})$ lose less mass,

and enter the PCSN instability region!

BUT mass loss uncertain!



PCSN range from Heger & Woosley (2002)

Consistent with Langer et al (2007): PCSN for $Z < Z_{\odot} / 3$

Key Open Questions Concerning Mass Loss

- Mass loss in cool parts of HRD: LBV & RSG, especially at low Z
- Position in & evolution across HRD: effects of rotation-induced mixing, feedback from mass loss [Yusof et al 13](#), [Langer 07](#), [Sanyal et al 15](#), [Kohler et al 15...](#)
- **Mass loss near Eddington limit** [Graefener & Hamann 08](#), [Vink et al 11](#), ...
- Importance of clumping, porosity, inflation [Fullerton et al 06](#), [Graefener et al. 12](#), [Vink et al](#), ...
- Which stars may explode in the LBV phase? [Smith et al 11](#), ... , [Vink et al](#), ...
- Look of WR stars: radius, spectra [Graefener et al. 2012](#), [Groh et al 2013-...](#)
- Additional mass loss mechanisms? Critical rotation at low Z ? Shell mergers in late phases of evolution? ... [Hirschi 2007](#), [Meynet et al 2006](#), ... , [Smith & Arnett 2014](#), ...
- ...

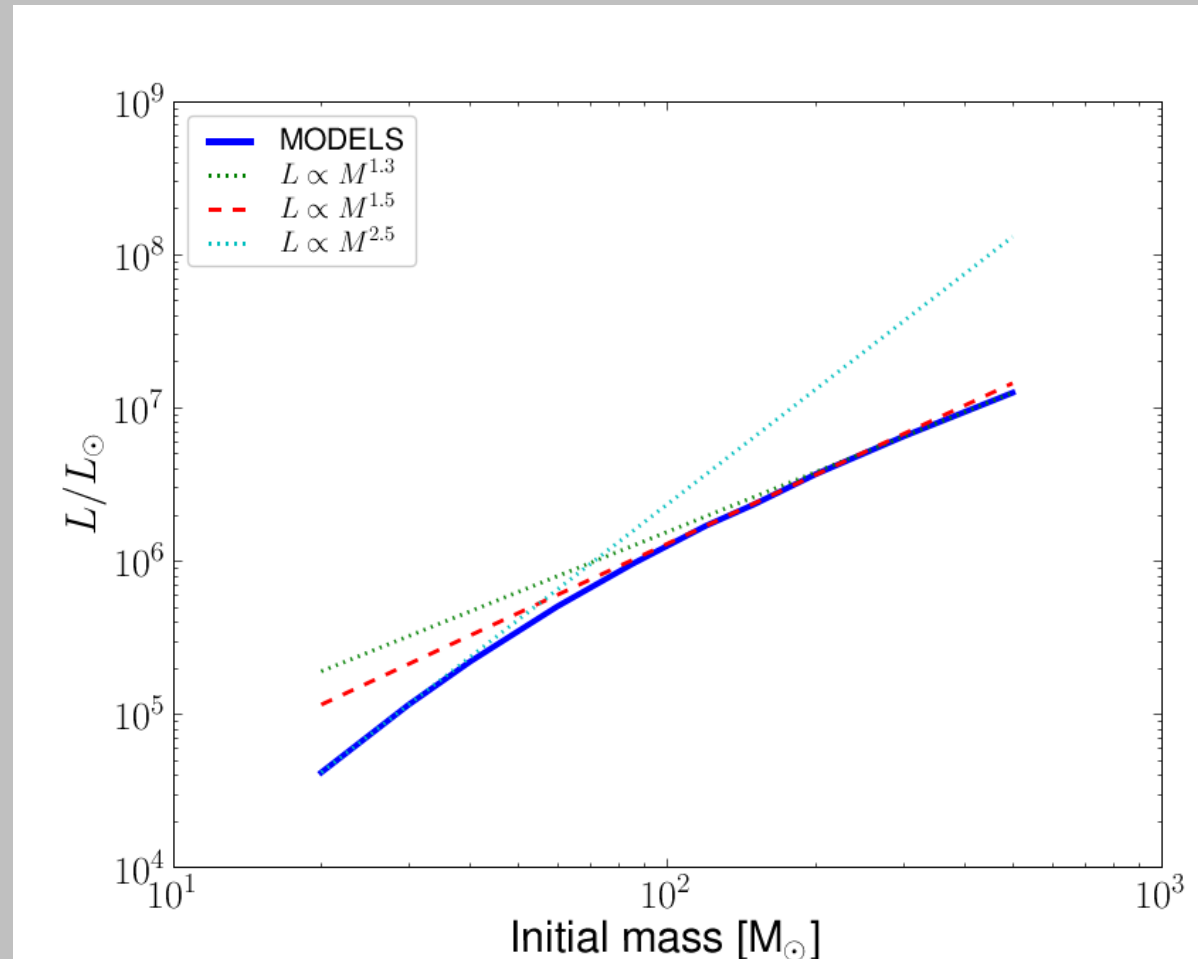
Very Massive Stars are Very Luminous ($\sim 10^7 L_{\odot}$)

R136a1 ($10^7 L_{\odot}$) alone supplies 7% of the ionizing flux of the entire 30 Doradus region!

What is the shape of the luminosity vs mass relation in this mass range?

Textbooks: $L \sim M^3$ for stars in the solar mass range

Above $100 M_{\odot}$: $L \sim M^{1.5}$



Very Massive Stars, $M > 100 M_{\text{sun}}$

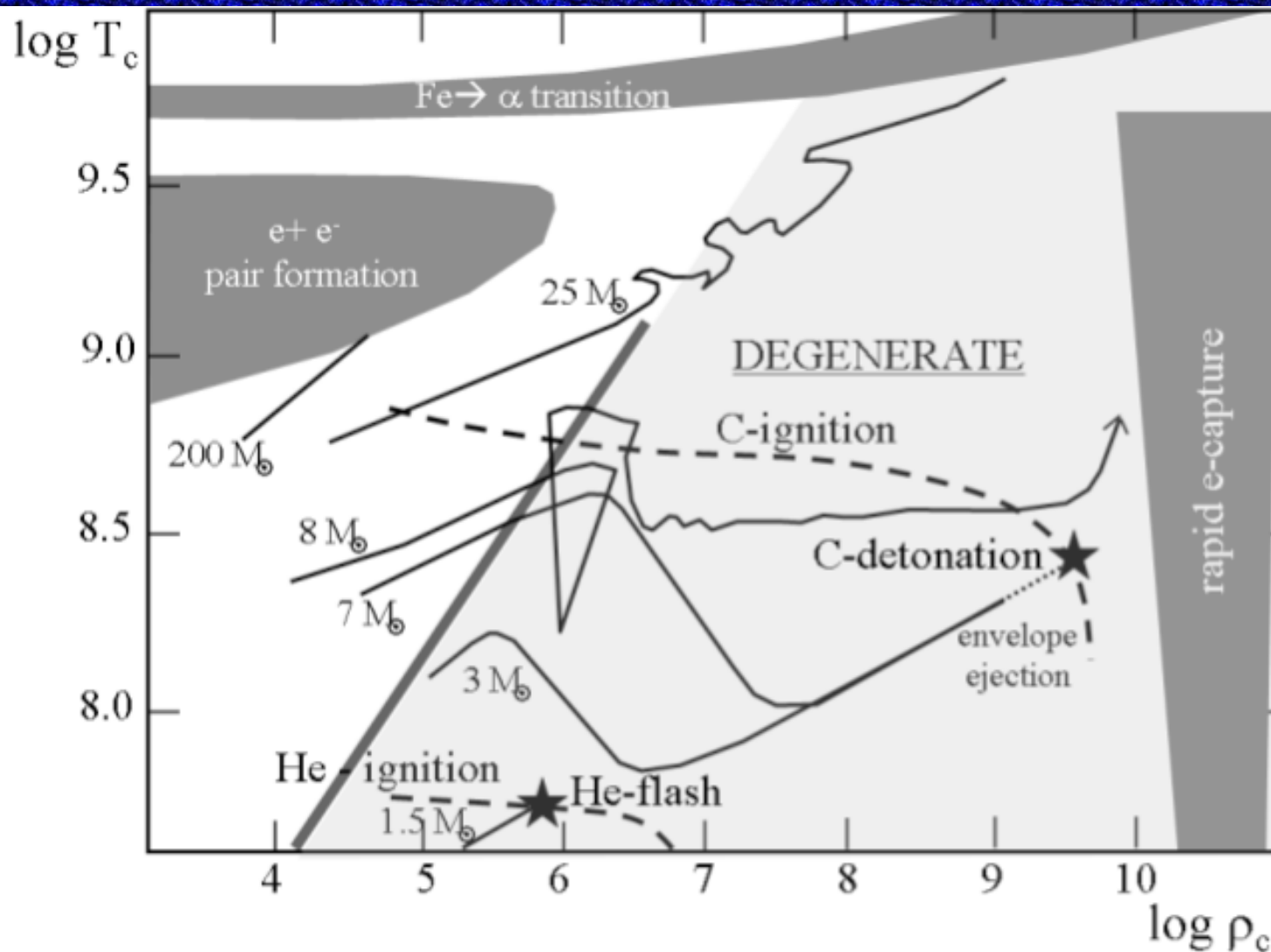
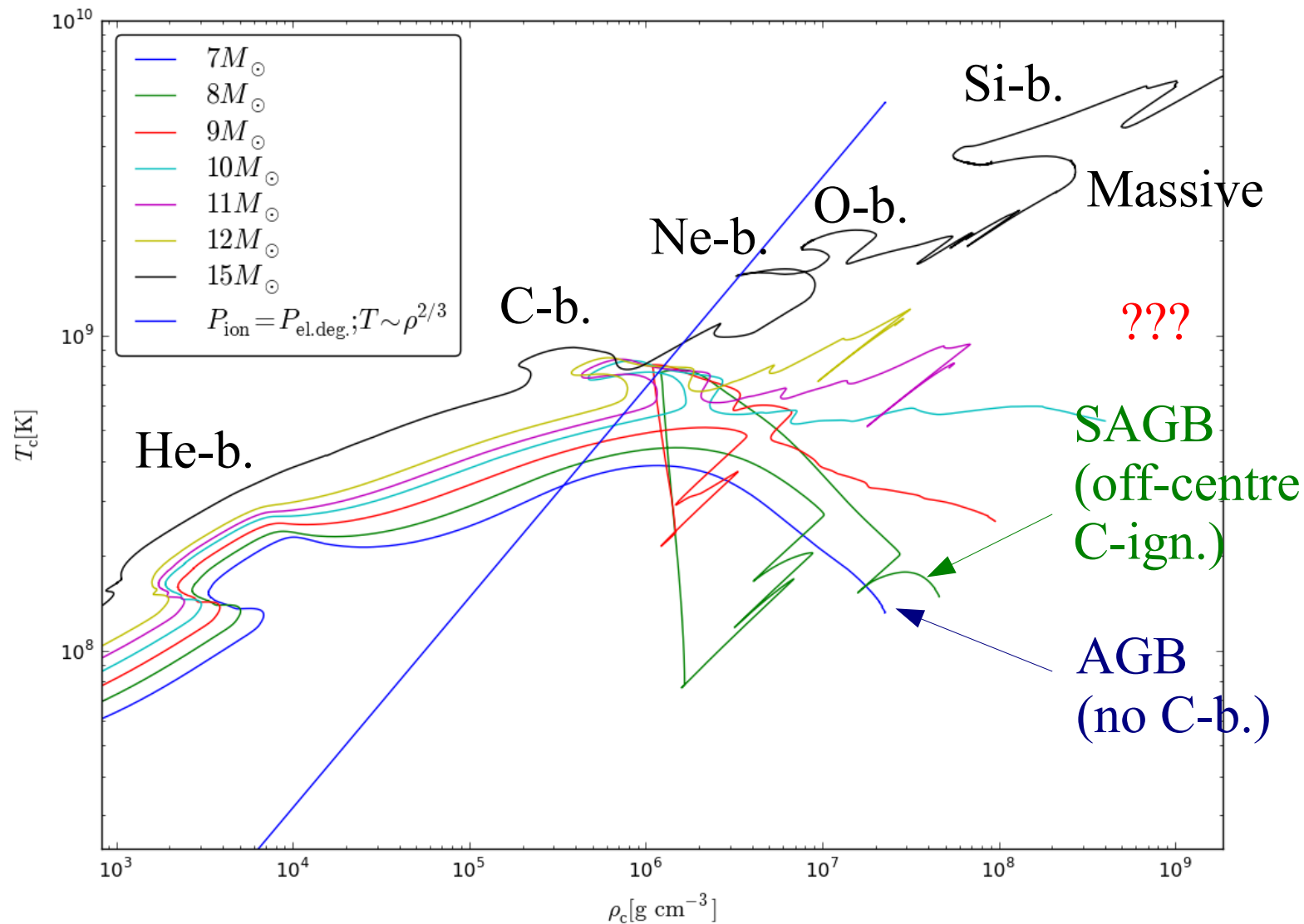


Fig. 26.10. Evolution of central conditions for different masses with indications of instability domains (Sect. 7.8), the Fe- α transition indicates the photodesintegration of Fe nuclei into α particles. The degenerate region is light gray. Dashed lines show the place where nuclear energy generation rates balance neutrino losses. Adapted from T.J. Mazurek and J.C. Wheeler [401]

Massive/AGB Stars Transition

7-15 M_{\odot} models ← MESA stellar evolution code: <http://mesa.sourceforge.net/>

Paxton et al 10

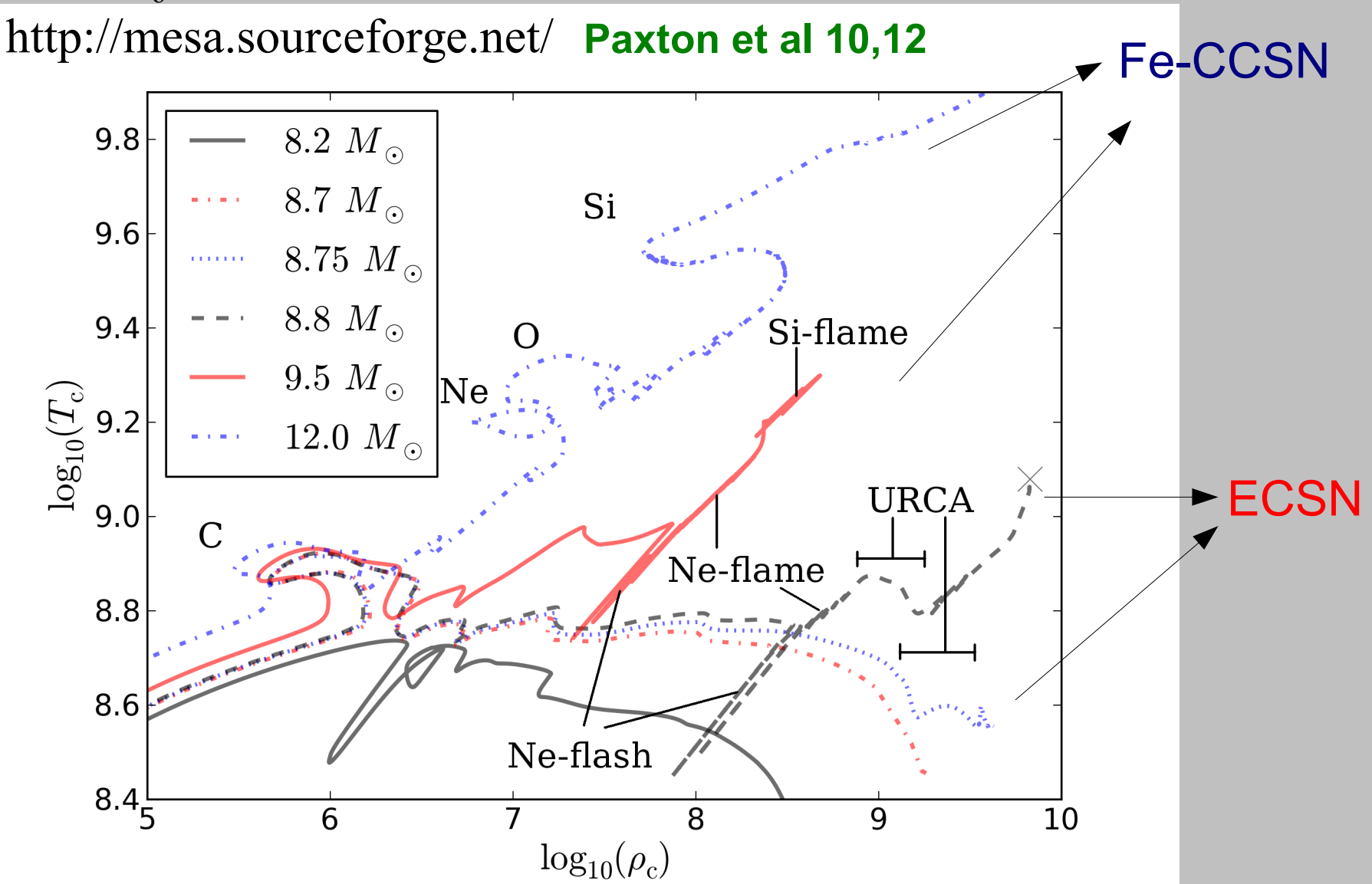


Jones et al 2013; Takahashi et al 13; see also Mueller et al 12, Umeda et al 12

Fate of Least-Massive MS: ECASN/Fe-CCSN?

7-15 M_{\odot} models ← MESA stellar evolution code:

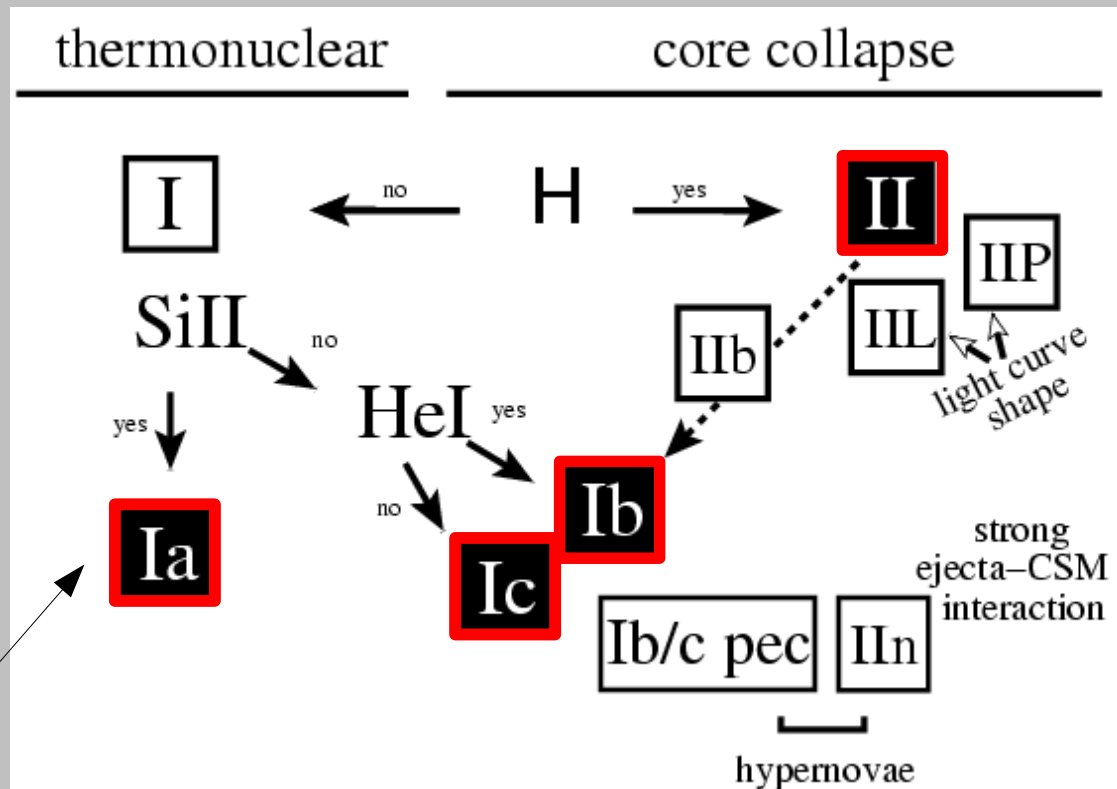
<http://mesa.sourceforge.net/> Paxton et al 10,12



Both SAGB and failed massive stars may produce ECASN

Supernova Explosion Types

Massive stars: → **SN II** (H envelope),
Ib (no H), **Ic** (no H & He) ← WR

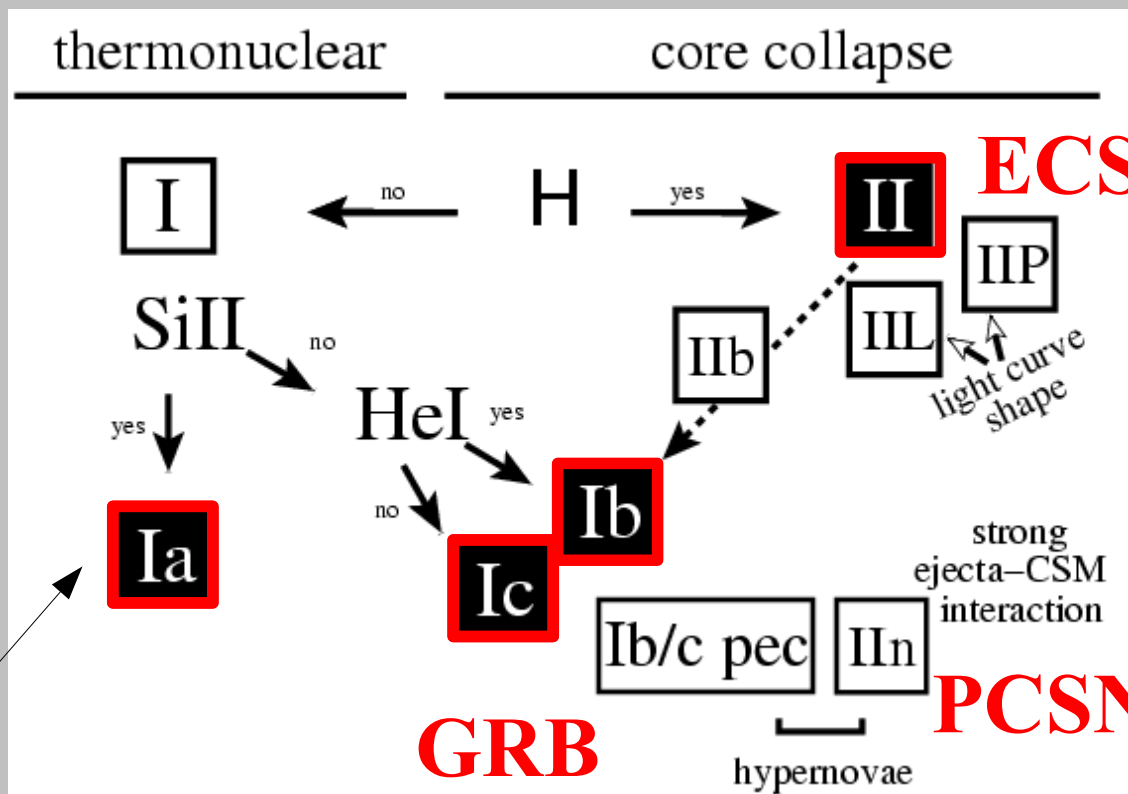


White dwarfs (WD):
 in binary systems
 Accretion →
 Chandrasekhar
 mass → SN Ia

(Turatto 03)

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ECSN?

White dwarfs (WD):
 in binary systems
 Accretion →
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GRB

PCSN(=PISN)?

(Hirschi+05
 Woosley+06
 Yoon+06, ...)

(Turatto 03)

Recent work

- Massive stars and the (not always) weak s process:

Large grid of massive star models + weak s proc (Frischknecht+2016, MNRAS):

Nugrid: set 1 (Pignatari+2016, ApJ), set1extension (Ritter+in subm.),

(main) s process with new convective boundary mixing (CBM): (Battino+ ApJ 2016)

- Nuclear uncertainties: MC-based sensitivity studies for gamma-process (Rauscher+2016, MNRAS), weak s process (Nishimura+2017, MNRAS), main s process (Cescutti+in prep)

- Stellar uncertainties:

Multi-D tests of convection (Cristini+ 2017, MNRAS) and rotation (Edelmann+2017, A&A)

- Reviews/book chapters: Springer Handbook of Supernovae

“Pre-supernova Evolution and Nucleosynthesis in Massive Stars and Their Stellar Wind Contribution”

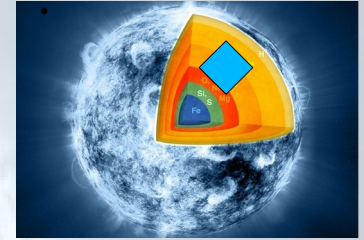
(doi:10.1007/978-3-319-20794-0_82-1)

“Very Massive and Supermassive Stars: Evolution and Fate” (doi:10.1007/978-3-319-20794-0_120-1)

- ChETEC COST Action started in April 2017: see www.chetec.eu for details

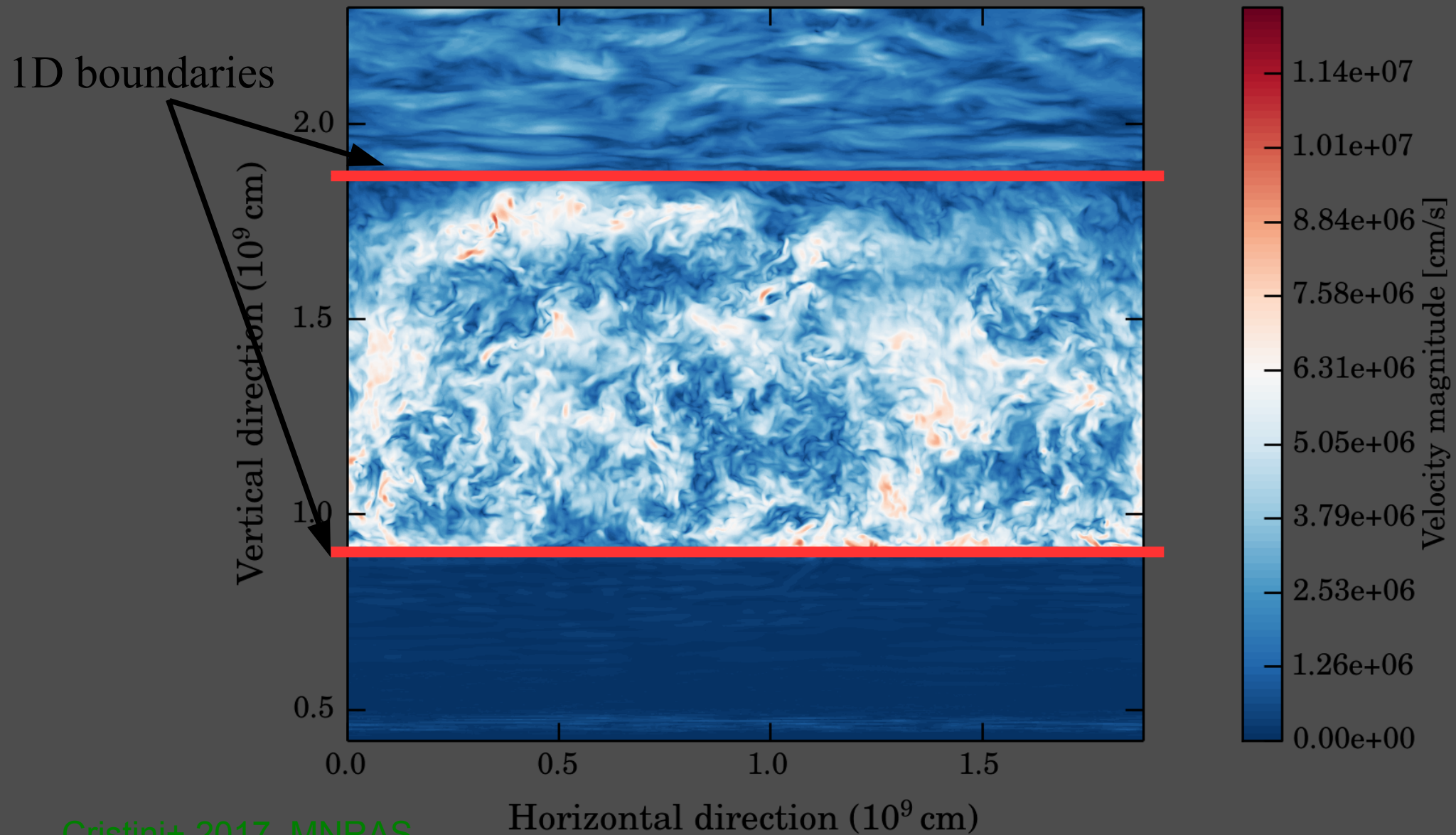
C-shell Setup & Approximations

- PROMPI code Meakin, Arnett et al 2007-...
- Initial conditions provided by stellar model from GENEC:
15M_☉, non-rotating at solar metallicity (see previous slide)
- “Box in a star” (plane-parallel) simulation using Cartesian co-ordinates
- Parameterised gravitational acceleration and ¹²C+¹²C energy generation rate
(energy rate boosted by a factor of 1000 for parameter study)
- Radiative diffusion neglected
- Turbulence initiated through random low-amplitude perturbations in temperature and density
- Constant abundance of ¹²C fuel over simulation time
- 4 resolutions: lrez: 128³, mrez: 256³, hrez: 512³, vhref: 1024³



3D C-shell Simulations

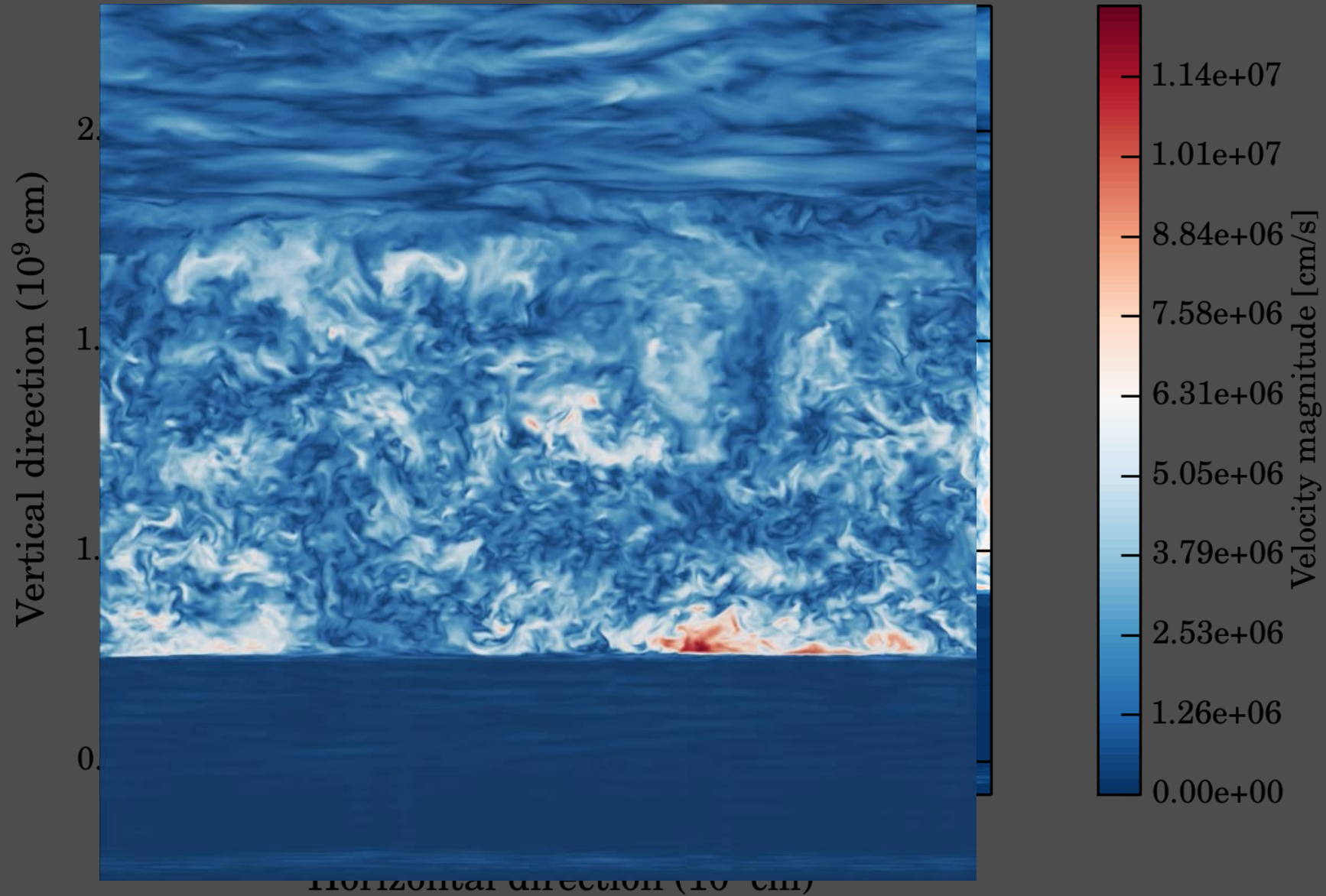
Snapshot from 1024^3 resolution run: Gas Velocity $\|v\|$



3D C-shell Simulations: $|v|$ movie

Cristini+ 2017, MNRAS

Gas Velocity $\|v\|$



3D C-shell Simulations

Snapshot from 1024^3 resolution run: Gas Velocity $\|\mathbf{v}\|$

